

On Baryogenesis via Neutrino Oscillation in the ν MSM

1

Hiroyuki Ishida (NCTS)

@NCTS Annual Theory Meeting 2017: Particles, Cosmology and Strings

2017/12/06

Collaboration with : Takehiko Asaka (Niigata)

Shintaro Eijima (EPFL→Leiden)

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Based on : PRD 96, 1704.02692 [hep-ph]

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Introduction

- Missing matter field in the SM

Quarks	$\begin{array}{c} u_L \\ \hline u_R \end{array}$	$\begin{array}{c} c_L \\ \hline c_R \end{array}$	$\begin{array}{c} t_L \\ \hline t_R \end{array}$
	$\begin{array}{c} d_L \\ \hline d_R \end{array}$	$\begin{array}{c} s_L \\ \hline s_R \end{array}$	$\begin{array}{c} b_L \\ \hline b_R \end{array}$
Leptons	$\begin{array}{c} \nu_{eL} \\ \hline \end{array}$	$\begin{array}{c} \nu_{\mu L} \\ \hline \end{array}$	$\begin{array}{c} \nu_{\tau L} \\ \hline \end{array}$
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Adding RH neutrinos looks natural!

Introduction

- After adding RH ν s,

$$\mathcal{L}_{\nu mass} = F_{\alpha I} \bar{L}_{\alpha} H \nu_{RI} + \text{h.c.} + \frac{M_M}{2} \overline{\nu_{RI}^c} \nu_{RI}$$

Neutrinos can obtain masses!

- Dirac masses : $M_D \equiv F_{\alpha I} \langle H \rangle$ -Majorana masses : M_M
- Observed tiny ν masses can explain by type-I seesaw
[Minkowski (1977); Yanagida (1979); Gell-Mann, Ramond, Slansky (1979);
Glashow (1980); Mohapatra, Senjanovic (1980)]

$$\hat{M} = \begin{pmatrix} 0 & M_D \\ M_D^T & M_M \end{pmatrix} \xrightarrow[M_D \ll M_M]{\text{diagonalization}} \begin{pmatrix} M_{\nu} & 0 \\ 0 & M_M \end{pmatrix}$$

where $M_{\nu} \simeq -M_D M_M^{-1} M_D^T$

How heavy RH ν is needed?

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- Seesaw mechanism can be applied when...

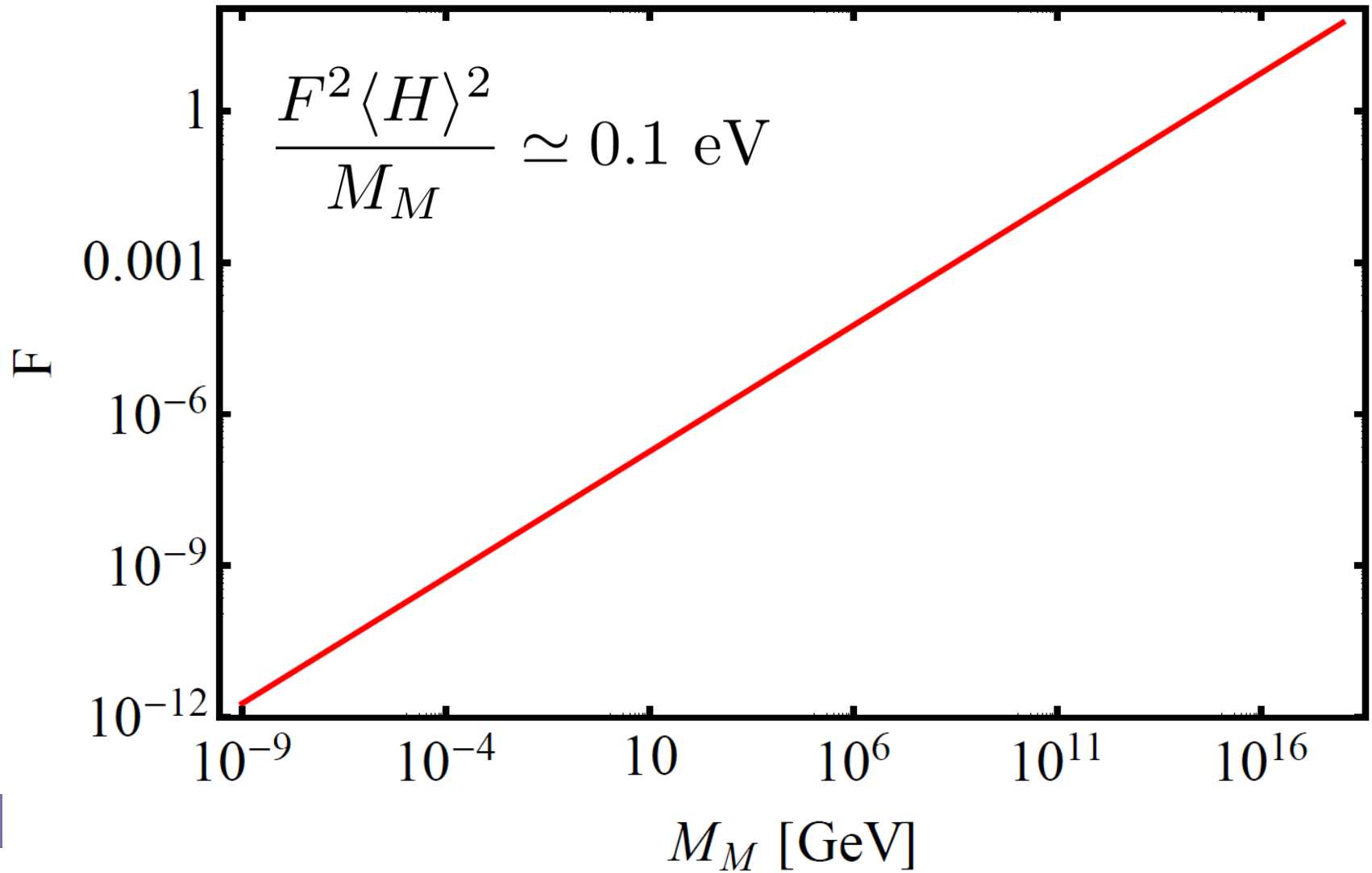
Introduction

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$$\frac{F^2 \langle H \rangle^2}{M_M} \simeq 0.1 \text{ eV}$$

