$R(D^{(*)})$ and $B_c \to \tau \nu$ in a generic 2HDM

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Introduction

□ A challenge to lepton universality is reported in B decays, such as the excesses in the measured ratios $R(D^{(*)}) = \frac{B(B \to D^{(*)}\tau\nu)}{B(B \to D^{(*)}\ell\nu)}$

Exp	$R(D^*)$	R(D)	remarks
BaBar	$0.332 \pm 0.024 \pm 0.018$	$0.440 \pm 0.058 \pm 0.042$	PRL109(12);PRD88(13)
Belle	$0.293 \pm 0.038 \pm 0.015$	$0.375 \pm 0.064 \pm 0.026$	PRD92(15)
Belle	$0.302 \pm 0.030 \pm 0.011$	—	PRD94(16)
LHCb	$0.336 \pm 0.027 \pm 0.030$	—	PRL115(15)
Belle	$0.270 \pm 0.035^{+0.028}_{-0.025}$	—	PRL118(17)
LHCb	$0.285 \pm 0.019 \pm 0.029$	_	FPCP2017
Avg	$0.304 \pm 0.013 \pm 0.007$	$0.407 \pm 0.039 \pm 0.024$	
SM	0.252 ± 0.003	$0.299 \pm 0.011/0.300 \pm 0.008$	PRD85(12); PRD92(15)
	3.4σ	2.3σ	

TABLE II: Average from the heavy flavor averaging group (HFLAV).

↔ Considering the R(D)-R(D*) correlation, 4.1 σ deviation from the SM

□ If the excesses hint at new physics, what effects causes the excesses? We investigate the charged Higgs (*H*[±]) effect in a two-Higgs-doublet model (2HDM)

		Type I	Type II	Lepton-specific	Flipped
v_2	ξ_h^u	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$
$tan\beta = \frac{1}{2}$	ξ^d_h	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$
v_1	ξ_h^ℓ	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$	$-\sin \alpha / \cos \beta$	$\cos \alpha / \sin \beta$
α : h – H	ξ^u_H	$\sin \alpha / \sin \beta$	$\sin \alpha / \sin \beta$	$\sin \alpha / \sin \beta$	$\sin \alpha / \sin \beta$
mixing angle	ξ^d_H	$\sin \alpha / \sin \beta$	$\cos lpha / \cos eta$	$\sin \alpha / \sin \beta$	$\cos lpha / \cos eta$
	ξ^ℓ_H	$\sin \alpha / \sin \beta$	$\cos lpha / \cos eta$	$\cos lpha / \cos eta$	$\sin \alpha / \sin \beta$
	ξ^u_A	\coteta	\coteta	\coteta	\coteta
	ξ^d_A	$-\cot eta$	aneta	$-\coteta$	aneta
	ξ^ℓ_A	$-\cot \beta$	aneta	aneta	$-\cot\beta$

 $> H^{\pm}$ couplings to the quarks and leptons depend on the taken schemes

Branco etal Phys.Rept. 516 (12)

➤ What we focus on is the generic 2HDM, where we do not impose extra symmetry to suppress the FCNCs at tree level

\blacktriangleright <u>*H*[±] Yukawa couplings to the quarks and leptons</u>:

$$-\mathcal{L}_{Y} = \bar{Q}_{L}Y_{1}^{d}D_{R}H_{1} + \bar{Q}_{L}Y_{2}^{d}D_{R}H_{2} + \bar{Q}_{L}Y_{1}^{u}U_{R}\tilde{H}_{1} + \bar{Q}_{L}Y_{2}^{u}U_{R}\tilde{H}_{2} + \bar{L}Y_{1}^{\ell}\ell_{R}H_{1} + \bar{L}Y_{2}^{\ell}\ell_{R}H_{2} + H.c., \qquad H_{i} = \begin{pmatrix} \phi_{i}^{+} \\ (v_{i} + \phi_{i} + i\eta_{i})/\sqrt{2} \end{pmatrix}$$

h couplings:

