# Gauging The Popular Two Higgs Doublet Model

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# Based on

- Wei-Chih Huang, Y. L. Sming Tsai, TCY, arxiv:1512.00229, JHEP04(2016)019.
- Adelssalem Arhrib, Wei-Chih Huang, Y. L. Sming Tsai, TCY, work in progress.

# Motivation

- Dark matter (DM) & neutrino masses -----> BSM
- 2 Higgs doublet model (2HDM) are very popular. For example,
   In MSSM, 2 Higgs doublets are needed due to holomorphic nature of the superpotential as well as anomaly cancellation.
   With its additional CP phases, general 2HDM is a prototype model to discuss matter-antimatter asymmetry in the universe.
- Inert Higgs Doublet Model (IHDM) (Deshpande and Ma, '78) can provide dark matter candidate, with a discrete Z<sub>2</sub> symmetry imposed. No FCNC at tree level too!
- Scalar singlet as DM: Silveria & Zee ('85), McDonald ('94), Burgess *et al* ('01), He *et al* ('09). Also based on Z<sub>2</sub>.
- However Wilczek and Krauss ('89) had argued that global symmetry (discrete or continuous) can be violated by gravitation processes like black hole evaporation or wormhole tunneling. Suggested discrete gauge symmetry.
- We embed the two Higgs doublets into a fundamental representation of a new gauge group SU(2)<sub>H</sub>.

## Some Highlights of G2HDM

- New gauge group  $SU(2)_H \otimes U(1)_X$
- Symmetry breaking of SU(2)<sub>L</sub> is triggered or induced by SU(2)<sub>H</sub> breaking
- One of the Higgs doublet (H<sub>2</sub>) can be inert and may play the role of dark matter, whose stability is protected by gauge invariance
- Unlike Left-Right symmetric models, the complex vector fields W'<sup>(p,m)</sup> are electrically neutral

• etc

# Outline

#### • Motivation

- Model Setup
  - Particle Content
  - Higgs Potential & Symmetry Breaking
  - Yukawa Couplings
  - Anomaly Cancellation
  - Theoretical Constraints
- Phenomenology
  - Mass Spectra
  - Z-Z'-Z" Mixing
  - Higgs Physics
- Summary & Outlook

#### Particle Content

		1	$\square$		$\square$
Matter Fields	$SU(3)_C$	$SU(2)_L$	$SU(2)_H$	$U(1)_Y$	$U(1)_X$
$Q_L = (u_L \ d_L)^T$	3	2	1	1/6	0
$U_R = \begin{pmatrix} u_R & u_R^H \end{pmatrix}^T$	3	1	2	2/3	1
$D_R = \begin{pmatrix} d_R^H & d_R \end{pmatrix}^T$	3	1	2	-1/3	-1
$L_L = (\nu_L \ e_L)^T$	1	2	1	-1/2	0
$N_R = \left(\nu_R \ \nu_R^H\right)^T$	1	1	2	0	1
$E_R = \begin{pmatrix} e_R^H & e_R \end{pmatrix}^T$	1	1	2	-1	-1
$\chi_u$	3	1	1	2/3	0
$\chi_d$	3	1	1	-1/3	0
$\chi_{ u}$	1	1	1	0	0
$\chi_e$	1	1	1	-1	0
$H = (H_1 \ H_2)^T$	1	2	2	1/2	1
$\Delta_{H} = \begin{pmatrix} \Delta_{3}/2 & \Delta_{p}/\sqrt{2} \\ \Delta_{m}/\sqrt{2} & -\Delta_{3}/2 \end{pmatrix}$	1	1	3	0	0
$\Phi_H = (\Phi_1 \ \Phi_2)^T$	1	1	2	0	1

TABLE I. Matter field contents and their quantum number assignments.

- H<sub>1</sub> and H<sub>2</sub> are embedded into a SU(2)<sub>H</sub> doublet
- SU(2)<sub>L</sub> doublet fermions are singlets under SU(2)<sub>H</sub> while SU(2)<sub>L</sub> singlet fermions pair up with heavy fermions as SU(2)<sub>H</sub> doublets
- VEVs of  $\Phi_H$  and  $\Delta_H$  give a mass to SU(2)<sub>H</sub> gauge bosons
- ✤ VEV of Φ<sub>H</sub> gives a Dirac mass to heavy fermions

VEV of  $\Delta_{\rm H}$  give mass to charged Higgs

$$\begin{array}{l} \mbox{Higgs Potential} & H = \begin{pmatrix} H_1 \\ H_2 \end{pmatrix} \\ V = \mu_1^2 |H_1|^2 + \mu_2^2 |H_2|^2 + \lambda_1 |H_1|^4 + \lambda_2 |H_2|^4 + \lambda_3 |H_1|^2 |H_2|^2 + \lambda_4 |H_1^{\dagger} H_2|^2 \\ \mbox{technische universität} \\ + \frac{\lambda_3}{2} \{ (H_1^{\dagger} H_2^{\dagger})^2 + \text{h.c.} \} . \end{array} \tag{IHDM}$$

$$V(H) = \mu_H^2 H^{\dagger} H + \lambda_H (H^{\dagger} H)^2 ,$$
  
=  $\mu_H^2 (H_1^{\dagger} H_1 + H_2^{\dagger} H_2) + \lambda_H (H_1^{\dagger} H_1 + H_2^{\dagger} H_2)^2 ,$ 

Higgs Potential 
$$H = \begin{pmatrix} H_1 \\ H_2 \end{pmatrix}$$

$$V = \mu_1^2 |H_1|^2 + \mu_2^2 |H_2|^2 + \lambda_1 |H_1|^4 + \lambda_2 |H_2|^4 + \lambda_3 |H_1|^2 |H_2|^2 + \lambda_4 |H_1^{\dagger} H_2|^2 + \lambda_4 |H_1^{\dagger} H_2|^2 + \lambda_5 |H_1^{\dagger} H_2^{\dagger}|^2 + h.c. \}.$$
(IHDM)

$$V(H, \Delta_H, \Phi_H) = V(H) + V(\Phi_H) + V(\Delta_H) + V_{\min}(H, \Delta_H, \Phi_H)$$

$$V(H) = \mu_H^2 H^{\dagger} H + \lambda_H (H^{\dagger} H)^2 ,$$
  

$$= \mu_H^2 \left( H_1^{\dagger} H_1 + H_2^{\dagger} H_2 \right) + \lambda_H \left( H_1^{\dagger} H_1 + H_2^{\dagger} H_2 \right)^2 ,$$
  

$$V(\Phi_H) = \mu_\Phi^2 \Phi_H^{\dagger} \Phi_H + \lambda_\Phi \left( \Phi_H^{\dagger} \Phi_H \right)^2 ,$$
  