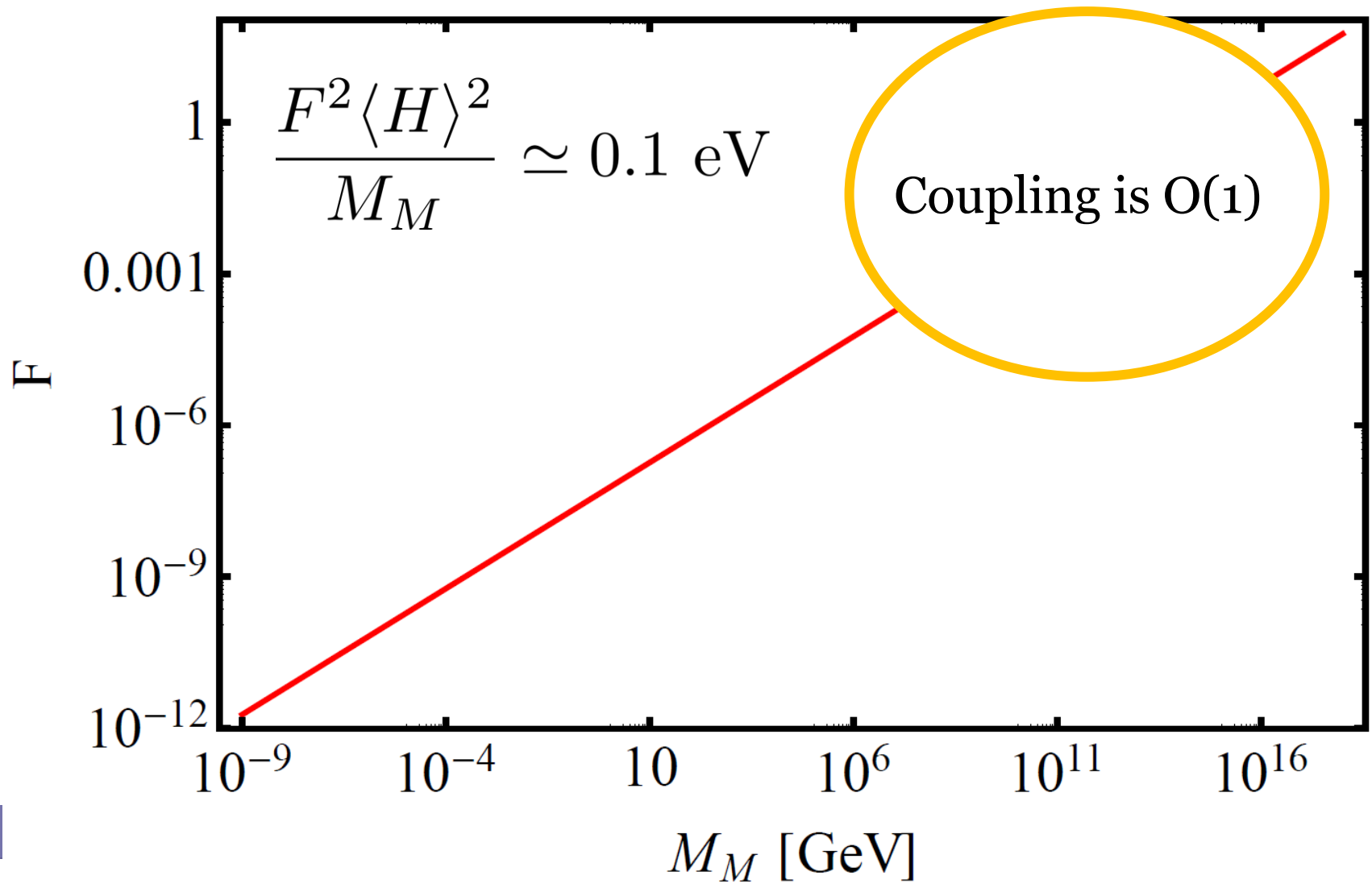
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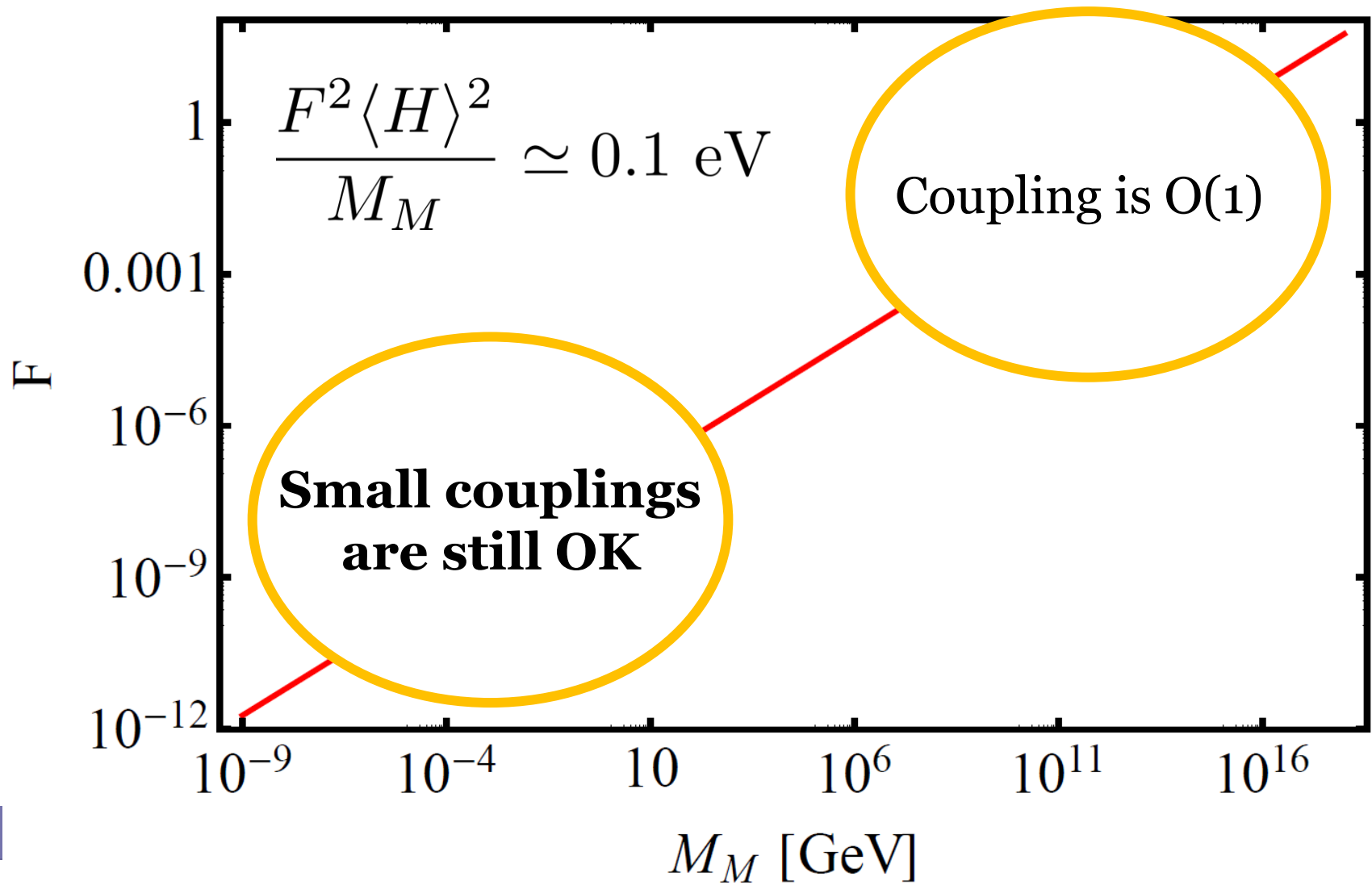
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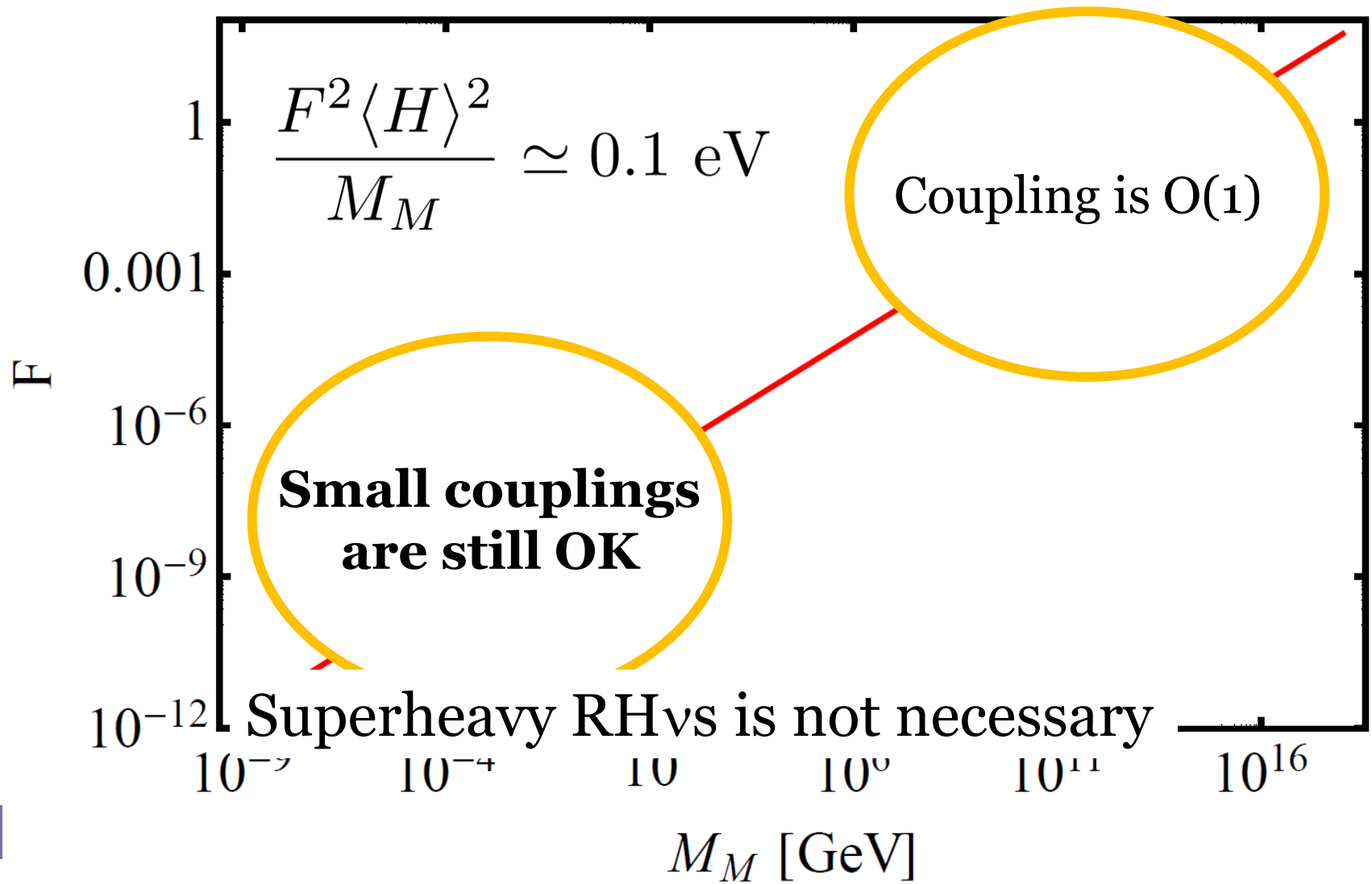
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The Neutrino Minimal Standard Model (The ν MSM)

The ν MSM [Asaka, Blanchet, and Shaposhnikov (2005)] [Asaka and Shaposhnikov (2005)]

- Most economical extension of the SM : SM+3 RH ν s

$$\mathcal{L}_N = i\bar{\nu}_{RI}\not{\partial}\nu_{RI} - F_{\alpha I}\bar{L}_{\alpha}H\nu_{RI} - \frac{M_M}{2}\overline{\nu_{RI}^c}\nu_{RI} + \text{h.c.}$$

- Key assumption

$$M_D \equiv F_{\alpha I}\langle H \rangle \ll M_M \lesssim \Lambda_{\text{EW}}$$

- Typical magnitude of Yukawa couplings

$$M_{\nu} = -M_D M_M^{-1} M_D^T \rightarrow 0.1 \text{ eV} \left(\frac{F}{10^{-7}} \right)^2 \left(\frac{1 \text{ GeV}}{M_M} \right)$$

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Direct testability!

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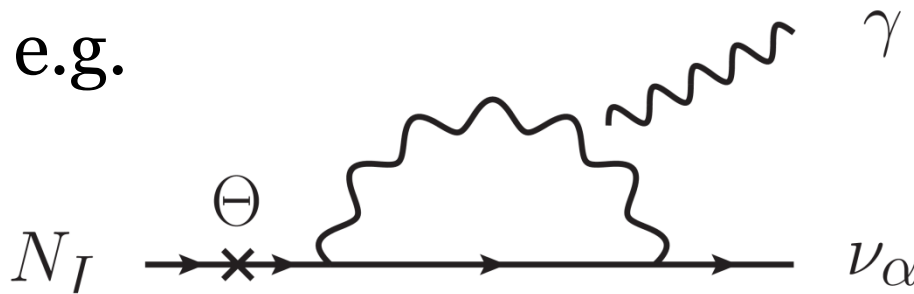
- Physical states of neutrinos

- *active neutrinos : $\nu_i = U_{\text{MNS}}^\dagger \nu_{L\alpha} - U_{\text{MNS}}^\dagger \Theta \nu_{RI}^C$

- *heavy neutral leptons : $N_I^C = \nu_{RI}^C + \Theta^\dagger \nu_{L\alpha}$

- Important parameter : $\Theta \equiv M_D/M_M$

RH ν can have gauge interaction through this mixing



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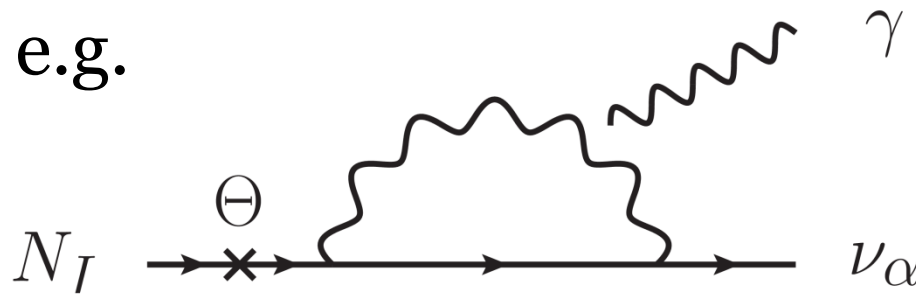
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↪ right-handed neutrinos