$$\begin{aligned} -\mathcal{L}_{Y}^{h} &= \bar{u}_{L} \left[\frac{c_{\alpha}}{v s_{\beta}} \mathbf{m}_{\mathbf{u}} - \frac{c_{\beta \alpha}}{s_{\beta}} \mathbf{X}^{u} \right] u_{R} h + \bar{d}_{L} \left[-\frac{s_{\alpha}}{v c_{\beta}} \mathbf{m}_{\mathbf{d}} + \frac{c_{\beta \alpha}}{c_{\beta}} \mathbf{X}^{d} \right] d_{R} h \qquad \mathbf{X}^{\mathbf{u}} = V_{L}^{u} \frac{Y_{1}^{u}}{\sqrt{2}} V_{R}^{u\dagger} \\ &+ \bar{\ell}_{L} \left[-\frac{s_{\alpha}}{v c_{\beta}} \mathbf{m}_{\ell} + \frac{c_{\beta \alpha}}{c_{\beta}} \mathbf{X}^{\ell} \right] \ell_{R} h + h.c. \,, \qquad \qquad \mathbf{X}^{\mathbf{d}} = V_{L}^{d} \frac{Y_{2}^{d}}{\sqrt{2}} V_{R}^{d\dagger} \, \mathbf{X}^{\ell} = V_{L}^{\ell} \frac{Y_{2}^{\ell}}{\sqrt{2}} V_{R}^{\ell\dagger} \end{aligned}$$

H,A couplings:

$$\begin{aligned} & + A \text{ couplings:} \\ -\mathcal{L}_{Y}^{H,A} &= \bar{u}_{L} \left[\frac{s_{\alpha}}{vs_{\beta}} \mathbf{m}_{\mathbf{u}} + \frac{s_{\beta\alpha}}{s_{\beta}} \mathbf{X}^{u} \right] u_{R}H + \bar{d}_{L} \left[\frac{c_{\alpha}}{vc_{\beta}} \mathbf{m}_{\mathbf{d}} - \frac{s_{\beta\alpha}}{c_{\beta}} \mathbf{X}^{d} \right] d_{R}H \\ &+ \bar{\ell}_{L} \left[\frac{c_{\alpha}}{vc_{\beta}} \mathbf{m}_{\ell} - \frac{s_{\beta\alpha}}{c_{\beta}} \mathbf{X}^{\ell} \right] \ell_{R}H + i\bar{u}_{L} \left[-\frac{\cot\beta}{v} \mathbf{m}_{\mathbf{u}} + \frac{\mathbf{X}^{u}}{s_{\beta}} \right] u_{R}A \\ &+ i\bar{d}_{L} \left[-\frac{\tan\beta}{v} \mathbf{m}_{\mathbf{d}} + \frac{\mathbf{X}^{d}}{c_{\beta}} \right] d_{R}A + i\bar{\ell}_{L} \left[-\frac{\tan\beta}{v} \mathbf{m}_{\ell} + \frac{\mathbf{X}^{\ell}}{s_{\beta}} \right] \ell_{L}A + h.c. \end{aligned}$$

$$\begin{aligned} & = \delta_{L} \left[-\frac{\tan\beta}{v} \mathbf{m}_{\mathbf{d}} + \frac{\mathbf{X}^{d}}{c_{\beta}} \right] d_{R}A + i\bar{\ell}_{L} \left[-\frac{\cosh\beta}{v} \mathbf{m}_{\mathbf{u}} + \frac{\mathbf{X}^{\ell}}{s_{\beta}} \right] u_{R}A \\ &+ i\bar{d}_{L} \left[-\frac{\tan\beta}{v} \mathbf{m}_{\mathbf{d}} + \frac{\mathbf{X}^{d}}{c_{\beta}} \right] d_{R}A + i\bar{\ell}_{L} \left[-\frac{\tan\beta}{v} \mathbf{m}_{\ell} + \frac{\mathbf{X}^{\ell}}{s_{\beta}} \right] \ell_{L}A + h.c. \end{aligned}$$