$$= \mu_\Phi^2 \left( \Phi_1^* \Phi_1 + \Phi_2^* \Phi_2 \right) + \lambda_\Phi \left( \Phi_1^* \Phi_1 + \Phi_2^* \Phi_2 \right)^2 ,$$
  

$$V(\Delta_H) = -\mu_\Delta^2 \operatorname{Tr} \left( \Delta_H^{\dagger} \Delta_H \right) + \lambda_\Delta \left( \operatorname{Tr} \left( \Delta_H^{\dagger} \Delta_H \right) \right)^2 ,$$
  

$$= -\mu_\Delta^2 \left( \frac{1}{2} \Delta_3^2 + \Delta_p \Delta_m \right) + \lambda_\Delta \left( \frac{1}{2} \Delta_3^2 + \Delta_p \Delta_m \right)^2 ,$$

$$\Delta_H = \begin{pmatrix} \Delta_3/2 & \Delta_p/\sqrt{2} \\ \Delta_m/\sqrt{2} & -\Delta_3/2 \end{pmatrix}$$

$$\Delta_m = (\Delta_p)^*$$
 and  $(\Delta_3)^* = \Delta_3$ 

#### Higgs Potential

$$\begin{split} V_{\text{mix}}\left(H,\Delta_{H},\Phi_{H}\right) &= + M_{H\Delta}\left(H^{\dagger}\Delta_{H}H\right) - M_{\Phi\Delta}\left(\Phi_{H}^{\dagger}\Delta_{H}\Phi_{H}\right) \\ &+ \lambda_{H\Delta}\left(H^{\dagger}H\right) \operatorname{Tr}\left(\Delta_{H}^{\dagger}\Delta_{H}\right) + \lambda_{H\Phi}\left(H^{\dagger}H\right)\left(\Phi_{H}^{\dagger}\Phi_{H}\right) \\ &+ \lambda_{\Phi\Delta}\left(\Phi_{H}^{\dagger}\Phi_{H}\right) \operatorname{Tr}\left(\Delta_{H}^{\dagger}\Delta_{H}\right) , \\ &= \left(+M_{H\Delta}\right)\left(\frac{1}{\sqrt{2}}H_{1}^{\dagger}H_{2}\Delta_{p} + \frac{1}{2}H_{1}^{\dagger}H_{1}\Delta_{3} + \frac{1}{\sqrt{2}}H_{2}^{\dagger}H_{1}\Delta_{m} - \frac{1}{2}H_{2}^{\dagger}H_{2}\Delta_{3}\right) \\ &- M_{\Phi\Delta}\left(\frac{1}{\sqrt{2}}\Phi_{1}^{*}\Phi_{2}\Delta_{p} + \frac{1}{2}\Phi_{1}^{*}\Phi_{1}\Delta_{3} + \frac{1}{\sqrt{2}}\Phi_{2}^{*}\Phi_{1}\Delta_{m} - \frac{1}{2}\Phi_{2}^{*}\Phi_{2}\Delta_{3}\right) \\ &+ \lambda_{H\Delta}\left(H_{1}^{\dagger}H_{1} + H_{2}^{\dagger}H_{2}\right)\left(\frac{1}{2}\Delta_{3}^{2} + \Delta_{p}\Delta_{m}\right) \\ &+ \lambda_{H\Phi}\left(H_{1}^{\dagger}H_{1} + H_{2}^{\dagger}H_{2}\right)\left(\Phi_{1}^{*}\Phi_{1} + \Phi_{2}^{*}\Phi_{2}\right) \\ &+ \lambda_{\Phi\Delta}\left(\Phi_{1}^{*}\Phi_{1} + \Phi_{2}^{*}\Phi_{2}\right)\left(\frac{1}{2}\Delta_{3}^{2} + \Delta_{p}\Delta_{m}\right) , \end{split}$$

Note that term like  $\Phi_H^T \epsilon \Delta_H \Phi_H$  is  $SU(2)_H$  invariant but forbidden by  $U(1)_X$ !

## Symmetry Breaking

$$H_{1} = \begin{pmatrix} \text{technische} \\ \text{dortmund} \\ \frac{v+h}{\sqrt{2}} + i\frac{G^{0}}{\sqrt{2}} \end{pmatrix} \qquad \Phi_{H} = \begin{pmatrix} G_{H}^{p} \\ \frac{v_{\Phi} + \phi_{2}}{\sqrt{2}} + i\frac{G_{H}^{0}}{\sqrt{2}} \end{pmatrix} \qquad \Delta_{H} = \begin{pmatrix} \frac{-v_{\Delta} + \delta_{3}}{2} & \frac{1}{\sqrt{2}}\Delta_{p} \\ \frac{1}{\sqrt{2}}\Delta_{m} & \frac{v_{\Delta} - \delta_{3}}{2} \end{pmatrix}$$

• If  $<\Delta_3 >= -v_{\Delta} \neq 0$ , the quadratic terms for H<sub>1</sub> and H<sub>2</sub> read:

$$\mu_H^2 \mp \frac{1}{2} M_{H\Delta} \cdot v_\Delta + \frac{1}{2} \lambda_{H\Delta} \cdot v_\Delta^2 + \frac{1}{2} \lambda_{H\Phi} \cdot v_\Phi^2$$

- If  $\langle \Delta_3 \rangle = -v_{\Delta} \neq 0$ , the quadratic terms for  $\Phi_1$  and  $\Phi_2$  read:  $\mu_{\Phi}^2 \pm \frac{1}{2} M_{\Phi\Delta} \cdot v_{\Delta} + \frac{1}{2} \lambda_{\Phi\Delta} \cdot v_{\Delta}^2 + \frac{1}{2} \lambda_{H\Phi} \cdot v^2$
- > Therefore, SU(2)<sub>H</sub> spontaneous symmetry breaking can trigger SU(2)<sub>L</sub> symmetry breaking even if  $\mu_H^2$  is positive

## Symmetry Breaking

$$V(v, v_{\Delta}, v_{\Phi}) = \frac{1}{4} \left[ \lambda_H v^4 + \lambda_{\Phi} v_{\Phi}^4 + \lambda_{\Delta} v_{\Delta}^4 + 2 \left( \mu_H^2 v^2 + \mu_{\Phi}^2 v_{\Phi}^2 - \mu_{\Delta}^2 v_{\Delta}^2 \right) - \left( M_{H\Delta} v^2 + M_{\Phi\Delta} v_{\Phi}^2 \right) v_{\Delta} + \lambda_{H\Phi} v^2 v_{\Phi}^2 + \lambda_{H\Delta} v^2 v_{\Delta}^2 + \lambda_{\Phi\Delta} v_{\Phi}^2 v_{\Delta}^2 \right]$$