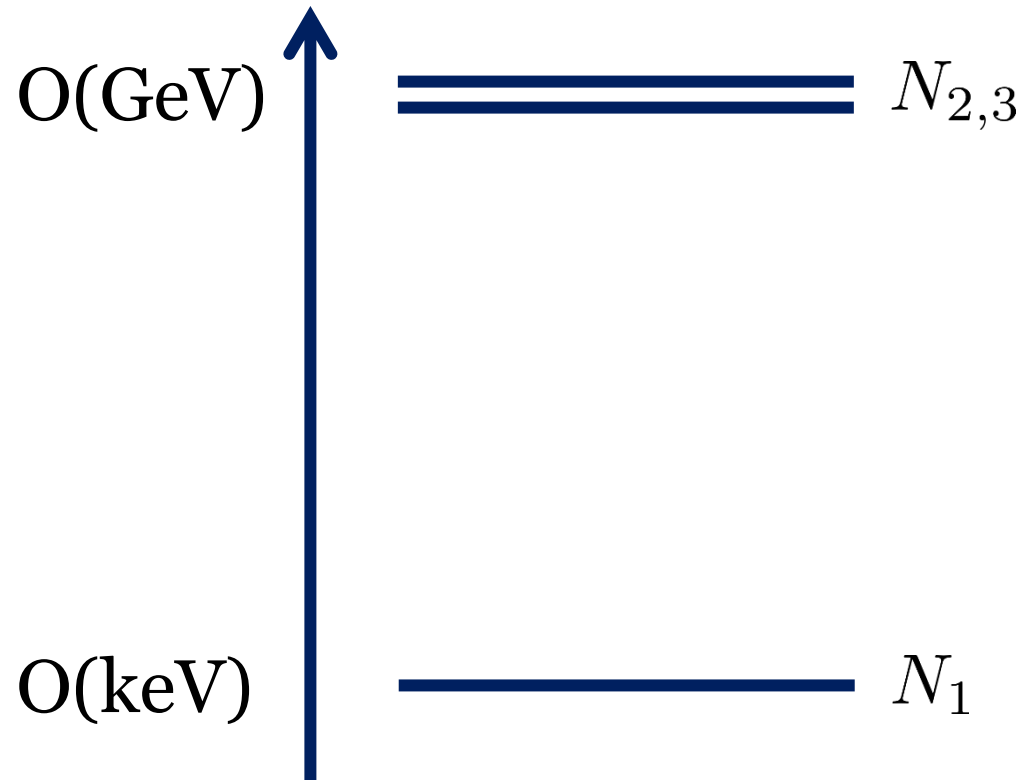
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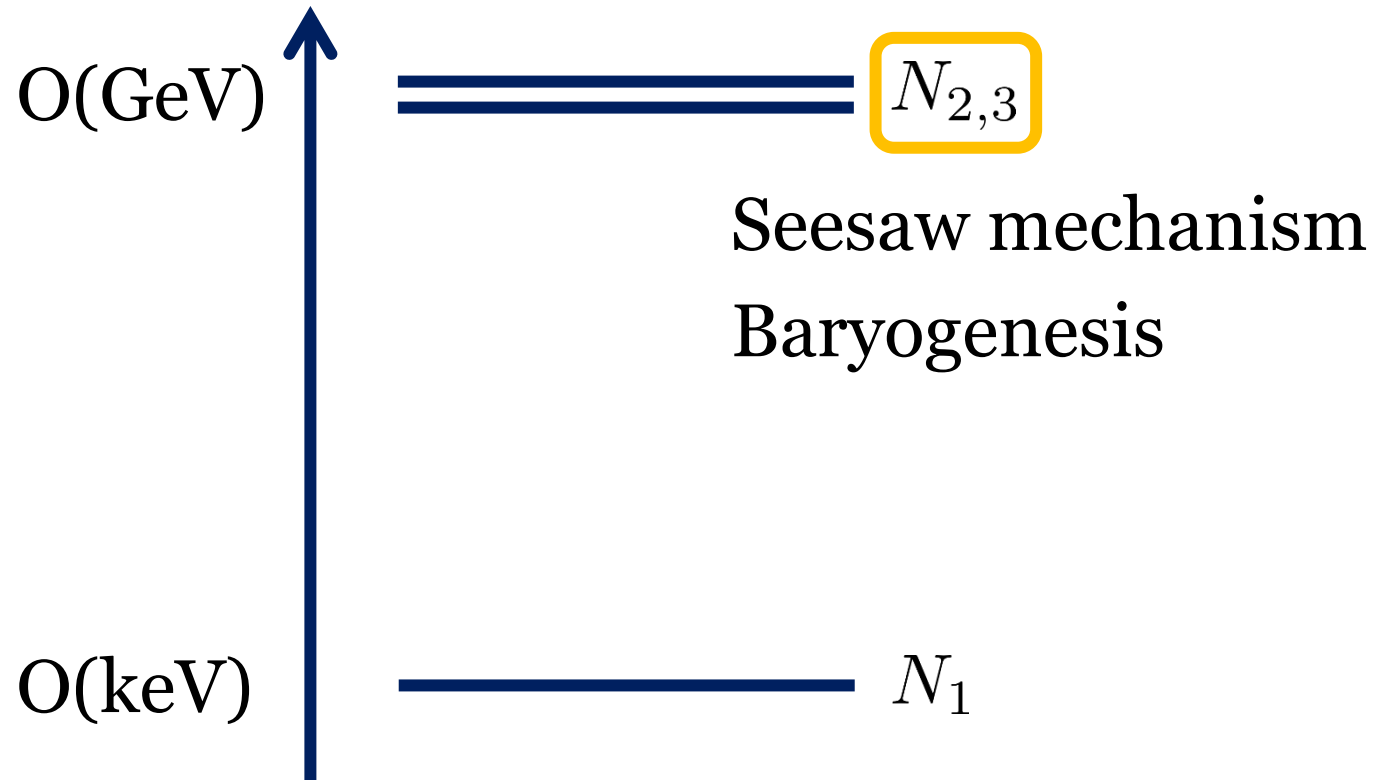
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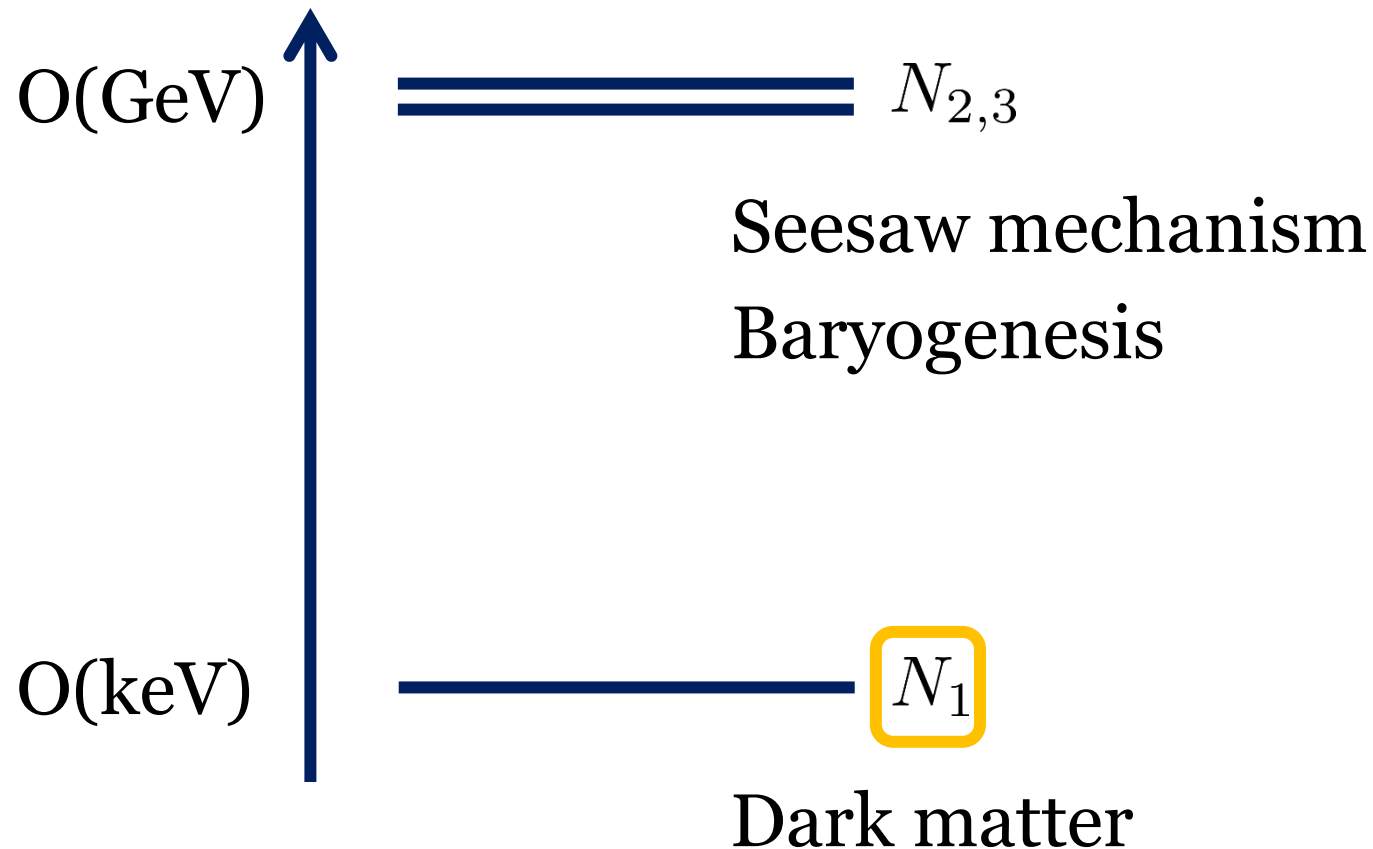
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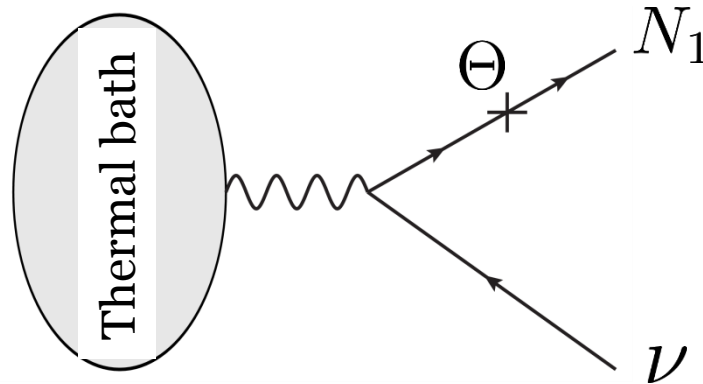


The ν MSM [Asaka, Blanchet, and Shaposhnikov (2005)] [Asaka and Shaposhnikov (2005)]

- Dark matter candidate : N_1

*simple production mechanism (Dodelson-Widrow)

[Dodelson and Widrow (1993)]