$$\begin{aligned} & = \delta_{L} \left[-\frac{\delta_{L}}{v} \mathbf{m}_{\mathbf{d}} + \frac{\mathbf{X}^{d}}{c_{\beta}} \right] d_{R}A + i\bar{\ell}_{L} \left[-\frac{\cos\beta}{v} \mathbf{m}_{\mathbf{d}} + \frac{\mathbf{X}^{\ell}}{s_{\beta}} \right] u_{R}A \\ &+ i\bar{d}_{L} \left[-\frac{\tan\beta}{v} \mathbf{m}_{\mathbf{d}} + \frac{\mathbf{X}^{d}}{s_{\beta}} \right] d_{R}A + i\bar{\ell}_{L} \left[-\frac{\tan\beta}{v} \mathbf{m}_{\ell} + \frac{\mathbf{X}^{\ell}}{s_{\beta}} \right] u_{R}A \\ &- \mathcal{L}_{Y}^{H^{\pm}} = \sqrt{2}\bar{d}_{L}V_{CKM} \left[-\frac{\cos\beta}{v} \mathbf{m}_{\mathbf{u}} + \frac{\mathbf{X}^{u}}{s_{\beta}} \right] u_{R}H^{-} \\ &+ \delta_{L} \left[-\frac{\sin\beta}{v} \mathbf{m}_{\mathbf{d}} + \frac{\mathbf{X}^{d}}{c_{\beta}} \right] d_{R}H^{+} \\ &+ \delta_{L} \left[-\frac{\tan\beta}{v} \mathbf{m}_{\mathbf{d}} + \frac{\mathbf{X}^{d}}{c_{\beta}} \right] d_{R}H^{+} \\ &+ \delta_{L} \left[-\frac{\cos\beta}{v} \mathbf{m}_{L} + \frac{\mathbf{X}^{\ell}}{c_{\beta}} \right] d_{R}H^{+} \\ &+ \delta_{L} \left[-\frac{\sin\beta}{v} \mathbf{m}_{L} + \frac{\mathbf{X}^{\ell}}{c_{\beta}} \right] \ell_{R}H^{+} \\ &+ \delta_{L} \left[-\frac{\sin\beta}{v} \mathbf{m}_{L} + \frac{\mathbf{X}^{\ell}}{c_{\beta}} \right] \ell_{R}H^{+} \\ &+ \delta_{L} \left[-\frac{\sin\beta}{v} \mathbf{m}_{L} + \frac{\mathbf{X}^{\ell}}{c_{\beta}} \right] \ell_{R}H^{+} \\ &+ \delta_{L} \left[-\frac{\sin\beta}{v} \mathbf{m}_{L} + \frac{\mathbf{X}^{\ell}}{c_{\beta}} \right] \ell_{L}H^{+} \\ &+ \delta_{L} \left[-\frac{\sin\beta}{v} \mathbf{m}_{L} + \frac{\mathbf{X}^{\ell}}{c_{\beta}} \right] \ell_{L}H^{+} \\ &+ \delta_{L} \left[-\frac{\sin\beta}{v} \mathbf{m}_{L} + \frac{\mathbf{X}^{\ell}}{c_{\beta}} \right] \ell_{L}H^{+} \\ &+ \delta_{L} \left[-\frac{\delta}{v} \mathbf{m}_{L} + \frac{\delta}{c_{\beta}} \right] \ell_{L} \\ &+ \delta_{L} \left[-\frac{\delta}{v} \mathbf{m}_{L} + \frac{\delta}{c_{\beta}} \right] \ell_{L} \\ &+ \delta_{L} \left[-\frac{\delta}{v} \mathbf{m}_{L} + \frac{\delta}{c_{\beta}} \right] \ell_{L} \\ &+ \delta_{L} \left[-\frac{\delta}{v} \mathbf{m}_{L} + \frac{\delta}{c_{\beta}} \right] \ell_{L} \\ &+ \delta_{L} \left[-\frac{\delta}{v} \mathbf{m}_{L} + \frac{\delta}{c_{$$

To suppress the tree FCNCs, we take Cheng-Sher ansatz,

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$$-\mathcal{L}_{Y}^{H^{\pm}} = \sqrt{2}\bar{d}_{L}V_{CKM}^{\dagger} \left[-\frac{\cot\beta}{v}\mathbf{m}_{u} + \frac{\mathbf{X}^{u}}{s_{\beta}} \right] u_{R}H^{-}$$

$$X_{ij}^{f} = \frac{\sqrt{m_{i}^{f}m_{j}^{f}}}{v}\chi_{ij}^{f}, \ \chi_{ij}^{f} \text{ are free parameters} + \sqrt{2}\bar{u}_{L}V_{CKM} \left[-\frac{\tan\beta}{v}\mathbf{m}_{d} + \frac{\mathbf{X}^{d}}{c_{\beta}} \right] d_{R}H^{+}$$
Enhancement factor of H^{\pm} coupling:
$$+ \sqrt{2}\bar{\nu}_{L}V_{PMNS} \left[-\frac{\tan\beta}{v}\mathbf{m}_{\ell} + \frac{\mathbf{X}^{\ell}}{c_{\beta}} \right] \ell_{R}H^{+} + h.c.,$$

