Leptoquark induced rare decay amplitudes $h \rightarrow \tau^{\mp} \mu^{\pm}$ and $\tau \rightarrow \mu \gamma$

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arXiv:[hep-ph] 1508.01897

NCTS Annual Theory Meeting 2015, Dec.09-12



- Introduction
- Leptoquark interactions
- Amplitudes $\tau \to \mu \gamma$ and $h \to \tau^{\mp} \mu^{\pm}$
- Physics possibilities
- Concluding Remarks



Introduction

- The width of 125 GeV Higgs is about 4 MeV. Rare decay from new physics can have measurable branching fraction.
- CMS lepton flavor violation(LFV) decay of Higgs. CMS: Br $(h \rightarrow \tau^{\mp} \mu^{\pm}) = 0.84^{+0.39}_{-0.37}$ %, excess 2.4 σ ATLAS: Br $(h \rightarrow \tau^{\mp} \mu^{\pm}) = 0.77 \pm 0.62$ %
- Rare decay constraint

 $Br(\tau \rightarrow \mu \gamma) < 4.4 \times 10^{-8}$ at 90% C.L. from BaBar experiment

CMS collaboration, Phys. Lett. B749 (2015) 337-362 ATLAS collaboration, arXiv [hep-ex]:1508.03372 BaBar collaboration, Phys. Rev. Lett. 104, 021802 (2010)



- We motivated by leptoquark(LQ) associated with 3rd generation, a top quark mass insertion in the loop diagrams.
- LQ gives amplitude for $\ au o \mu \gamma$.
- Cancellation between two types of LQ for $\tau \to \mu \gamma$, leave detectable rate for $h \to \tau^{\mp} \mu^{\pm}$.



- We associate the new LQs with the top quark of 3rd generation.
- Mass insertion of top enhance the LFV Higgs decay mode.
- Under electroweak gauge symmetry, two types of LQs

$$\chi^{1/3}: SU(2) \text{ singlet}$$

$$\Omega^{T} = (\Omega^{5/3}, \Omega^{2/3}): SU(2) \text{ doublet}$$

$$\mathcal{L} \supset g_{L}^{\tau} \chi^{\frac{1}{3}} (Q_{3})_{L}^{T} \epsilon L_{\tau,L} - g_{R}^{\tau} \chi^{\frac{1}{3}} t_{R} \tau_{R}$$

$$+ g_{L}^{\prime \tau} \Omega^{T} \epsilon \overline{t_{R}} L_{\tau,L} - g_{R}^{\prime \tau} \overline{Q_{3,L}} \tau_{R} \Omega + (\tau \leftrightarrow \mu) + \text{ h.c.}$$

 $g_{L,R}^{\tau,\mu}, g_{L,R}^{\prime\tau,\mu}$ are LQs couplings



Amplitude $\tau \rightarrow \mu \gamma$

• Feynman diagrams from LQs contribution to $\tau \rightarrow \mu \gamma$.





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Amplitude $\tau \rightarrow \mu \gamma$

• Effective operators

$$\begin{split} & L_{\text{eff}} \supset \frac{e}{m_{t}} \Big[\overline{\mu} \sigma^{\alpha\beta} \left(C_{L}L + C_{R}R \right) \tau \Big] F_{\alpha\beta} + \text{h.c.} \\ & C_{R} = \frac{3_{c}}{32\pi^{2}} \Big(g_{R}^{\tau} g_{L}^{\mu} x_{t} H_{1}(x_{t}) + g_{R}^{\tau} g_{L}^{\mu} x_{t}^{\mu} H_{2}(x_{t}^{\prime}) \Big) \\ & C_{L} = \frac{3_{c}}{32\pi^{2}} \Big(g_{L}^{\tau} g_{R}^{\mu} x_{t} H_{1}(x_{t}) + g_{L}^{\tau} g_{R}^{\mu} x_{t}^{\mu} H_{2}(x_{t}^{\prime}) \Big) \\ \end{split}$$

• Partial decay width

$$\Gamma(\tau \to \mu\gamma) = \frac{e^2}{4\pi} m_\tau \left(\frac{m_\tau^2}{m_t^2}\right) \left(\left|C_L\right|^2 + \left|C_R\right|^2\right)$$

$$x_t \equiv m_t^2 / m_\chi^2$$
$$x'_t \equiv m_t^2 / m_\Omega^2$$





• Feynman diagrams from LQs contribution to $h \rightarrow \tau^{\mp} \mu^{\pm}$

Amplitude $h \rightarrow \tau^{\mp} \mu^{\pm}$



 The logarithmic divergence has to be canceled by the one-particle reducible (1PR) diagrams with bubbles in the external lepton lines. Amplitude $h \rightarrow \tau^{\mp} \mu^{\pm}$