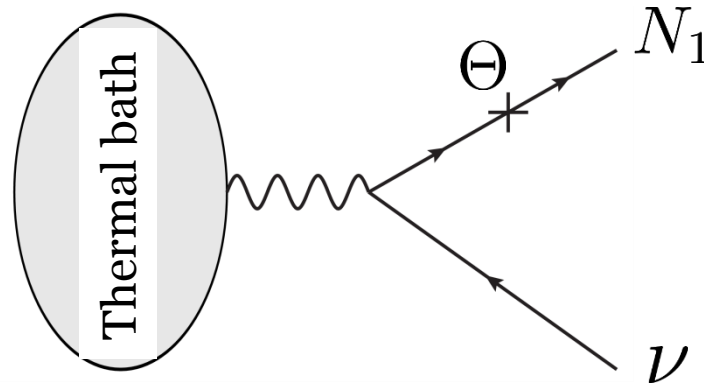
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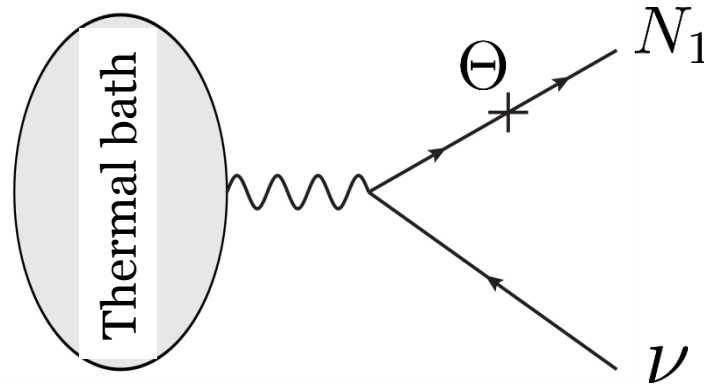
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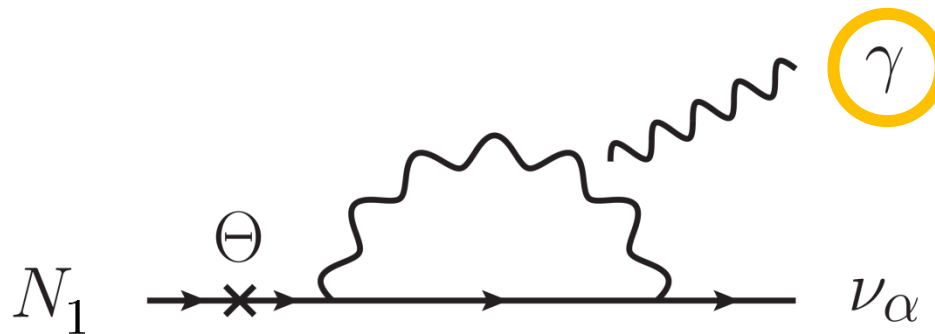
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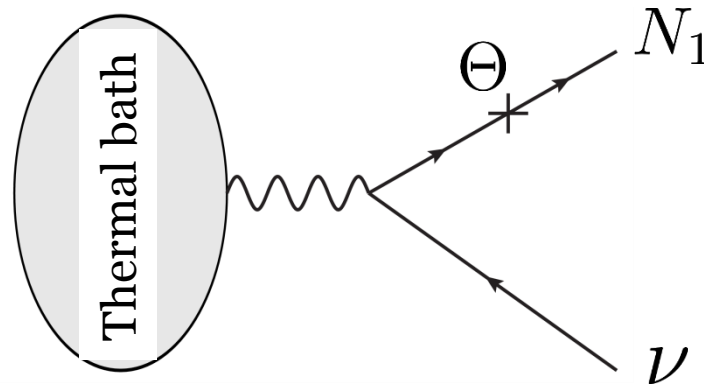


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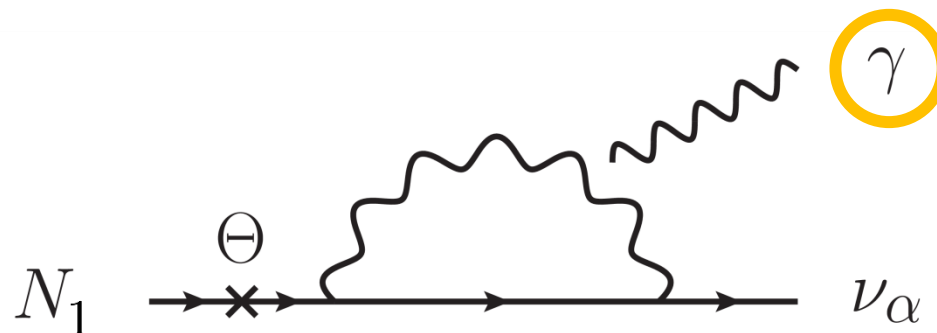
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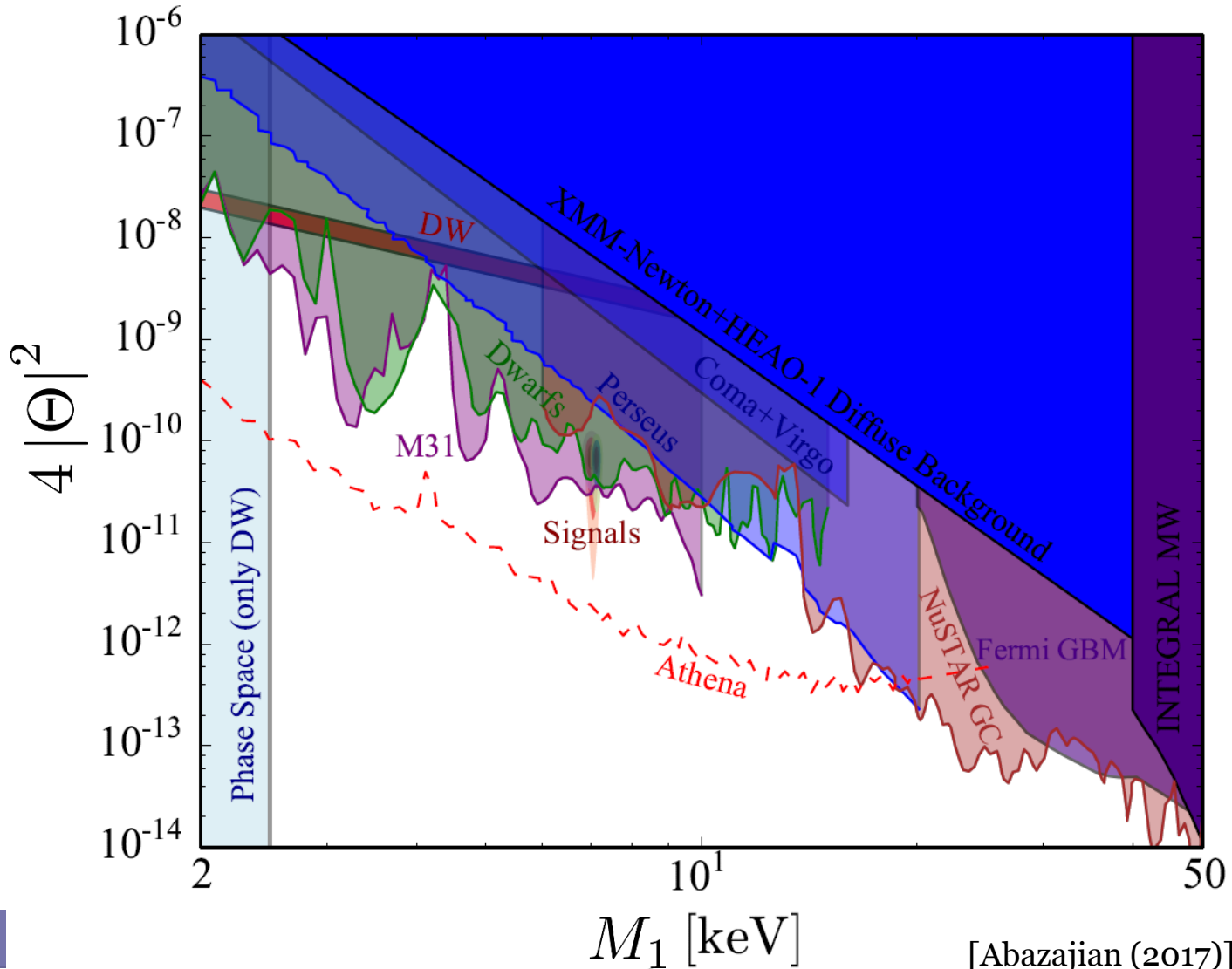