- Lepton current in $b \to c \,\ell\nu$: $tan\beta \sim \frac{m_t}{m_b}$, $\chi^{\ell}_{\tau\tau} \sim O(1-10)$
- Quark current: for simplicity we take $\chi_{ij}^d \ll 1$, the interesting enhancement factor:

$$(\mathbf{V}^{\dagger}\mathbf{X}^{\mathbf{u}})_{bc} = V_{ub}^{*}X_{uc}^{u} + V_{cb}^{*}X_{cc}^{u} + V_{tb}^{*}X_{tc}^{u},$$
$$\approx \frac{\sqrt{m_{t}m_{c}}}{v}\chi_{tc}^{u}, \qquad V_{ub}, V_{cb} \ll V_{tb} \approx 1$$
Numerically, $\frac{\sqrt{m_{c}m_{t}}}{v} \approx 0.06 \sim V_{cb} \approx 0.04$, if $\chi_{tc}^{u} \sim O(1) \rightarrow$ an enhancement factor

Phenomenological analysis of $B \rightarrow D^{(*)} \ell \nu$

□ The SM W + H^{\pm} -mediated effects



- $H \supset \frac{G_F}{\sqrt{2}} V_{cb}(\bar{c}b)_{V-A}(\bar{\ell}\nu_\ell)_{V-A}$
- The effective Hamiltonian



$$\begin{aligned} H_{\text{eff}} &= \frac{G_F}{\sqrt{2}} V_{cb} \left[(\bar{c}b)_{V-A} (\bar{\ell}\nu)_{V-A} + C_L^{\ell} (\bar{c}b)_{S-P} (\bar{\ell}\nu)_{S-P} + C_R^{\ell} (\bar{c}b)_{S+P} (\bar{\ell}\nu)_{S-P} \right] \\ & C_L^{\ell} \approx -\frac{m_c m_\ell}{m_{H^{\pm}}^2} \left(1 - \frac{\chi_{\ell\ell}^{\ell}}{s_{\beta}} \right) \left(1 - \sqrt{\frac{m_t}{m_c}} \frac{\chi_{ct}^u}{c_{\beta}V_{cb}} \right) \,, \\ & C_R^{\ell} \approx -\frac{m_b m_\ell \tan^2 \beta}{m_{H^{\pm}}^2} \left(1 - \frac{\chi_{\ell\ell}^{\ell}}{s_{\beta}} \right) \,. \end{aligned}$$

▶ Decay amplitudes of $B \to D^{(*)} \ell \bar{\nu}_{\ell}$

$$\begin{split} A_{D} &= \frac{G_{F}}{\sqrt{2}} V_{cb} \left[F_{1} \left(P^{\mu} - \frac{P \cdot q}{q^{2}} q^{\mu} \right) (\bar{\ell}\nu)_{V-A} \right. \\ &+ \left(m_{\ell} F_{0} \frac{P \cdot q}{q^{2}} + \left(C_{R}^{\ell} + C_{L}^{\ell} \right) (m_{B} + m_{D}) F_{S} \right) (\bar{\ell}\nu)_{S-P} \right] \\ A_{D^{*}}^{L} &= -i \frac{G_{F}}{\sqrt{2}} V_{cb} \left\{ \epsilon^{*} \cdot q \left(\left(C_{R}^{\ell} - C_{L}^{\ell} \right) F_{P} + 2A_{0} \frac{m_{D^{*}} m_{\ell}}{q^{2}} \right) (\bar{\ell}\nu)_{S-P} \right. \\ &+ \left[(m_{B} + m_{D^{*}}) A_{1} \left(\epsilon^{*}_{\mu} (L) - \frac{\epsilon^{*} \cdot q}{q^{2}} q_{\mu} \right) - \frac{A_{2} \epsilon^{*} \cdot q}{m_{B} + m_{D}} \left(P_{\mu} - \frac{P \cdot q}{q^{2}} q_{\mu} \right) \right] (\bar{\ell}\nu)_{V-A} \,, \\ A_{D^{*}}^{T} &= \frac{G_{F}}{\sqrt{2}} V_{cb} \left[\frac{V}{m_{B} + m_{D^{*}}} \varepsilon_{\mu\nu\rho\sigma} \epsilon^{*}_{\nu} (T) P^{\rho} q^{\sigma} - i(m_{B} + m_{D^{*}}) A_{1} \epsilon^{*}_{\mu} (T) \right] (\bar{\ell}\nu)_{V-A} \,, \end{split}$$