• The partial decay width, summing both process $h \to \tau^{\mp} \mu^{\pm}$ is

$$\Gamma\left(h \to \tau^{\mp} \mu^{\pm}\right) = \frac{9}{2048\pi^{5}} m_{h} \left(\frac{m_{t}}{v}\right)^{2}$$
$$\times \left(\left|G_{\chi}g_{R}^{\tau}g_{L}^{\mu} + G_{\Omega}g_{R}^{\prime\tau}g_{L}^{\prime\mu}\right|^{2} + \left|G_{\chi}g_{R}^{\mu}g_{L}^{\tau} + G_{\Omega}g_{R}^{\prime\mu}g_{L}^{\prime\tau}\right|^{2}\right)$$

 G_{χ} and G_{Ω} are loop functions from LQs $\chi^{1/3}$ and $\Omega^{5/3}$ running in the diagrams, respectively.



Amplitude $h \rightarrow \tau^{\mp} \mu^{\pm}$

• Higgs couples to LQs from bosonic interaction $-\lambda_{\chi}H^{\dagger}H\chi^{\dagger}\chi$.

I.Doršner, S.Fajfer, A.Greljo, J.F.Kamenik, N.Košnik and I.Nišandžic, JHEP 1506 (2015) 108.

• The explicit expresses of the loop functions are

 $G_{\chi} = (m_{\chi}^2 + m_t^2)C_0(0, 0, s, m_t^2, m_{\chi}^2, m_t^2) + B_0(s, m_t^2, m_t^2) - B_0(0, m_t^2, m_{\chi}^2) + \lambda_{\chi}v^2C_0(0, 0, s, m_{\chi}^2, m_t^2, m_{\chi}^2)$

 $G_{\Omega} = (m_{\Omega}^2 + m_t^2)C_0(0, 0, s, m_t^2, m_{\Omega}^2, m_t^2) + B_0(s, m_t^2, m_t^2) - B_0(0, m_t^2, m_{\Omega}^2) + \lambda_{\Omega}v^2C_0(0, 0, s, m_{\Omega}^2, m_t^2, m_{\Omega}^2) + B_0(s, m_t^2, m_t^2) - B_0(0, m_t^2, m_{\Omega}^2) + \lambda_{\Omega}v^2C_0(0, 0, s, m_{\Omega}^2, m_t^2, m_{\Omega}^2) + B_0(s, m_t^2, m_t^2) - B_0(0, m_t^2, m_{\Omega}^2) + \lambda_{\Omega}v^2C_0(0, 0, s, m_{\Omega}^2, m_t^2, m_{\Omega}^2) + B_0(s, m_t^2, m_{\Omega$

 B_0 and C_0 are the Passarino-Veltman (PV) function



• Reminding the $\tau \rightarrow \mu \gamma$ and BaBar experimental constraint

$$C_{R} = \frac{3_{c}}{32\pi^{2}} \left(g_{R}^{\tau} g_{L}^{\mu} x_{t} H_{1}(x_{t}) + g_{R}^{\prime \tau} g_{L}^{\prime \mu} x_{t}^{\prime} H_{2}(x_{t}^{\prime}) \right)$$
$$C_{L} = \frac{3_{c}}{32\pi^{2}} \left(g_{L}^{\tau} g_{R}^{\mu} x_{t} H_{1}(x_{t}) + g_{L}^{\prime \tau} g_{R}^{\prime \mu} x_{t}^{\prime} H_{2}(x_{t}^{\prime}) \right)$$

$$\Gamma(\tau \to \mu\gamma) = \frac{e^2}{4\pi} m_{\tau} \left(\frac{m_{\tau}^2}{m_t^2}\right) \left(\left|C_L\right|^2 + \left|C_R\right|^2\right) \Longrightarrow \operatorname{Br}(\tau \to \mu\gamma) \approx 10^{-1}$$

 $Br(\tau \rightarrow \mu \gamma) < 4.4 \times 10^{-8}$ at 90% C.L. from BaBar experiment

• Reminding the $\tau \rightarrow \mu \gamma$ and BaBar experimental constraint

$$C_{R} = \frac{3_{c}}{32\pi^{2}} \left(g_{R}^{\tau} g_{L}^{\mu} x_{t} H_{1}(x_{t}) + g_{R}^{\prime \tau} g_{L}^{\prime \mu} x_{t}^{\prime} H_{2}(x_{t}^{\prime}) \right)$$
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We tune the cancellation

 $g_{R}^{\tau}g_{L}^{\mu}x_{t}H_{1}(x_{t}) + g_{R}^{\prime \tau}g_{L}^{\prime \mu}x_{t}^{\prime}H_{2}(x_{t}^{\prime}) \approx 0$ $g_{L}^{\tau}g_{R}^{\mu}x_{t}H_{1}(x_{t}) + g_{L}^{\prime \tau}g_{R}^{\prime \mu}x_{t}^{\prime}H_{2}(x_{t}^{\prime}) \approx 0$

• Only one chiral mode of the muon interactions is important. Say, $g_{I}^{\mu} \gg g_{R}^{\mu}$ and $g_{I}^{\prime \mu} \gg g_{R}^{\prime \mu}$.