#### Minimization:

$$v \cdot \left(2\lambda_H v^2 + 2\mu_H^2 - M_{H\Delta} v_\Delta + \lambda_{H\Phi} v_{\Phi}^2 + \lambda_{H\Delta} v_{\Delta}^2\right) = 0 ,$$
  

$$v_{\Phi} \cdot \left(2\lambda_{\Phi} v_{\Phi}^2 + 2\mu_{\Phi}^2 - M_{\Phi\Delta} v_\Delta + \lambda_{H\Phi} v^2 + \lambda_{\Phi\Delta} v_{\Delta}^2\right) = 0 ,$$
  

$$4\lambda_{\Delta} v_{\Delta}^3 - 4\mu_{\Delta}^2 v_\Delta - M_{H\Delta} v^2 - M_{\Phi\Delta} v_{\Phi}^2 + 2v_\Delta \left(\lambda_{H\Delta} v^2 + \lambda_{\Phi\Delta} v_{\Phi}^2\right) = 0 .$$

$$v^{2} = \frac{(2\lambda_{\Phi}\lambda_{H\Delta} - \lambda_{H\Phi}\lambda_{\Phi\Delta})v_{\Delta}^{2} + (\lambda_{H\Phi}M_{\Phi\Delta} - 2\lambda_{\Phi}M_{H\Delta})v_{\Delta} + 2(2\lambda_{\Phi}\mu_{H}^{2} - \lambda_{H\Phi}\mu_{\Phi}^{2})}{\lambda_{H\Phi}^{2} - 4\lambda_{H}\lambda_{\Phi}},$$

$$(A.1)$$

$$v_{\Phi}^{2} = \frac{(2\lambda_{H}\lambda_{\Phi\Delta} - \lambda_{H\Phi}\lambda_{H\Delta})v_{\Delta}^{2} + (\lambda_{H\Phi}M_{H\Delta} - 2\lambda_{H}M_{\Phi\Delta})v_{\Delta} + 2(2\lambda_{H}\mu_{\Phi}^{2} - \lambda_{H\Phi}\mu_{H}^{2})}{\lambda_{H\Phi}^{2} - 4\lambda_{H}\lambda_{\Phi}}.$$

$$(A.2)$$

11

Cubic Equation for  $v_{\Delta}$ 

$$v_{\Delta}^3 + a_2 v_{\Delta}^2 + a_1 v_{\Delta} + a_0 = 0$$

where  $a_2 = C_2/C_3$ ,  $a_1 = C_1/C_3$  and  $a_0 = C_0/C_3$  with

$$C_{0} = 2 \left(\lambda_{H\Phi} M_{\Phi\Delta} - 2\lambda_{\Phi} M_{H\Delta}\right) \mu_{H}^{2} + 2 \left(\lambda_{H\Phi} M_{H\Delta} - 2\lambda_{H} M_{\Phi\Delta}\right) \mu_{\Phi}^{2} ,$$

$$C_{1} = 2 \left[ 2 \left(2\lambda_{H\Delta}\lambda_{\Phi} - \lambda_{H\Phi}\lambda_{\Phi\Delta}\right) \mu_{H}^{2} + 2 \left(2\lambda_{H}\lambda_{\Phi\Delta} - \lambda_{H\Delta}\lambda_{H\Phi}\right) \mu_{\Phi}^{2} \right.$$

$$\left. + 2 \left(4\lambda_{H}\lambda_{\Phi} - \lambda_{H\Phi}^{2}\right) \mu_{\Delta}^{2} + \lambda_{H} M_{\Phi\Delta}^{2} - \lambda_{H\Phi} M_{H\Delta} M_{\Phi\Delta} + \lambda_{\Phi} M_{H\Delta}^{2} \right] ,$$

$$C_{2} = 3 \left[ \left(\lambda_{H\Delta}\lambda_{H\Phi} - 2\lambda_{H}\lambda_{\Phi\Delta}\right) M_{\Phi\Delta} + \left(\lambda_{H\Phi}\lambda_{\Phi\Delta} - 2\lambda_{H\Delta}\lambda_{\Phi}\right) M_{H\Delta} \right] ,$$

$$C_{3} = 4 \left[ \lambda_{H} \left(\lambda_{\Phi\Delta}^{2} - 4\lambda_{\Delta}\lambda_{\Phi}\right) - \lambda_{H\Delta}\lambda_{H\Phi}\lambda_{\Phi\Delta} + \lambda_{H\Delta}^{2}\lambda_{\Phi} + \lambda_{\Delta}\lambda_{H\Phi}^{2} \right] .$$

#### Solution:

$$\begin{aligned} v_{\Delta 1} &= -\frac{1}{3}a_2 + (S+T) , \\ v_{\Delta 2} &= -\frac{1}{3}a_2 - \frac{1}{2}(S+T) + \frac{1}{2}i\sqrt{3}(S-T) , \\ v_{\Delta 3} &= -\frac{1}{3}a_2 - \frac{1}{2}(S+T) - \frac{1}{2}i\sqrt{3}(S-T) , \end{aligned}$$

$$\begin{aligned} & Girolamo \ Cardano \ (1501-1576) \\ & S &\equiv \sqrt[3]{R+\sqrt{D}} , \\ & T &\equiv \sqrt[3]{R-\sqrt{D}} , \\ & D &\equiv Q^3 + R^2 , \end{aligned}$$

$$\begin{aligned} & Girolamo \ Cardano \ (1501-1576) \\ & R &\equiv \frac{9a_1a_2 - 27a_0 - 2a_2^3}{54} \end{aligned}$$

#### Yukawa Couplings

We choose to pair SM SU(2)<sub>L</sub> singlet fermions with heavy fermions to form SU(2)<sub>H</sub> doublets as

$$\begin{aligned} \mathcal{L}_{\text{Yuk}} \supset y_d \bar{Q}_L \left( D_R \cdot H \right) + y_u \bar{Q}_L \left( U_R \cdot \tilde{H} \right) + \text{H.c.}, \\ &= y_d \bar{Q}_L \left( d_R^H H_2 - \begin{pmatrix} d_R H_1 \\ \text{SM} \end{pmatrix} - y_u \bar{Q}_L \left( u_R \tilde{H}_1 \\ \text{SM} \end{pmatrix} + u_R^H \tilde{H}_2 \right) + \text{H.c.}, \end{aligned} \qquad \begin{aligned} U_R^T &= (u_R \ u_R^H)_{2/3} \\ D_R^T &= (d_R^H \ d_R)_{-1/3} \end{aligned}$$

• To give a mass to heavy fermions, we add "left-handed" partners with the help of the SU(2)<sub>H</sub> scalar doublet  $\Phi_{H}$ :

$$\mathcal{L}_{\text{Yuk}} \supset y'_d \overline{\chi}_d \left( D_R \cdot \Phi_H \right) + y'_u \overline{\chi}_u \left( U_R \cdot \tilde{\Phi}_H \right) + \text{H.c.}, \qquad \Phi_H = (\Phi_1 \Phi_2)^T$$
$$= y'_d \overline{\chi}_d \left( d_R^H \Phi_2 - d_R \Phi_1 \right) - y'_u \overline{\chi}_u \left( u_R \tilde{\Phi}_1 + u_R^H \tilde{\Phi}_2 \right) + \text{H.c.}, \qquad \chi_u, \chi_d$$

Absence of FCNC interaction!