- $C^{\mu}_{R,L} \propto m_{\mu}$, influence could be small, we drop them with $\chi^{\ell}_{22} \ll 1$
- $|C_L^{\tau}| < |C_R^{\tau}|$, $C_R^{\tau} < 0$ in type-II 2HDM, destructive contribution
- To obtain constructive interference with the SM, we need $C_R^{\tau} \pm C_L^{\tau} > 0$, $C_R^{\tau} > 0 > C_L^{\tau}$

> Generic 2HDM, we need $\chi^{\ell}_{\tau\tau}$ to change the sign of C_R^{τ} ; we also need χ_{ct}^u so that $C_L^{\ell} \approx -\frac{m_c m_\ell}{m_{L^+}^2} \left(1 - \frac{\chi_{\ell\ell}^{\epsilon}}{s_\beta}\right) \left(1 - \sqrt{\frac{m_t^-}{m_c}} \frac{\chi_{ct}^u}{c_\beta V_{ch}}\right)$, $C_R^{\ell} \approx -\frac{m_b m_\ell \tan^2 \beta}{m_{\mu +}^2} \left(1 - \frac{\chi_{\ell \ell}^{\ell}}{s_\beta} \right) \,.$ $C_L^{\tau} < 0$; that is, we need two parameters to enhance R(D) and $R(D^*)$ > Ratios of the BR of $D^{(*)}\tau$ to $D^{(*)}\ell$ modes Fajfer etal, PRD85(12) $R_D \approx R_D^{\rm SM} \left[1 + 1.5 Re(C_R^{\tau} + C_L^{\tau}) + 1.0 |C_R^{\tau} + C_L^{\tau}|^2 \right] \,,$ $R_{D^*} \approx R_{D^*}^{\rm SM} \left[1 + 0.12 Re(C_R^{\tau} - C_L^{\tau}) + 0.05 |C_R^{\tau} - C_L^{\tau}|^2 \right] .$ 0.8F 0.31 0.29 0.30.27 0.26 0.6 0.6 R_D 0.31 $\chi^{\ell}_{\tau\tau} = 4$ $\tan\beta = 40$ 0.4 لار $50.4 - m_{H^{\pm}} = 400 \, \text{GeV}$ -0.33 $m_{H^{\pm}} = 400 \, \text{GeV}$ 0.2 0.2 *(a)* 0.0 *(b)* 0.0 0 6 30 50 20 40 108 $\chi^{\ell}_{\tau\tau}$ $tan\beta$

□ Unfortunately, the charged-Higgs effects also enhance the BR for the

 $B_c \rightarrow \tau \nu$ decay, which has not yet observed. $BR(B_c \rightarrow \tau \nu)^{SM} \approx 2.2\%$

> constraint from $BR(B_c \rightarrow \tau \nu) \leq 1$ Li etal JHEP1608(16)

> Based on the inconsistency in B_c lifetime between experimental

data and theoretical estimation, it is found that $BR(B_c \rightarrow \tau \nu) \leq 30\%$



Limit on the BR($B_c \rightarrow \tau \nu$) from LEP1

References

□ Although the result of $BR(B_c \rightarrow \tau \nu) \leq 30\%$ limits R(D*) < 0.29, the

deviation from the SM of $R(D^*)=0.25$ is still significant.

□ Can we further bound the BR of $B_c \rightarrow \tau \nu$?