• Reminding the $\tau \rightarrow \mu \gamma$ and BaBar experimental constraint

$$C_{R} = \frac{3_{c}}{32\pi^{2}} \left(\underline{g}_{R}^{\tau} \underline{g}_{L}^{\mu} x_{t} H_{1}(x_{t}) + \underline{g}_{R}^{\prime \tau} \underline{g}_{L}^{\prime \mu} x_{t}^{\prime} H_{2}(x_{t}^{\prime}) \right)$$
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• The ratio of the couplings

$$\frac{g_R^{\tau} g_L^{\mu}}{g_R^{\prime \tau} g_R^{\prime \mu} g_L^{\prime \tau}} = -\frac{x_t^{\prime} H_2(x_t^{\prime})}{x_t H_1(x_t)}$$

depend on the mass of two LQs $m_{\chi^{1/3}}$ and $m_{\Omega^{5/3}}$.



Large parameter space remains available for the required fine-tuning.

• Value of $Br(h \to \tau^{\mp} \mu^{\pm})$ v.s $g_R^{\tau} g_L^{\mu}$ for various LQ masses when the tuned cancellation is satisfied.



• Branching ratio = 1% occurs for the coupling product $g_R^{\tau} g_L^{\mu} \simeq 0.3 - 1$ and $m_{\chi} = m_{\Omega}$ from 600 GeV to 1 TeV.





Concluding Remarks

- We invoke two LQs, which couple to the 3rd generation quark and 2nd and 3rd generation leptons, for cancellation in $\tau \rightarrow \mu \gamma$ but sizable contribution to $h \rightarrow \tau^{\mp} \mu^{\pm}$. Kingman Cheung, Phys.Rev.D64.033001.
- The contribution of LQs, we consider here, to muon g-2 is very small. We assume $g_L^{\mu} \gg g_R^{\mu}$, $g_L^{\prime\mu} \gg g_R^{\prime\mu}$, s.t. it is suppressed by m_{μ} / M_{LQ} .
- ATLAS and CMS search for the 3rd generation LQ. For $\chi^{1/3}$, mass limit is 685 GeV at 95% CL, $\Omega^T = (\Omega^{5/3}, \Omega^{2/3})$ is 740 GeV at 95% CL.

CMS Collaboration, JHEP 1507, 042 (2015) ATLAS Collaboration, JHEP 1306, 033 (2013) CMS Collaboration, Phys.Lett.B 739, 229 (2014)





- To demonstrate the level of fine-tuned cancellation in ${\rm Br}(\tau \to \mu \gamma)$.
- We switch off either one of the cancelling amplitudes in $Br(\tau \rightarrow \mu \gamma)$ and show the individual contribution.

$$C_{R} = \frac{3_{c}}{32\pi^{2}} \left(g_{R}^{\tau} g_{L}^{\mu} x_{t} H_{1}(x_{t}) + g_{R}^{\prime \tau} g_{L}^{\prime \mu} x_{t}^{\prime} H_{2}(x_{t}^{\prime}) \right)$$
$$C_{L} = \frac{3_{c}}{32\pi^{2}} \left(g_{L}^{\tau} g_{R}^{\mu} x_{t} H_{1}(x_{t}) + g_{L}^{\prime \tau} g_{R}^{\prime \mu} x_{t}^{\prime} H_{2}(x_{t}^{\prime}) \right)$$

$$\Gamma(\tau \to \mu \gamma) = \frac{e^2}{4\pi} m_\tau \left(\frac{m_\tau^2}{m_t^2}\right) \left(\left|C_L\right|^2 + \left|C_R\right|^2\right)$$

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- To demonstrate the level of fine-tuned cancellation in ${\rm Br}(\tau \to \mu \gamma)$.
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• Go down from 10^{-2} to 10^{-8} in the branching ratio, the two amplitudes are required to cancel each other by almost one part in 1000.



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- So far we set the interactions of Higgs and LQs zero $\lambda_{\chi}=\lambda_{\Omega}=0~.$
- Value of $\operatorname{Br}(h \to \tau^{\mp} \mu^{\pm})$ with various $\lambda_{\chi} = \lambda_{\Omega} = \pm 1$, where the tune cancellation satisfied.



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