(Natural flavor conservation: Weinberg & Glashow, '77; Paschos, '77 Minimal flavor violation: G. D'Ambrosio, G. F. Giudice, G. Isidori, A. Strumia '02)

If the second doublet  $H_2$  is inert, it could be DM candidate if it is lighter than all heavy fermions and scalars.

#### Yukawa Couplings

• Similarly, for the lepton sector we have:

$$\begin{aligned} \mathcal{L}_{\text{Yuk}} &\supset y_e \bar{L}_L \left( E_R \cdot H \right) + y_\nu \bar{L}_L \left( N_R \cdot \tilde{H} \right) + y'_e \overline{\chi}_e \left( E_R \cdot \Phi_H \right) + y'_\nu \overline{\chi}_\nu \left( N_R \cdot \tilde{\Phi}_H \right) + \text{H.c.}, \\ &= y_e \bar{L}_L \left( e_R^H H_2 - \underbrace{e_R H_1}_{\text{SM}} \right) - y_\nu \bar{L}_L \left( \nu_R \tilde{H}_1 + \nu_R^H \tilde{H}_2 \right) \\ &+ y'_e \overline{\chi}_e \left( e_R^H \Phi_2 - e_R \Phi_1 \right) - y'_\nu \overline{\chi}_\nu \left( \nu_R \tilde{\Phi}_1 + \nu_R^H \tilde{\Phi}_2 \right) + \text{H.c.}, \end{aligned}$$

where we introduce the right-handed neutrino and its SU(2)<sub>H</sub> partner,  $N_R = (\nu_R \ \nu_R^H)^T$ 

 The SM neutrinos have only Dirac masses unless the Majorana mass is introduced such as:

 $\overline{N_R^c}\Delta_N N_R \implies \text{where U(1)}_X \text{ is broken because } N_R \\ \text{carries U(1)}_X \text{ charge}$ 

 $H_1$  does not couple to heavy fermions. So the SM Higgs signal strengths are not affected by the new fermions.

#### technische universität dortmund maly Cancellation

- The anomaly cancellation for the SM gauge groups  $SU(3)_C \times SU(2)_L \times U(1)_Y$  is guaranteed since addition heavy particles of the same hypercharge form Dirac pairs. Therefore, contributions of the left-handed currents from  $\chi_u$ ,  $\chi_d$ ,  $\chi_\nu$  and  $\chi_e$  cancel those of right-handed ones from  $u_R^H$ ,  $d_R^H$ ,  $\nu_R^H$  and  $e_R^H$  respectively.
- For  $[SU(2)_H]^2 U(1)_Y$  from the doublets  $U_R$ ,  $D_R$ ,  $N_R$  and  $E_R$  with the following result, one has

$$2\operatorname{Tr}[T^{a}\{T^{b},Y\}] = 2\delta^{ab}\left(\sum_{l}Y_{l} - \sum_{r}Y_{r}\right) = -2\delta^{ab}\sum_{r}Y_{r}$$
$$= -2\delta^{ab}\left(3\cdot 2\cdot Y(U_{R}) + 3\cdot 2\cdot Y(D_{R}) + 2\cdot Y(N_{R}) + 2\cdot Y(E_{R})\right)$$



In terms of  $U(1)_X$ , one has to check  $[SU(3)_C]^2 U(1)_X$ ,  $[SU(2)_H]^2 U(1)_X$ ,  $[U(1)_X]^3$ ,  $[U(1)_Y]^2 U(1)_X$  and  $[U(1)_X]^2 U(1)_Y$ . The first three terms are zero due to cancellation between  $U_R$  and  $D_R$  and between  $E_R$  and  $N_R$  with opposite  $U(1)_X$  charges. For  $[U(1)_Y]^2 U(1)_X$ and  $[U(1)_X]^2 U(1)_Y$ , one has respectively

$$2 \cdot \left(3 \cdot \left(Y(U_R)^2 X(U_R) + Y(D_R)^2 X(D_R)\right) + Y(E_R)^2 X(E_R)\right) 2 \cdot \left(3 \cdot \left(X(U_R)^2 Y(U_R) + X(D_R)^2 Y(D_R)\right) + X(E_R)^2 Y(E_R)\right).$$

 $\blacktriangleright$  One can also check the perturbative gravitational anomaly associated with the hypercharge and  $U(1)_X$ -charge current couples to two gravitons is proportional to the following sum of the hypercharge

$$3 \cdot (2 \cdot Y(Q_L) + Y(\chi_u) + Y(\chi_d) - 2 \cdot Y(U_R) - 2 \cdot Y(D_R)) + 2 \cdot Y(L_L) + Y(\chi_\nu) + Y(\chi_e) - 2 \cdot Y(N_R) - 2 \cdot Y(E_R),$$

[Alvarez-Gaume and Witten, '84]

and  $U(1)_X$ -charge

$$X(U_R) + X(D_R) + X(E_R) + X(N_R).$$

Also, there are a total of  $12 \text{ SU}(2)_L$  doublets and a total of  $24 \text{ SU}(2)_H$  doublets. Free of Witten SU(2) global anomaly too!

[Witten, '82]

#### Particle Content

			$\frown$		$\frown$
Matter Fields	$SU(3)_C$	$SU(2)_L$	$SU(2)_H$	$U(1)_Y$	$U(1)_X$
$Q_L = (u_L \ d_L)^T$	3	2	1	1/6	0
$U_R = \begin{pmatrix} u_R & u_R^H \end{pmatrix}^T$	3	1	2	2/3	1
$D_R = \begin{pmatrix} d_R^H & d_R \end{pmatrix}^T$	3	1	2	-1/3	-1
$L_L = (\nu_L \ e_L)^T$	1	2	1	-1/2	0
$N_R = \left(\nu_R \left(\nu_R^H\right)^T\right)$	1	1	2	0	1
$E_R = \begin{pmatrix} e_R^H & e_R \end{pmatrix}^T$	1	1	2	-1	-1
$\chi_u$	3	1	1	2/3	0
$\chi_d$	3	1	1	-1/3	0
$\chi_{\nu}$	1	1	1	0	0
$\chi_e$	1	1	1	-1	0
$H = (H_1 H_2)^T$	1	2	2	1/2	1
$\Delta_{H} = \begin{pmatrix} \Delta_{3}/2 & \Delta_{p}/\sqrt{2} \\ \Delta_{m}/\sqrt{2} & -\Delta_{3}/2 \end{pmatrix}$	1	1	3	0	0
$\Phi_H = (\Phi_1 \ \Phi_2)^T$	1	1	2	0	1

- H<sub>1</sub> and H<sub>2</sub> are embedded into a SU(2)<sub>H</sub> doublet
- SU(2)<sub>L</sub> doublet fermions are singlets under SU(2)<sub>H</sub> while SU(2)<sub>L</sub> singlet fermions pair up with heavy fermions as SU(2)<sub>H</sub> doublets
- VEVs of  $\Phi_H$  and  $\Delta_H$  give a mass to SU(2)<sub>H</sub> gauge bosons
- VEV of Φ<sub>H</sub> gives a Dirac mass to heavy fermions

VEV of  $\Delta_{\rm H}$  give mass to charged Higgs

TABLE I. Matter field contents and their quantum number assignments. Optional  $\Delta_N(1, 1, 3, 0, -2)$  to provide Majorana neutrino masses.