X-ray
observatory

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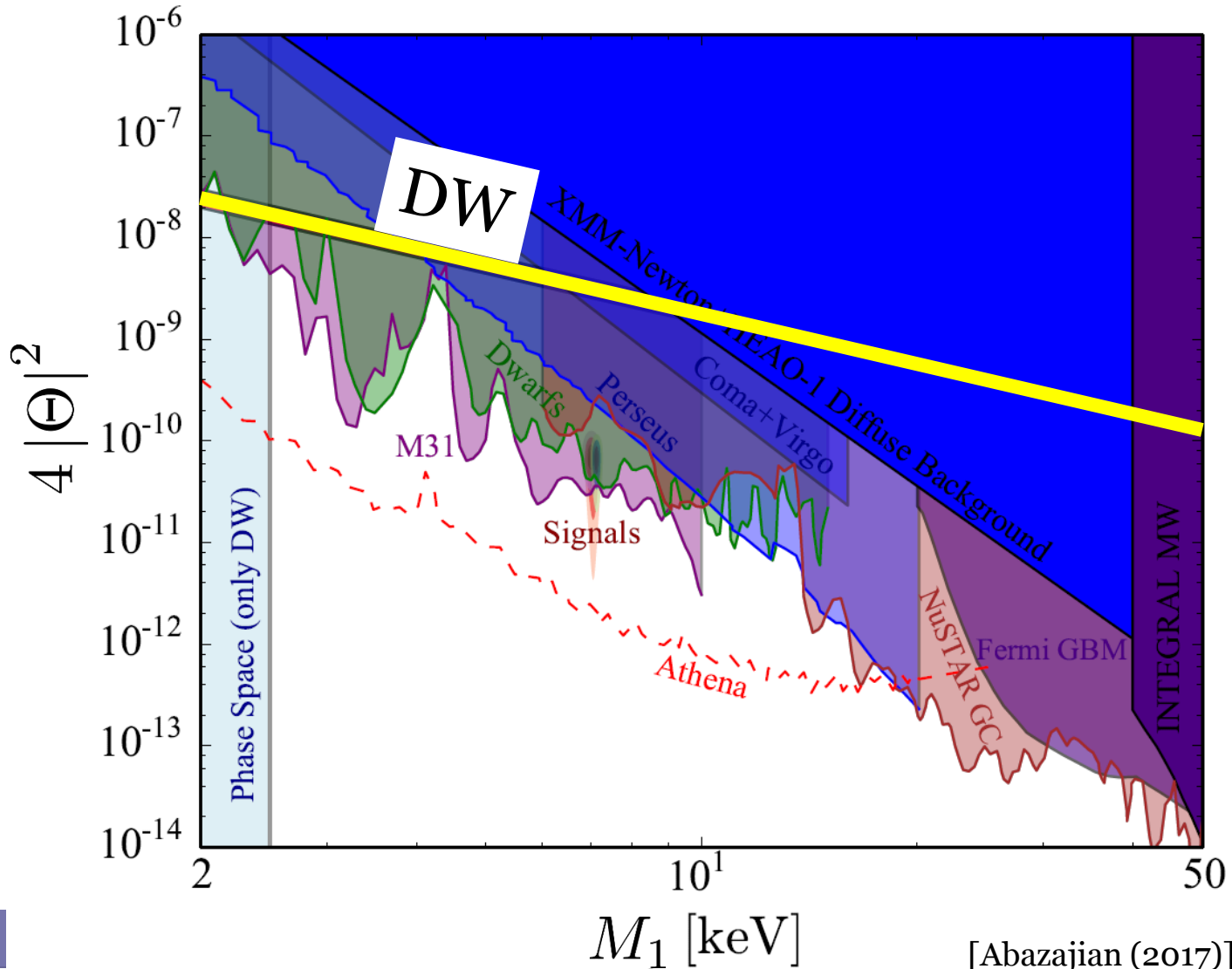
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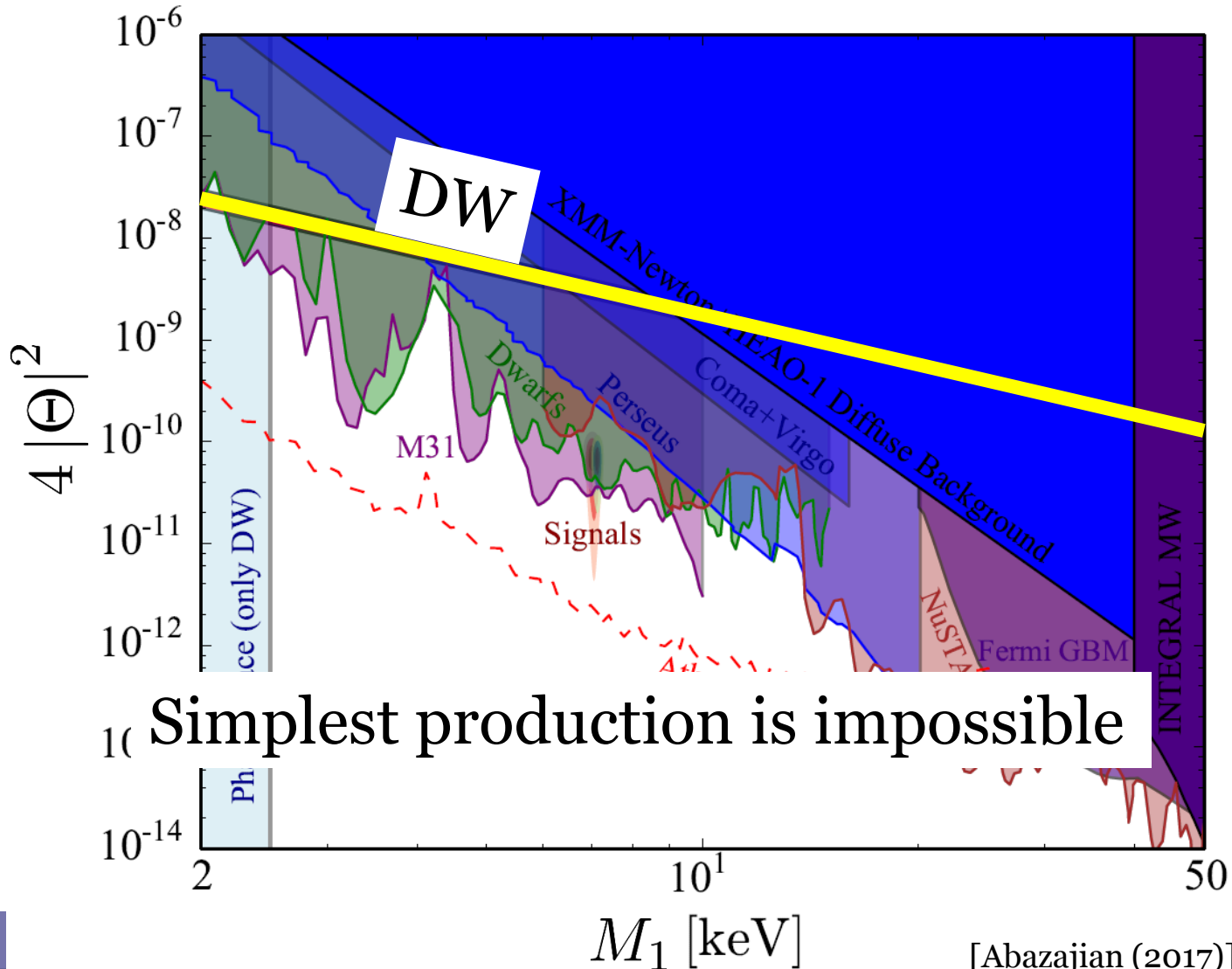
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Roughly speaking,

$$F_{\alpha 1}^2 \sim 10^{-24} \left(\frac{\Theta^2}{10^{-8}} \right) \left(\frac{1 \text{ keV}}{M_1} \right)^2$$

We need really tiny Yukawa coupling for the DM

 Decouple from seesaw relation $\frac{F_{\alpha 1}^2 \langle H \rangle^2}{1 \text{ keV}} \sim 10^{-5} \text{ eV}$

 Consider separately from $N_{2,3}$

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In this talk, I just focus on physics of N_1

Higher dimensional operator for initial conditions of physics in the ν MSM

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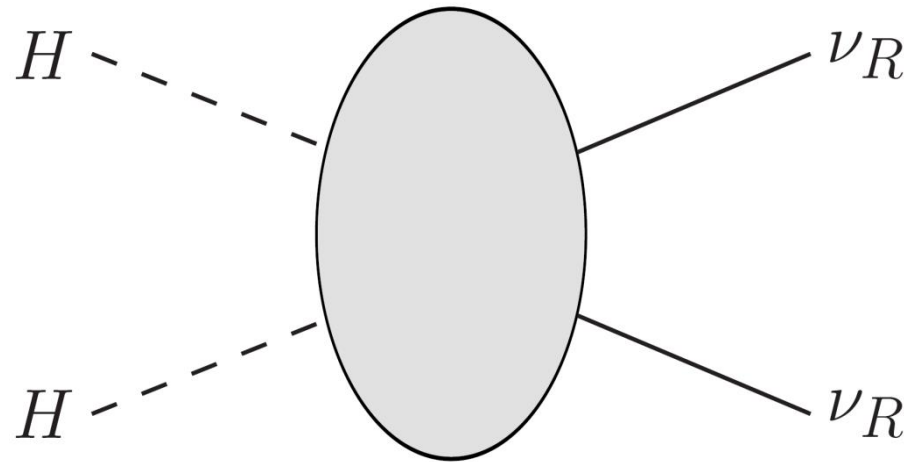
So far...

In the analysis of the BAU and the DM,
no initial $RH\nu$ is assumed.

Higher dimensional operator effect

- RHvs could be produced via...

$$\mathcal{L}_{\text{HD}} = \frac{A_{IJ}}{\Lambda} H^\dagger H \overline{\nu_{RI}^c} \nu_{RJ} + \text{h.c.}$$



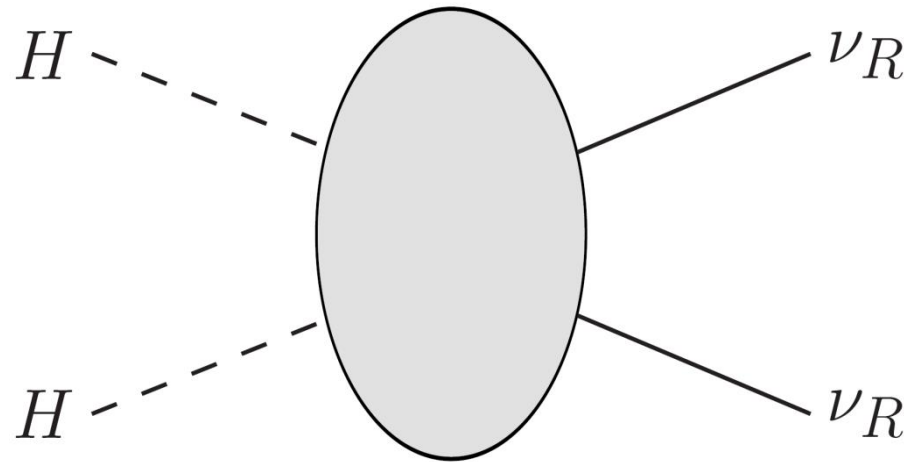
Produced amount of RHvs

$$\begin{aligned} [\rho_N^I]_{IJ} &= \# \times \frac{M_P T_R}{\Lambda^2} [A^\dagger A]_{IJ} \\ &\xrightarrow{\Lambda \rightarrow M_P} \# \times \frac{T_R}{M_P} [A^\dagger A]_{IJ} \end{aligned}$$

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Previous work : [Bezrukov, Gorbunov, and Shaposhnikov (2009)]

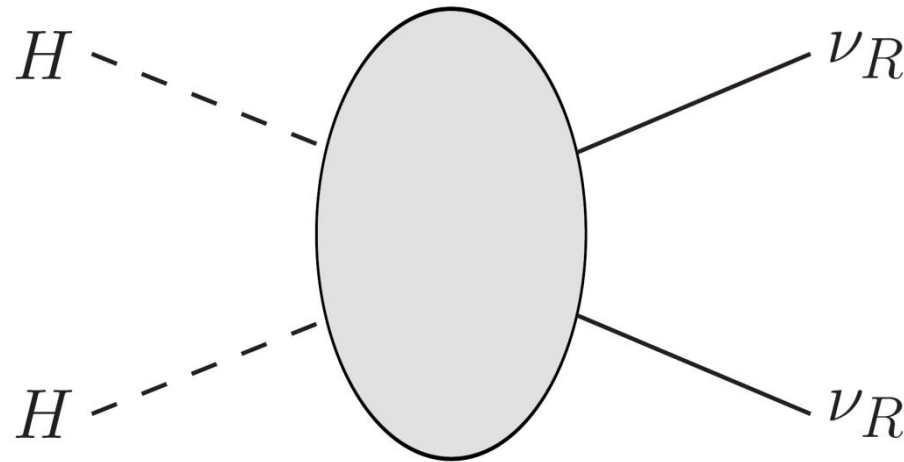
Higgs-driven inflation are low energy phenomena, having nothing to do with inflation. We study then a modification of the ν MSM, adding to its Lagrangian higher dimensional operators suppressed by the Planck scale. The role of these operators in Higgs-driven inflation is clarified. We find that these operators do not contribute to the production of *Warm Dark Matter* (WDM) and to baryogenesis. We also demonstrate that the sterile neutrino with

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$$\longrightarrow \gamma \neq \wedge \frac{1}{M_P} [\chi^\dagger \chi]_{IJ}$$

Higher dimensional operator effect

- Reason of previous conclusions

Produced amount of right-handed neutrino

$$[\rho_N^I]_{IJ} = \# \times \frac{T_R}{M_P} [A^\dagger A]_{IJ}$$

Reheating is governed by Higgs boson decay

$$T_R \simeq (3 - 15) \times 10^{13} \text{ GeV}$$

 $\frac{T_R}{M_P} \sim 10^{-5}$ suppressed enough!!