→ B_c contributing to $B \rightarrow \tau \nu$ was investigated

The contribution of B_c mesons to the search for $B^+ \to \tau^+ v_{\tau}$ decays at LEP Michelangelo L. Mangano ^{a, 1} , S.R. Slabospitsky ^b PLB410(97)

E Show more

$$\begin{split} N_{P}: \# \ of \ \tau\nu \ from \ P \to \tau\nu \\ \frac{N_{B_{c}}}{N_{B_{u}}} &= \left. \frac{f(b \to B_{c})}{f(b \to B_{u})} \left| \frac{V_{cb}}{V_{ub}} \right|^{2} \left(\frac{f_{B_{c}}}{f_{B_{u}}} \right)^{2} \frac{m_{B_{c}}}{m_{B_{u}}} \frac{\tau_{B_{c}}}{\tau_{B_{u}}} \frac{(1 - \frac{m_{\tau}^{2}}{m_{B_{c}}^{2}})^{2}}{(1 - \frac{m_{\tau}^{2}}{m_{B_{u}}^{2}})^{2}}, & f(b \to P): \text{probability} \\ \text{that a b-quark} \\ \text{hadronizes into a P} \\ \text{although } f(b \to B_{u}) \gg f(b \to B_{c}), \ V_{ub} \ll V_{cb} \\ \frac{N_{B_{c}}}{N_{B_{u}}} &= 1.2 \left[\frac{f(b \to B_{c})}{10^{-3}} \right] & \text{Br}(B_{u} \to \tau\nu) < 5.7 \times 10^{-4} \quad (90\% \ CL) . \\ \text{LEP(L3) PLB396(97)} \\ \text{Need to take the contamination from Bc} \\ 10 \end{split}$$

□ Following MS approach, we updated the N_{B_c}/N_{B_u} with more accurate f_B and CKM matrix elements in Akeroyd etal PRD77(08); a specific limit on $BR(B_c \rightarrow \tau \nu)$ did not explicitly show

□ Can the bound of the BR($B_c \rightarrow \tau \nu$) from the LEP be more strict?

- We reexamine the LEP (L3) bound with updated CDF run II data and LHC results
- > The effective BR for $b \rightarrow \tau \nu$ can be expressed as:

$$BR_{eff} = BR(B_u^- \to \tau\bar{\nu}) \left(1 + \frac{N_c}{N_u}\right) \qquad \frac{N_c}{N_u} = \frac{f_c}{f_u} \frac{BR(B_c^- \to \tau\bar{\nu})}{BR(B_u^- \to \tau\bar{\nu})}$$

model-independent

$$BR(B_c^- \to \tau\bar{\nu}) = \frac{f_u}{f_c} \left[BR_{eff} - BR(B_u^- \to \tau\bar{\nu}) \right]$$

 $BR_{\rm eff} < 5.7 \times 10^{-4} \ (L3); BR(B_u \to \tau \nu)^{exp} = (1.06 \pm 0.09) \times 10^{-4}$

If we can determine f_u/f_c , then we can give an upper limit on $B_c \rightarrow \tau \nu$

□ Using $f_u = 0.404 \pm 0.006$ (HFLAV) and $f_c \sim 10^{-3}$, $\frac{BR(B_c \to \tau \nu)}{N} \sim 18.7\%$

 $\Box f_c/f_u$ from CDF Run II and LHC data:

CDF measured the ratio:
theoretical input

$$\mathcal{R}_{\ell} = \frac{\sigma(B_c) \cdot \mathrm{BR}(B_c^- \to J/\psi \ell \bar{\nu})}{\sigma(B_u) \cdot \mathrm{BR}(B_u^- \to J/\psi K^-)}$$
 from B factory

 $\frac{f_c}{f_u} = \frac{f(b \to B_c)}{f(b \to B_u)} = \frac{\sigma(B_c)}{\sigma(B_u)}$

	PRD58(98)	PRD93(16)		
\mathcal{R}_ℓ	0.13 ± 0.06	0.211 ± 0.024	0.171 ± 0.032	0.143 ± 0.017
	Tevatron Run I	Tevatron Run II	Average I+II	LHC