# Theoretical Constraints

- Vacuum Stability
   Scalar potential should be bounded from below
- Perturbative Unitarity
   Scattering amplitudes in the scalar sector

# Potential (Quartic terms)

• Due to gauge symmetry, the potential depends only on the following combinations

$$\mathcal{X}^{2} = h^{2} + (G^{0})^{2} + 2G^{+}G^{-} + S^{2} + P^{2} + 2H^{+}H^{-}$$
$$\mathcal{Y}^{2} = \phi_{2}^{2} + (G_{H}^{0})^{2} + 2G_{H}^{p}G_{H}^{m}$$
$$\mathcal{Z}^{2} = \delta_{3}^{2} + 2\Delta_{p}\Delta_{m}$$

$$V_4 = \frac{1}{4} \left( \lambda_H \mathcal{X}^4 + \lambda_\Phi \mathcal{Y}^4 + \lambda_\Delta \mathcal{Z}^4 + \lambda_{H\Delta} \mathcal{X}^2 \mathcal{Z}^2 + \lambda_{H\Phi} \mathcal{X}^2 \mathcal{Y}^2 + \lambda_{\Phi\Delta} \mathcal{Y}^2 \mathcal{Z}^2 \right)$$

### Scalar Bosons Scattering Amplitudes

$$\mathcal{M}_{1} = \begin{pmatrix} 6\lambda_{H} & \lambda_{H} & \lambda_{H} & \lambda_{H} & \lambda_{H} & \lambda_{H} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Delta} & \lambda_{H\Delta} \\ \lambda_{H} & 6\lambda_{H} & \lambda_{H} & \lambda_{H} & \lambda_{H} & \lambda_{H} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Delta} & \lambda_{H\Delta} \\ \lambda_{H} & \lambda_{H} & 6\lambda_{H} & \lambda_{H} & \lambda_{H} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Delta} & \lambda_{H\Delta} \\ \lambda_{H} & \lambda_{H} & \lambda_{H} & 6\lambda_{H} & \lambda_{H} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Delta} & \lambda_{H\Delta} \\ \lambda_{H} & \lambda_{H} & \lambda_{H} & \lambda_{H} & 6\lambda_{H} & \lambda_{H} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Delta} & \lambda_{H\Delta} \\ \lambda_{H} & \lambda_{H} & \lambda_{H} & \lambda_{H} & \delta_{H} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Delta} & \lambda_{H\Delta} \\ \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \delta_{A\Phi} & \lambda_{\Phi} & \lambda_{\Phi\Delta} & \lambda_{\Phi\Delta} \\ \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{H\Phi} & \lambda_{\Phi} & \Delta_{\Phi} & \delta_{A\Phi} & \lambda_{\Phi\Delta} & \lambda_{\Phi\Delta} \\ \lambda_{H\Delta} & \lambda_{H\Delta} & \lambda_{H\Delta} & \lambda_{H\Delta} & \lambda_{H\Delta} & \lambda_{H\Delta} & \lambda_{\Phi\Delta} & \lambda_{\Phi\Delta} & \lambda_{\Phi\Delta} & \lambda_{\Delta} & \delta_{A\Delta} \\ \lambda_{H\Delta} & \lambda_{H\Delta} & \lambda_{H\Delta} & \lambda_{H\Delta} & \lambda_{H\Delta} & \lambda_{H\Delta} & \lambda_{\Phi\Delta} & \lambda_{\Phi\Delta} & \lambda_{\Phi\Delta} & \lambda_{\Delta} & \delta_{A} \end{pmatrix}$$

The first row corresponds to the processes

$$hh \longleftrightarrow hh, G^0G^0, G^+G^-, SS, PP, H^+H^-, \phi_2\phi_2, G^0_HG^0_H, G^p_HG^m_H, \delta_3\delta_3, \Delta_p\Delta_m$$
.

The second row is for

$$G^{0}G^{0} \longleftrightarrow hh, G^{0}G^{0}, G^{+}G^{-}, SS, PP, H^{+}H^{-}, \phi_{2}\phi_{2}, G^{0}_{H}G^{0}_{H}, G^{p}_{H}G^{m}_{H}, \delta_{3}\delta_{3}, \Delta_{p}\Delta_{m}$$

And so on. Here we decompose  $H_2^{0*} = (S - iP)/\sqrt{2}$  and consider S and P separately. This was usually done in IHDM. Unitarity constraints require all eigenvalues of  $\mathcal{M}_1$  to satisfy

$$|\lambda_i| \leq 8\pi$$
,  $\forall i = 1, \cdots, 11$ 

$$\mathcal{M}_2 = \begin{pmatrix} \lambda_{H\Phi} \mathcal{I}_{18 \times 18} & 0 & 0 \\ 0 & \lambda_{\Phi\Delta} \mathcal{I}_{6 \times 6} & 0 \\ 0 & 0 & \lambda_{H\Delta} \mathcal{I}_{12 \times 12} \end{pmatrix}$$

where  $\mathcal{I}_{n \times n}$  is the  $n \times n$  unit matrix. The first block corresponds to

$$h\phi_2 \longleftrightarrow h\phi_2, hG_H^0 \longleftrightarrow hG_H^0, hG_H^p \longleftrightarrow hG_H^p,$$
$$G^0\phi_2 \longleftrightarrow G^0\phi_2, G^0G_H^0 \longleftrightarrow G^0G_H^0, G^0G_H^p \longleftrightarrow G^0G_H^p,$$
$$\cdots \text{ and so on.}$$

The second block corresponds to

$$\phi_2 \delta_3 \longleftrightarrow \phi_2 \delta_3, \phi_2 \Delta_p \longleftrightarrow \phi_2 \Delta_p,$$
$$G_H^0 \delta_3 \longleftrightarrow G_H^0 \delta_3, G_H^0 \Delta_p \longleftrightarrow G_H^0 \Delta_p,$$
$$G_H^p \delta_3 \longleftrightarrow G_H^p \delta_3, G_H^p \Delta_p \longleftrightarrow G_H^p \Delta_p.$$