Here, we just blind ourselves to the reheating

Higher dimensional operator effect

- Effect on (constraint from) DM production

If
$$\sum_{\alpha} |\Theta_{\alpha 1}|^2 \ll 8 \times 10^{-8} \left(\frac{M_1}{1 \text{ keV}} \right)^{-2}$$



DW mechanism does not work at all

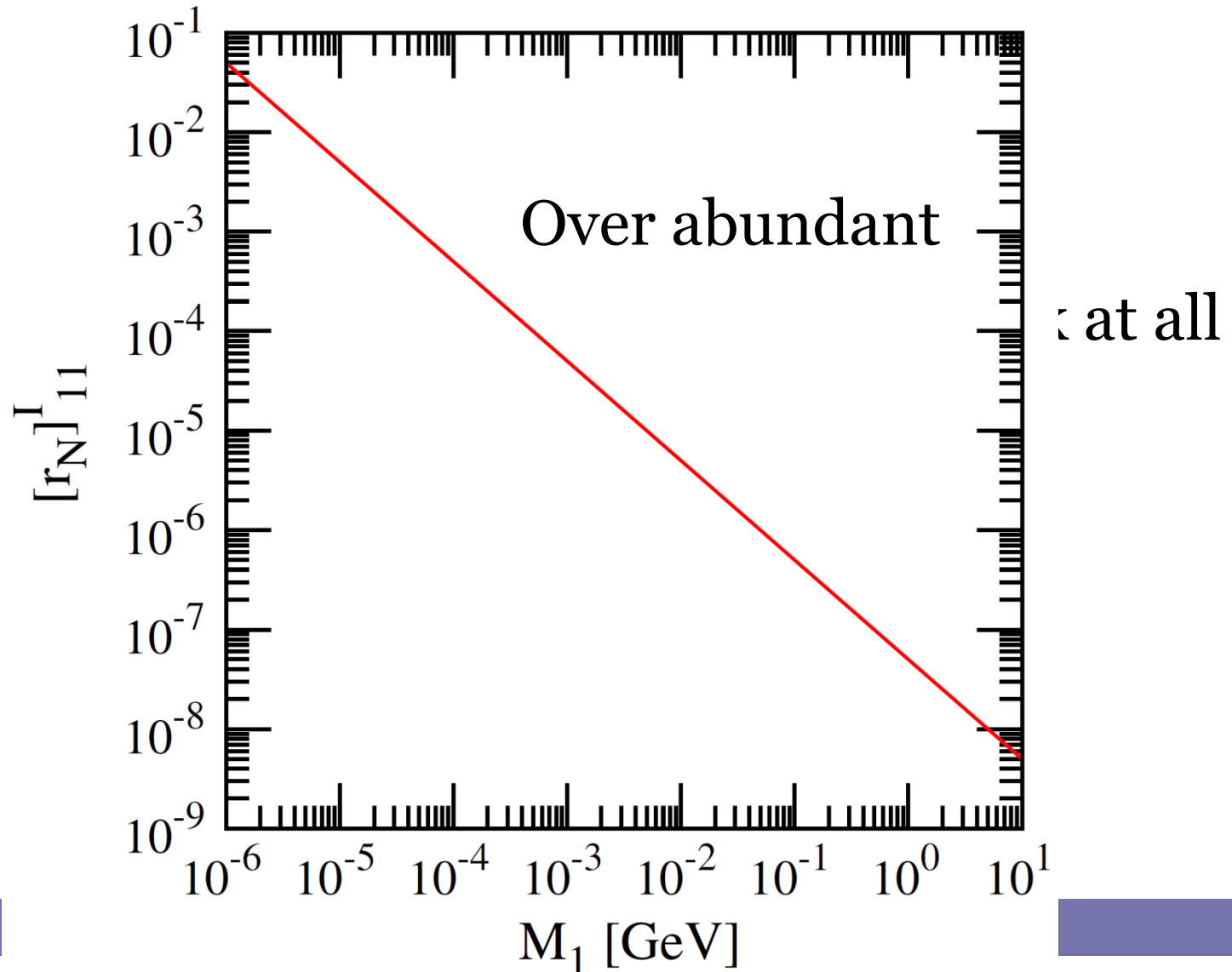


Production via HD operators
becomes more important!!

Higher dimensional operator effect

- Effect on (constraint from) DM production

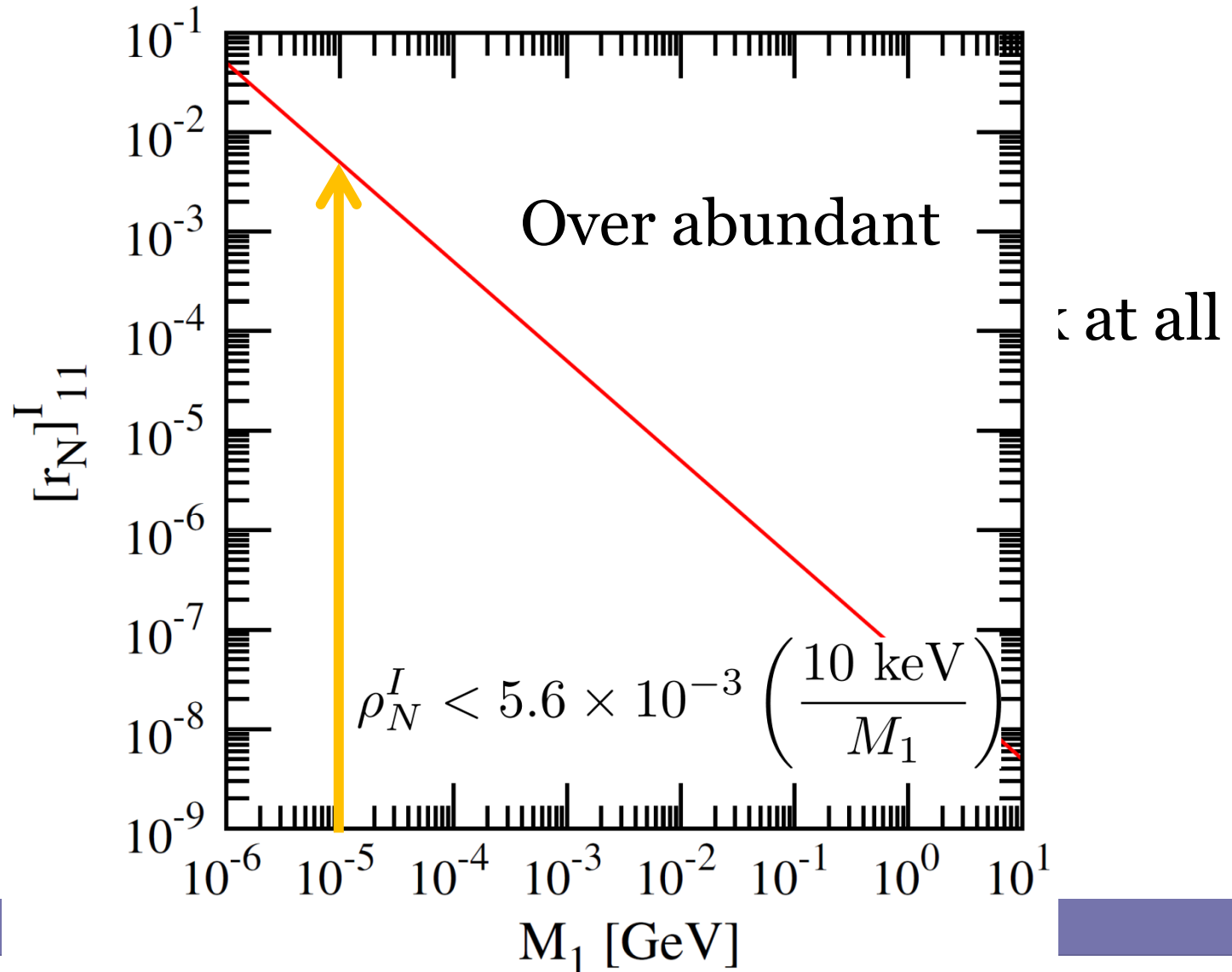
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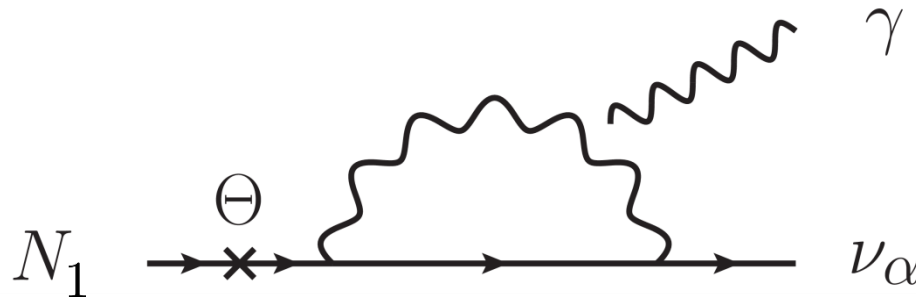
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Higher dimensional operator effect