> LHC does not directly show the observation of R_{ℓ} ; but the measurements are shown:

$$R_{\pi/K} = \frac{\sigma(B_c)}{\sigma(B_u)} \frac{BR(B_c \to J/\psi\pi^-)}{BR(B_u \to J/\psiK^-)} = (6.72 \pm 0.19) \times 10^{-3},$$

$$R_{\pi/\mu} = \frac{BR(B_c \to J/\psi\pi^-)}{BR(B_c \to J/\psi\mu\nu)} = 0.0469 \pm 0.0054$$

$$\mathcal{R}_{\ell} = \frac{\mathcal{R}_{\pi/K}}{\mathcal{R}_{\pi/\mu}} = 0.143 \pm 0.017$$

▶ The theoretical estimations of $BR(B_c \rightarrow J/\psi \ell \nu)$ are diverse

TABLE XX. Branching-fraction predictions for the decay $B_c^+ \to J/\psi \,\mu^+ \nu$.

Branching-fraction predictions in $\%$														
Reference	[5]	[39]	[40]	[41]	[6]	[42]	[43]	[44]	[45]	[46]	[47]	[48]	[49]	CDI
Prediction	1.9	2.37	1.44	1.21	2.07	2.35	1.5	1.2	1.49	1.15	1.47	2.01	6.7	CDF

CDF PRD93(16)

- ► HPQCD lattice results can help to judge: $B_c \rightarrow J/\psi$ form factors at $q^2 = [0, \max]$ are given as $A_1 = [0.49, 0.79]$ and V = [0.77, none]arXiv:1611.01987
- ► $BR(B_c \rightarrow J/\psi \,\ell \nu) = (1.5 2.5)\%$ by the QCD models, which the obtained form factors can match HPQCD results within 15%,

TABLE III: Form factors for $B_c^- \to J/\psi$ at $q^2 = 0$ and q_{max}^2 .

	$(F(0), F(q_{max}^2))$	A_1	V	$\mathrm{BR}(B_c \to J/\Psi \ell \bar{\nu})$
	HPQCD[34]	(0.49, 0.79)	(0.77, None)	None
Rel. quark-meson model	NW[26]	$(0.53, 0.76^a)$	$(0.73, 1.29^a)$	1.47%
Rel. quark model	IKS[28]	(0.55, 0.85)	(0.83,1.53)	2.17%
Light-Front QCD	WSL[31]	(0.50, 0.80)	(0.74, 1.45)	1.49%





▶ Using LEP, Tevatron, and LHC data, we obtain $BR(B_c \rightarrow \tau \nu) \leq 10\%$





 $\mathrm{BR}(B_c^- \to \tau \bar{\nu}) = \mathrm{BR}(B_c^- \to J/\psi \ell \bar{\nu}) \frac{1}{\mathcal{R}_\ell} \frac{\mathrm{BR}_{\mathrm{eff}} - B_u^{exp}}{\mathrm{BR}(B_u^- \to J/\psi K^-)_{exp}}$

 \Box Revisit R(D) and R(D^{*}) by H^{\pm} effects

$$\mathcal{H}_{\text{eff}} = \frac{G_F V_{cb}}{\sqrt{2}} \left[(\bar{c}b)_{V-A} (\bar{\tau}\nu_{\tau})_{V-A} + (C_R^{\tau}(\bar{c}b)_{S+P} + C_L^{\tau}(\bar{c}b)_{S-P}) (\bar{\tau}\nu_{\tau})_{S-P} \right]$$



R(D) can still be as large as 0.4; but, $R(D*) \leq 0.26$ when $BR(B_c \rightarrow \tau \nu) \leq 10\%$ is taken into account

Summary:

 \Box Charged-Higgs in the generic 2HDM can enhance R(D) and R(D^{*})

- □ R(D^{*}) can be limited to be less than 0.29 by the constraint of $BR(B_c \rightarrow \tau \nu) < 30\%$, which is obtained from the B_c lifetime difference between theoretical estimation and data
- □ We find that $BR(B_c \to \tau \nu) < 10\%$ can be achieved by LEP data, R(D) can reach 0.4, but R(D^{*}) ≤ 0.26
- Belle & LHCb with hadronic tau decays show R(D*) is lower than leptonic decays, 0.270(Belle) & 0.285(LHCb); If the excess just occurs in R(D), not in R(D*), the charged-Higgs effects could be the potential candidate