The third block corresponds to

$$h\delta_3 \longleftrightarrow h\delta_3, h\Delta_p \longleftrightarrow h\Delta_p,$$

$$G^0\delta_3 \longleftrightarrow G^0\delta_3, G^0\Delta_p \longleftrightarrow G^0\Delta_p,$$

$$G^+\delta_3 \longleftrightarrow G^+\delta_3, G^+\Delta_p \longleftrightarrow G^+\Delta_p,$$

$$\cdots \text{ and so on.}$$

Eigenvalues of  $\mathcal{M}_2$  are  $\lambda_{H\Phi}$ ,  $\lambda_{\Phi\Delta}$  and  $\lambda_{H\Delta}$ . Unitarity requires

$$\begin{aligned} |\lambda_{H\Phi}| &\leq 8\pi \; , \\ |\lambda_{\Phi\Delta}| &\leq 8\pi \; , \\ |\lambda_{H\Delta}| &\leq 8\pi \; . \end{aligned}$$

•  $\lambda_H$ ,  $\lambda_{\Phi}$ ,  $\lambda_{\Delta}$  must be positive definite:

$$\lambda_H, \ \lambda_\Phi, \ \lambda_\Delta > 0 \ . \tag{73}$$

•  $\lambda_{H\Phi}$ ,  $\lambda_{\Phi\Delta}$ ,  $\lambda_{H\Delta}$  can be positive or negative. Their ranges are determined by unitarity constraint

$$|\lambda_{H\Phi}|, |\lambda_{\Phi\Delta}|, |\lambda_{H\Delta}| < 8\pi.$$
(74)

(1) 
$$\lambda_{H\Phi}$$
,  $\lambda_{\Phi\Delta}$ ,  $\lambda_{H\Delta} > 0$   
 $\lambda_{H\Phi}$ ,  $\lambda_{\Phi\Delta}$ ,  $\lambda_{H\Lambda} < 8\pi$ . (75)

(2) 
$$\lambda_{H\Phi}, \ \lambda_{\Phi\Delta} > 0; \ \lambda_{H\Delta} < 0$$

$$4\lambda_H \lambda_\Delta - \lambda_{H\Delta}^2 > 0 \tag{76}$$

Similar conditions for two other permutation cases.

(3)  $\lambda_{H\Phi} > 0$ ;  $\lambda_{\Phi\Delta}$ ,  $\lambda_{H\Delta} < 0$ 

$$4\lambda_{\Phi}\lambda_{\Delta} - \lambda_{\Phi\Delta}^{2} > 0$$

$$4\lambda_{H}\lambda_{\Delta} - \lambda_{H\Delta}^{2} > 0$$

$$2\lambda_{\Delta}\lambda_{H\Phi} - \lambda_{H\Delta}\lambda_{\Phi\Delta} > -\sqrt{(4\lambda_{H}\lambda_{\Delta} - \lambda_{H\Delta}^{2})(4\lambda_{\Phi}\lambda_{\Delta} - \lambda_{\Phi\Delta}^{2})}$$
(77)

Similar conditions for two other permutation cases.

(4)  $\lambda_{H\Phi}$ ,  $\lambda_{\Phi\Delta}$ ,  $\lambda_{H\Delta} < 0$ 

$$4\lambda_{H}\lambda_{\Phi} - \lambda_{H\Phi}^{2} > 0$$

$$4\lambda_{\Phi}\lambda_{\Delta} - \lambda_{\Phi\Delta}^{2} > 0$$

$$4\lambda_{H}\lambda_{\Delta} - \lambda_{H\Delta}^{2} > 0$$

$$2\lambda_{\Phi}\lambda_{H\Delta} - \lambda_{H\Phi}\lambda_{\Phi\Delta} > -\sqrt{(4\lambda_{H}\lambda_{\Phi} - \lambda_{H\Phi}^{2})(4\lambda_{\Phi}\lambda_{\Delta} - \lambda_{\Phi\Delta}^{2})}$$

$$2\lambda_{H}\lambda_{\Phi\Delta} - \lambda_{H\Phi}\lambda_{H\Delta} > -\sqrt{(4\lambda_{H}\lambda_{\Phi} - \lambda_{H\Phi}^{2})(4\lambda_{H}\lambda_{\Delta} - \lambda_{H\Delta}^{2})}$$

$$2\lambda_{\Delta}\lambda_{H\Phi} - \lambda_{\Phi\Delta}\lambda_{H\Delta} > -\sqrt{(4\lambda_{\Phi}\lambda_{\Delta} - \lambda_{\Phi\Delta}^{2})(4\lambda_{H}\lambda_{\Delta} - \lambda_{H\Delta}^{2})}$$
(78)

• All eigenvalues  $\lambda_i$  of  $\mathcal{M}_1$  in (66) must be constrained by  $|\lambda_i| < 8\pi$ .



#### Scalar mass spectrum

• First, we Taylor expand scalar fields around the vacua

$$H_1 = \begin{pmatrix} G^+ \\ \frac{v+h}{\sqrt{2}} + iG^0 \end{pmatrix} \quad , \quad \Phi_H = \begin{pmatrix} G_H^p \\ \frac{v_{\Phi} + \phi_2}{\sqrt{2}} + iG_H^0 \end{pmatrix} \quad , \quad \Delta_H = \begin{pmatrix} \frac{-v_{\Delta} + \delta_3}{2} & \frac{1}{\sqrt{2}}\Delta_p \\ \frac{1}{\sqrt{2}}\Delta_m & \frac{v_{\Delta} - \delta_3}{2} \end{pmatrix}$$

 $H_2 = (H_2^+ H_2^0)^T \qquad \qquad \Psi_G \equiv \{G^+, G^0, G_H^p, G_H^0\} \text{ are Goldstone bosons}$  $\Psi \equiv \{h, H_2, \Phi_1, \phi_2, \delta_3, \Delta_p\} \text{ are the physical fields}$ 