- When $T_R = 10^{13}$ GeV, $A = \mathcal{O}(1)$

$$M_{N_1} \simeq 5 \text{ GeV}$$

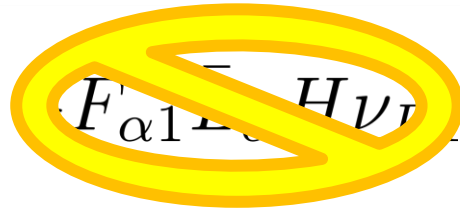
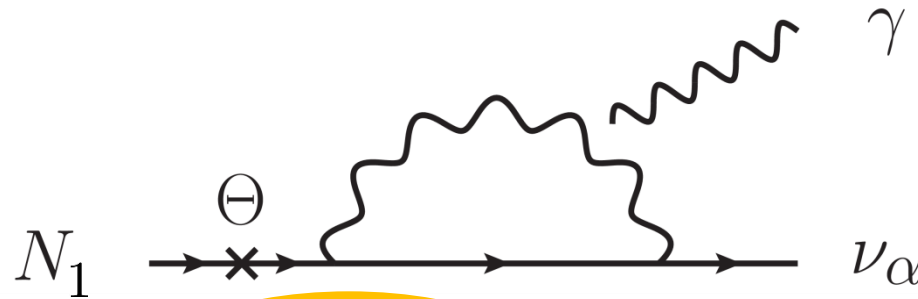


$$-F_{\alpha 1} \bar{L}_\alpha H \nu_{R1}$$

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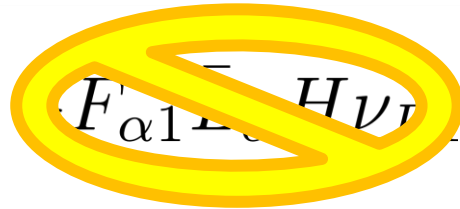


Z_2 need to be imposed

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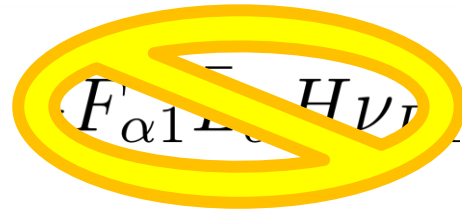
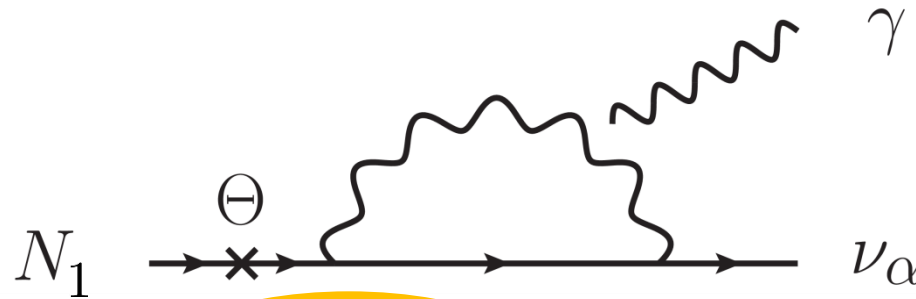
Z2 need to be imposed

$$\frac{A_{11}}{\Lambda} H^\dagger H \overline{\nu_{R1}^c} \nu_{R1} \text{ is invariant under } Z_2$$

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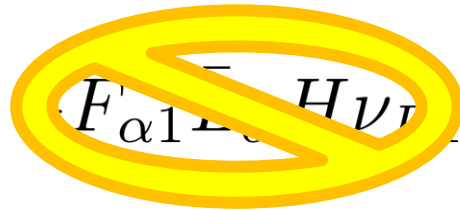
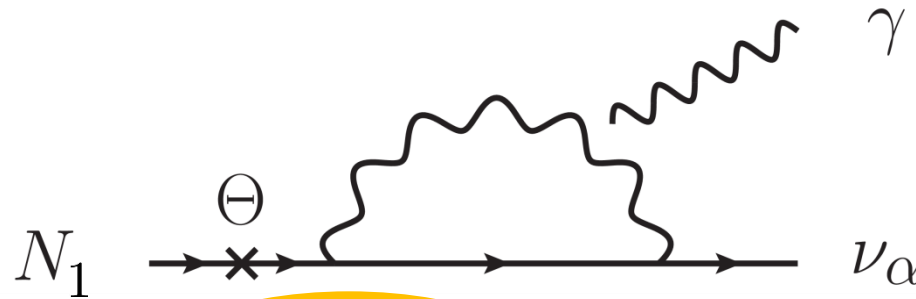


This DM production becomes important!

Higher dimensional operator effect

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Test might become difficult...

Higher dimensional operator effect

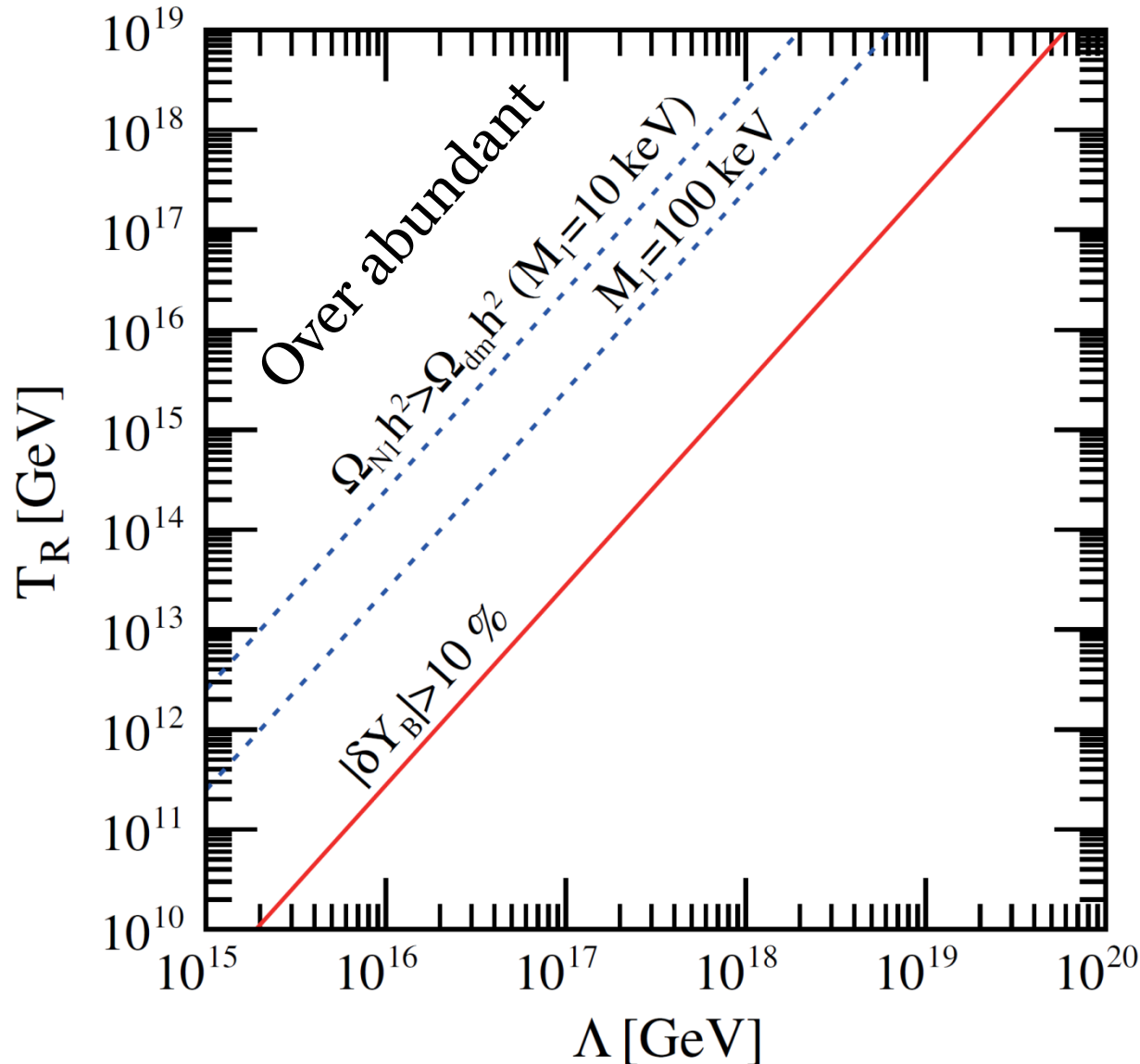
- Predicted reheating temperature

Coupling constant is assumed to be universal $A_{IJ} = 1$

Higher dimensional operator effect

- Predicted reheating temperature

Coupl



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Higher dimensional operator effect

- Implication to DM physics

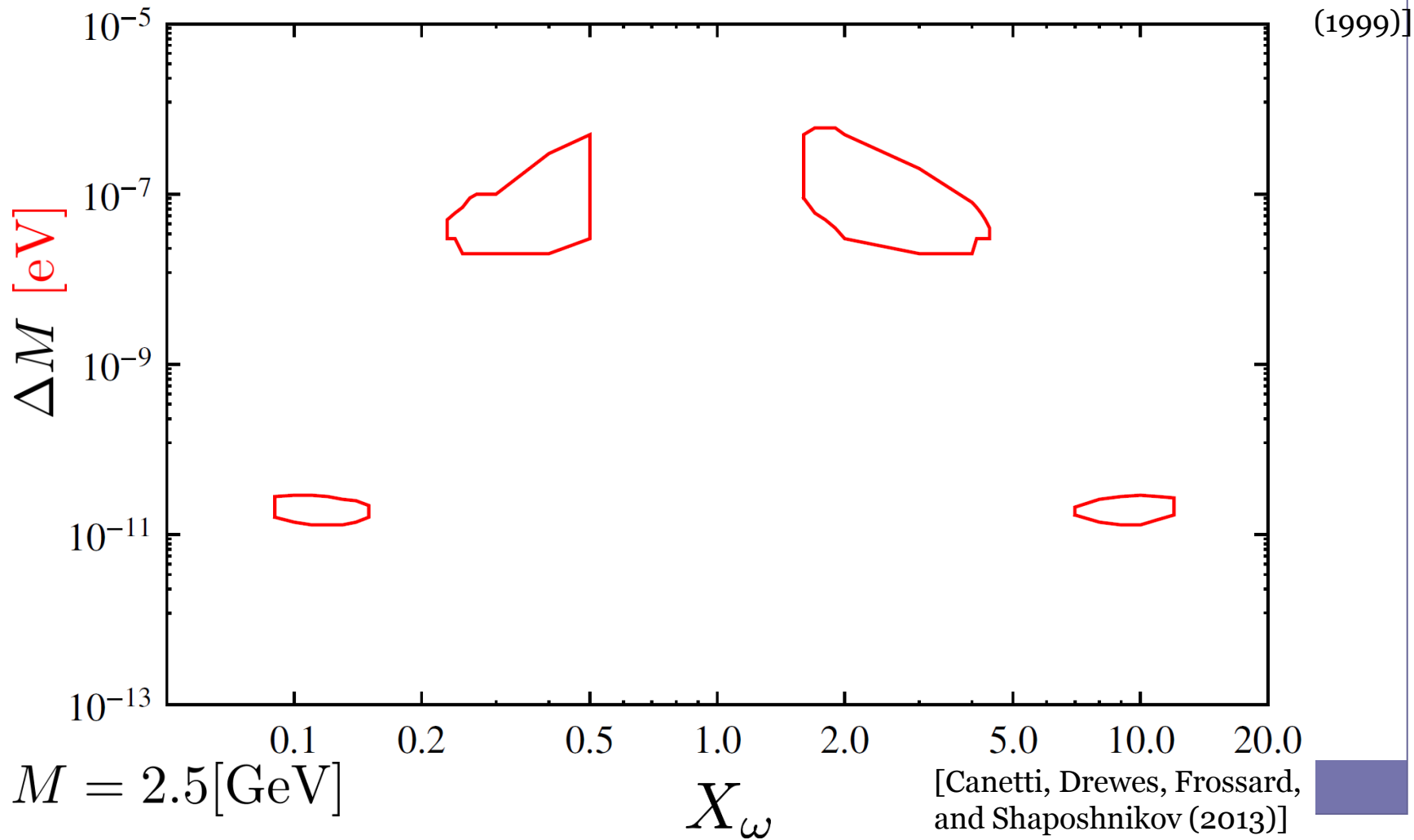
Resonant production with lepton asymmetry

[Shi and Fuller (1999)]

Higher dimensional operator effect

- Implication to DM physics

Resonant production with lepton asymmetry



Higher dimensional operator effect

- Implication to DM physics

Resonant production with lepton asymmetry

[Shi and Fuller (1999)]

Higher-dimensional operator could give significant effects on baryogenesis

 Parameter space could be changed enough!