Mass Matrix is 10 x 10

- We have 6 Goldstone bosons, absorbed by 3 SM gauge bosons and 3 SU(2)<sub>H</sub> ones, yielding the massless photon and dark photon
  More later!
- We have the mixing between  $\{h, \delta_3, \phi_2\}$  and  $\{G_H^p, \Delta_p, H_2^{0*}\}$  due to:

$$V_{\text{mix}}(h, \delta_{3}, \phi_{2}) \supset + M_{H\Delta}\left(\frac{1}{2}H_{1}^{\dagger}H_{1}\Delta_{3}\right) + \lambda_{H\Delta}\left(H_{1}^{\dagger}H_{1}\right)\left(\frac{1}{2}\Delta_{3}^{2}\right) \qquad V_{\text{mix}}\left(G_{H}^{p}, \Delta_{p}, H_{2}^{0*}\right) \supset + M_{H\Delta}\left(\frac{1}{\sqrt{2}}H_{1}^{\dagger}H_{2}\Delta_{p} + \frac{1}{\sqrt{2}}H_{2}^{\dagger}H_{1}\Delta_{m}\right) \\ + \lambda_{H\Phi}\left(H_{1}^{\dagger}H_{1}\right)\left(\Phi_{2}^{*}\Phi_{2}\right) + \lambda_{\Phi\Delta}\left(\Phi_{2}^{*}\Phi_{2}\right)\left(\frac{1}{2}\Delta_{3}^{2}\right) \qquad - M_{\Phi\Delta}\left(\frac{1}{\sqrt{2}}\Phi_{1}^{*}\Phi_{2}\Delta_{p} + \frac{1}{\sqrt{2}}\Phi_{2}^{*}\Phi_{1}\Delta_{m}\right) \\ - M_{\Phi\Delta}\left(\frac{1}{2}\Phi_{2}^{*}\Phi_{2}\Delta_{3}\right)$$

#### Scalar Mass Spectrum

$$\mathcal{M}_{0}^{2} = \begin{pmatrix} 2\lambda_{H}v^{2} & \frac{v}{2}\left(M_{H\Delta} - 2\lambda_{H\Delta}v_{\Delta}\right) & \lambda_{H\Phi}vv_{\Phi} \\ \frac{v}{2}\left(M_{H\Delta} - 2\lambda_{H\Delta}v_{\Delta}\right) & \frac{1}{4v_{\Delta}}\left(8\lambda_{\Delta}v_{\Delta}^{3} + M_{H\Delta}v^{2} + M_{\Phi\Delta}v_{\Phi}^{2}\right) & \frac{v_{\Phi}}{2}\left(M_{\Phi\Delta} - 2\lambda_{\Phi\Delta}v_{\Delta}\right) \\ \lambda_{H\Phi}vv_{\Phi} & \frac{v_{\Phi}}{2}\left(M_{\Phi\Delta} - 2\lambda_{\Phi\Delta}v_{\Delta}\right) & 2\lambda_{\Phi}v_{\Phi}^{2} \end{pmatrix}$$

 $S = \{h, \delta_3, \phi_2\}$ 

- The 125 GeV Higgs is now a mixture of  $\{h, \delta_3, \phi_2\}$
- However, the mixing is constrained to be quite small, suppressed by  $v/v_{\Phi}$  as  $v \sim 246$  GeV and  $v_{\Phi} \ge 10$  TeV due to LEP Z-Z' mixing constraint (More on this later)!



#### Scalar mass spectrum

- The determinant of the second mass matrix is zero since one of the mass eigenstates and its complex conjugate correspond to the Goldstone bosons, eaten by SU(2)<sub>H</sub> W'
- > For  $H_2^0$  to be the DM candidate, one has to make sure it is lighter than its charged component  $H_2^{\pm}$  of mass  $M_{H\Delta}v_{\Delta}$

$$\mathcal{M}_{0}^{\prime 2} = \begin{pmatrix} M_{\Phi\Delta} v_{\Delta} & -\frac{1}{2} M_{\Phi\Delta} v_{\Phi} & 0\\ -\frac{1}{2} M_{\Phi\Delta} v_{\Phi} & \frac{1}{4v_{\Delta}} \left( M_{H\Delta} v^{2} + M_{\Phi\Delta} v_{\Phi}^{2} \right) & \frac{1}{2} M_{H\Delta} v\\ 0 & \frac{1}{2} M_{H\Delta} v & M_{H\Delta} v_{\Delta} \end{pmatrix}$$

 $\{G_H^p, \Delta_p, H_2^{0*}\}$ 



#### Scalar mass spectrum

The charged components of H<sub>2</sub> do not mix with other neutral scalars:

$$m_{H_2^{\pm}}^2 = M_{H\Delta} v_{\Delta}$$

Different from IHDM!!

The rest is the Goldstone bosons:

$$m_{G^{\pm}}^2 = m_{G^0}^2 = m_{G^0_H}^2 = 0$$

#### Reproducing the SM 125 GeV Higgs



- We have 6 Goldstone bosons: 2 absorbed by SM W, 2 eaten by SU(2)<sub>H</sub> W' and the rest two by Z and Z'.
- > The SM W bosons acquire a mass by eating the charged components of H<sub>1</sub> as in the SM since H<sub>2</sub> does not get a VEV and the other scalars ( $\Phi_H$  and  $\Delta_H$ ) are neutral

$$M_{W^{\pm}} = \frac{1}{2}gv$$

 $\begin{array}{l} & \succ \mathrm{SU(2)_H} \text{ W' bosons receive a mass from all VEVs, } <\Delta_3 > \text{, } <\Phi_2 > \\ & \text{and } <\mathrm{H_1 > :} \\ & m_{W'^{(p,m)}}^2 = \frac{1}{4}g_H^2 \left(v^2 + v_\Phi^2 + 4v_\Delta^2\right) \end{array} \end{array}$ 



> < $\Delta_3$ > gives a mass to SU(2)<sub>H</sub> W' bosons but not W'<sup>3</sup> while one linear combination of W'<sup>3</sup> and X obtains a mass from < $\Phi_2$ >

> < H<sub>1</sub>> also gives a mass to W'<sup>3</sup> and X because of its quantum numbers. Hence, W'<sup>3</sup> and X mix with the SM W<sub>3</sub> and Y.

$$\mathcal{M}_{1}^{2} = \begin{pmatrix} \frac{g'^{2}v^{2}}{4} & -\frac{g'gv^{2}}{4} & \frac{g'g_{H}v^{2}}{4} & \frac{g'g_{X}v^{2}}{2} \\ -\frac{g'gv^{2}}{4} & \frac{g^{2}v^{2}}{4} & -\frac{gg_{H}v^{2}}{4} & -\frac{gg_{H}v^{2}}{4} & -\frac{gg_{X}v^{2}}{2} \\ \frac{g'g_{H}v^{2}}{4} & -\frac{gg_{H}v^{2}}{4} & \frac{g_{H}^{2}\left(v^{2}+v_{\Phi}^{2}\right)}{4} & \frac{g_{H}g_{X}\left(v^{2}-v_{\Phi}^{2}\right)}{2} \\ \frac{g'g_{X}v^{2}}{2} & -\frac{gg_{X}v^{2}}{2} & \frac{g_{H}g_{X}\left(v^{2}-v_{\Phi}^{2}\right)}{2} & g_{X}^{2}\left(v^{2}+v_{\Phi}^{2}\right) \end{pmatrix}$$

No  $v_{\Delta}$  dependent!



- > The mass matrix contains 2 massive particles, identified as SM Z and additional Z' and also two massless photon  $\gamma$  and dark photon  $\gamma'$
- $\succ \gamma$ ' also couples to SM fermions and are thermally produced in the early universe. It would be excluded, for instance, by CMB observables
- There exist at least two solutions: Stueckelberg mass terms (Kors and Nath '04 '05) or simply setting g<sub>x</sub> zero.

 $\succ$  In the following, we present results for the second solution.



The 3-by-3 mass matrix can be diagonalized by only 2 mixing angles:

$$\begin{pmatrix} m_{\gamma}^{2} & 0 & 0 \\ 0 & m_{Z}^{2} & 0 \\ 0 & 0 & m_{Z'}^{2} \end{pmatrix} = R_{23} \left(\theta_{ZZ'}\right)^{T} R_{12} \left(\theta_{w}\right)^{T} \begin{pmatrix} \frac{g'^{2}v^{2}}{4} & -\frac{g'gv^{2}}{4} & \frac{g'g_{H}v^{2}}{4} \\ -\frac{g'gv^{2}}{4} & \frac{g^{2}v^{2}}{4} & -\frac{gg_{H}v^{2}}{4} \\ \frac{g'g_{H}v^{2}}{4} & -\frac{gg_{H}v^{2}}{4} & \frac{g^{2}_{H}\left(v^{2}+v_{\Phi}^{2}\right)}{4} \end{pmatrix} R_{12} \left(\theta_{w}\right) R_{23} \left(\theta_{ZZ'}\right)$$

$$m_Z \simeq \sqrt{g^2 + {g'}^2} \frac{v}{2} \qquad \qquad \sin \theta_w = \frac{g'}{\sqrt{g^2 + {g'}^2}} \ , \ \mathbf{Q} = \mathbf{Y} + \mathbf{I}_3 \text{ is a good quantum number}$$
$$m_{Z'} \simeq g_H \frac{v_\Phi}{2} \qquad \qquad \sin \theta_{ZZ'} \approx \frac{\sqrt{g^2 + {g'}^2} v^2}{g_H v_\Phi^2} \ (\text{in the limit of } v_\Phi \gg v) \ ,$$



#### Experimental constraints on Z'



- The red line comes from direct Z' resonance searches (1412.6302)
- The black dashed line comes from LEP constraints on the cross-section of  $e^+e^- \rightarrow e^+e^-$  (hep-ex/0312023)  $\Rightarrow v_{\Phi} > 10 \text{ TeV}$
- The blue dotted line comes from EWPT data and collider constraints on the Z-Z' mixing(0906.2435, 1406.6776)

$$m_{Z'} \simeq g_H \frac{v_\Phi}{2}$$



## $h \to H_2^{\pm} \operatorname{loop} \to \gamma \gamma \text{ or } Z\gamma$



Predictions of  $h \to \gamma \gamma$  and  $h \to Z \gamma$ in this model. Due to the fact  $\lambda_H (\approx m_h^2/2v^2)$ is positive,  $R_{\gamma\gamma}$  is always less than the SM prediction while  $R_{Z\gamma}$  ranges from 0.9 to 1, given the ATLAS and CMS measurements on  $R_{\gamma\gamma}$ : CMS: 1.13 ± 0.24 and ATLAS: 1.17 ± 0.27 (1408.7084 and CMS-PAS-HIG-14-009 (2014)).

$$V(H) = \mu_H^2 H^{\dagger} H + \lambda_H \left( H^{\dagger} H \right)^2 ,$$
  
=  $\mu_H^2 \left( H_1^{\dagger} H_1 + H_2^{\dagger} H_2 \right) + \lambda_H \left( H_1^{\dagger} H_1 + H_2^{\dagger} H_2 \right)^2 ,$ 

#### IHDM

$$H_1 = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v+h+iG^0) \end{pmatrix}, \qquad H_2 = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}}(S+iA) \end{pmatrix}$$

 $V = \mu_1^2 |H_1|^2 + \mu_2^2 |H_2|^2 + \lambda_1 |H_1|^4 + \lambda_2 |H_2|^4 + \lambda_3 |H_1|^2 |H_2|^2 + \lambda_4 |H_1^{\dagger} H_2|^2 + \frac{\lambda_5}{2} \{ (H_1^{\dagger} H_2)^2 + \text{h.c.} \}.$  1.2

$$\begin{split} m_h^2 &= -2\mu_1^2 = 2\lambda_1 v^2 \\ m_S^2 &= \mu_2^2 + \frac{1}{2}(\lambda_3 + \lambda_4 + \lambda_5)v^2 = \mu_2^2 + \lambda_L v^2 \\ m_A^2 &= \mu_2^2 + \frac{1}{2}(\lambda_3 + \lambda_4 - \lambda_5)v^2 = \mu_2^2 + \lambda_A v^2 \\ m_{H^{\pm}}^2 &= \mu_2^2 + \frac{1}{2}\lambda_3 v^2 \end{split}$$

$$\lambda_{L,A} = \frac{1}{2}(\lambda_3 + \lambda_4 \pm \lambda_5)$$

Arhrib, Tsai, Yuan, TCY, JCAP 06, (2014), 030





![](_page_35_Figure_0.jpeg)

![](_page_36_Figure_0.jpeg)

![](_page_37_Figure_0.jpeg)

Signal Strengths  $R_{\gamma\gamma}$  and  $R_{\gamma Z}$  versus Charged Higgs Mass

![](_page_38_Figure_1.jpeg)

#### Conclusions and Outlook

- We have constructed a model with the 2 Higgs doublets embedded into a 2 dim spinor representation of a new gauge group SU(2)<sub>H</sub>.
- Spontaneous symmetry breaking of  $SU(2)_H$  by a triplet triggers the breaking of the SM  $SU(2)_L$ .
- An inert doublet can be emerged as DM candidate due to local gauge invariance rather than the ad hoc Z<sub>2</sub> discrete symmetry.
- $W^{\{p,m\}}$  gauge bosons are complex fields but electrically neutral.
- Z-Z' mixing is constrained to be small by LEP data, direct Z' search at LHC, etc implies the VEV v<sub>Φ</sub> ≥ 10 TeV and a heavy Z'. This also implies the mixings between SM Higgs and other heavy scalars are small.
- Signal strengths for  $h\gamma\gamma$  and  $hZ\gamma$  are consistent with LHC data provided that the charged Higgs is heavier than 100 GeV. They are always <1, in contrast with IHDM which can > or < 1!

#### Conclusions and Outlook

- EWPT (S, T, U) new contributions from extra scalars and gauge bosons. (Note: They vanish in the exact SU(2)<sub>H</sub> limit!)
- LHC phenomenology of heavy fermions, gauge particles  $Z', Z'', W^{\{p,m\}}$  and scalars
- Rare Decays (Loop processes)
  FCNH decay e.g. h→μτ, etc
  μ→eγ (MEG), μ-e conversion (Mu2E, COMET), etc
- DM (relic density, direct/indirect detection, collider)

# Thank you for your attention!