 DM production need to be reevaluated!

Conclusions

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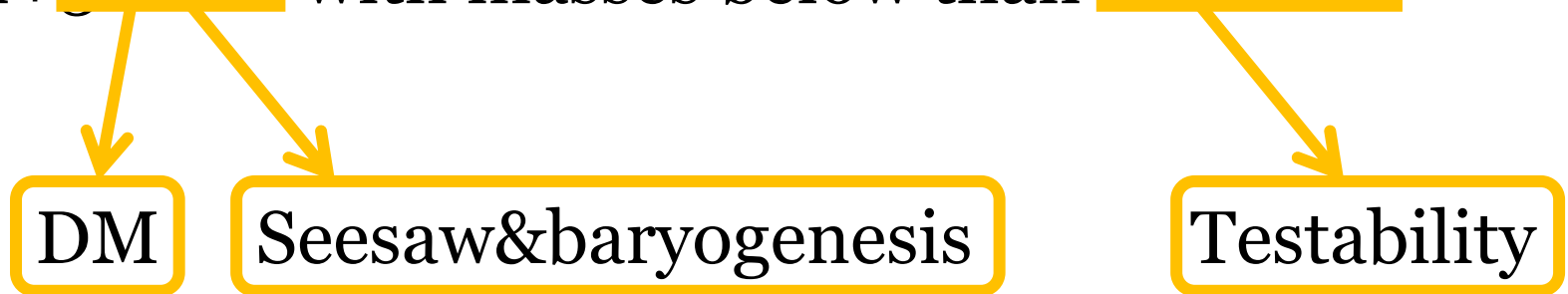
- The ν MSM

SM+3RH ν s with masses below than EW scale

Conclusions

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Conclusions

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Seesaw&baryogenesis

Testability

Simple production conflict with observation...

Conclusions

- The ν MSM

SM+3RH ν s with masses below than EW scale

DM Seesaw&baryogenesis Testability

Simple production conflict with observation...

- Impact of higher-dimensional operator on DM

HD operators could help to produce DM abundance

BAU could also be improved

- When $\Lambda \gg T_R$, HD effects become negligible

**THANK YOU
FOR YOUR ATTENTION!**





Introduction


- Testability of RHvs

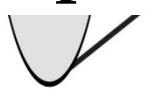
Center mass energy of LHC: 10^4 GeV



Direct production is impossible
when $M_M \sim 10^{15}$ GeV

If $M_M < M_{\text{meson}}$



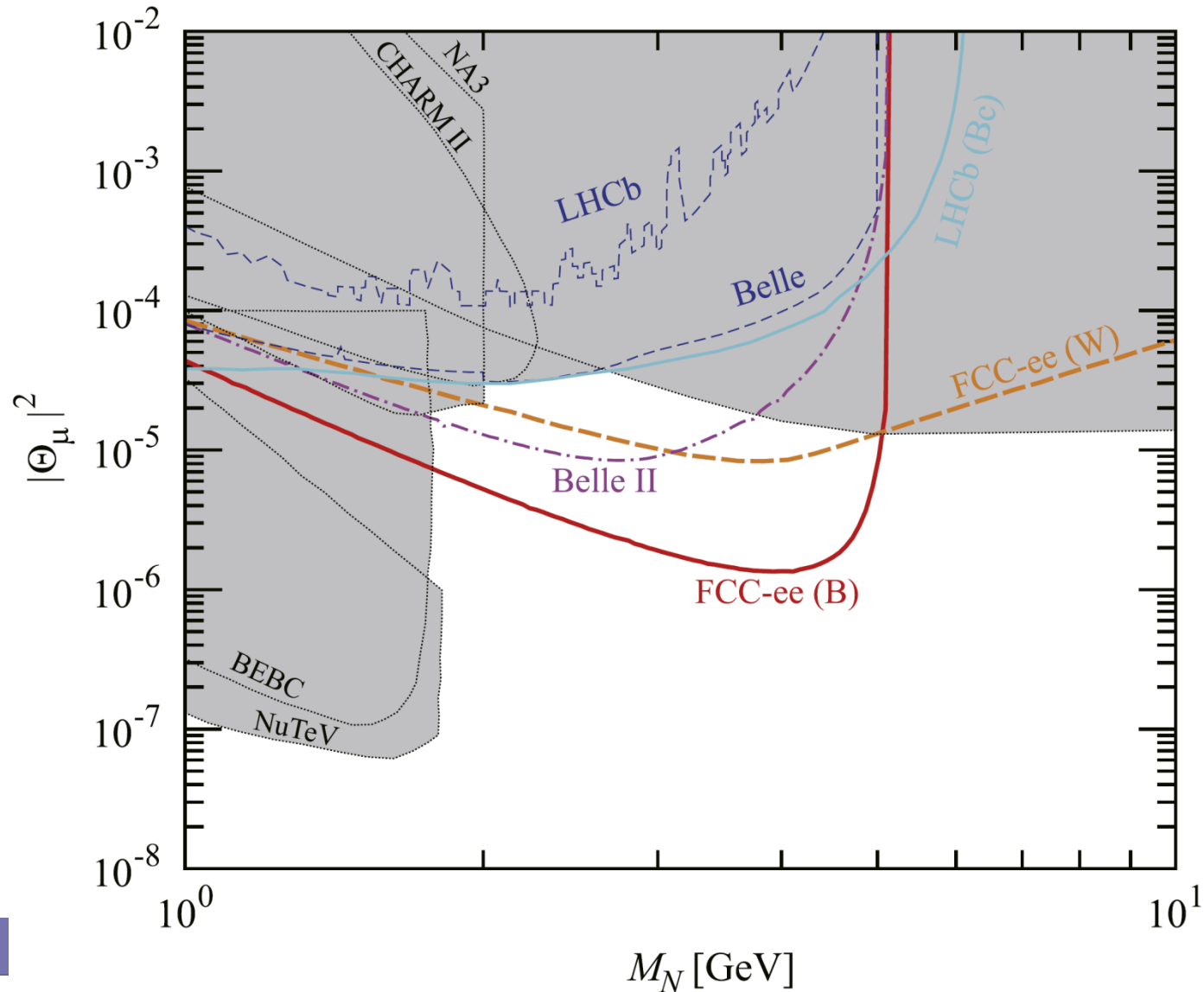
$$\Gamma_{\text{prod}}^N \simeq |\Theta|^2 \times \Gamma_{\text{weak}} \simeq \frac{M_\nu}{M_M} \times \Gamma_{\text{weak}}$$


High intensity experiments becomes very important!!

N_I

Introduction

- Testability of RHvs [Asaka and HI (2016)]



Generic form of Yukawa coupling [Casas, Ibarra(2001)]

- When 2RH ν explain the tiny ν masses by seesaw

$$F_{\alpha I} = \frac{i}{\langle H \rangle} U D_{\nu}^{\frac{1}{2}} \Omega D_N^{\frac{1}{2}} \quad (M_N = 3 \text{ GeV})$$

$$* D_N^{\frac{1}{2}} = \text{diag} \left(\sqrt{M_2}, \sqrt{M_3} \right) \equiv \left(\sqrt{M_N - \Delta M/2}, \sqrt{M_N + \Delta M/2} \right)$$

$$* D_{\nu}^{\frac{1}{2}} = \text{diag} \left(\sqrt{m_1}, \sqrt{m_2}, \sqrt{m_3} \right)$$

$$* U = \begin{pmatrix} c_{13}c_{12} & c_{13}s_{12} & s_{13}e^{-i\delta} \\ -c_{23}s_{12}-s_{23}s_{13}c_{12}e^{i\delta} & c_{23}c_{12}-s_{23}s_{13}s_{12}e^{i\delta} & s_{13}c_{13} \\ s_{23}s_{12}-c_{23}s_{13}c_{12}e^{i\delta} & -s_{23}c_{12}-c_{23}s_{13}s_{12}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} 1 & & \\ & e^{i\eta} & \\ & & 1 \end{pmatrix}$$

$$* \Omega = \begin{pmatrix} 0 & 0 \\ \cos \omega & -\sin \omega \\ \xi \sin \omega & \xi \cos \omega \end{pmatrix} \text{ for N.H.} \quad \Omega = \begin{pmatrix} \cos \omega & -\sin \omega \\ \xi \sin \omega & \xi \cos \omega \\ 0 & 0 \end{pmatrix} \text{ for I.H.}$$

ω is arbitrary complex $\xi = \pm 1$

Generic form of Yukawa coupling [Casas, Ibarra(2001)]

• Feature of matrix Ω

$$\Omega = \begin{pmatrix} 0 & 0 \\ \cos \omega & -\sin \omega \\ \xi \sin \omega & \xi \cos \omega \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & \cos \operatorname{Re} \omega & -\sin \operatorname{Re} \omega \\ 0 & \xi \sin \operatorname{Re} \omega & \xi \cos \operatorname{Re} \omega \end{pmatrix} \begin{pmatrix} 0 & 0 \\ \cosh \operatorname{Im} \omega & -i \sinh \operatorname{Im} \omega \\ i \sinh \operatorname{Im} \omega & \cosh \operatorname{Im} \omega \end{pmatrix}$$



Imaginary part can determine
the magnitude of Yukawa coupling

$$\begin{aligned} \text{Because, } \sinh \operatorname{Im} \omega &= \frac{1}{2} (\exp [\operatorname{Im} \omega] - \exp [-\operatorname{Im} \omega]) \\ \cosh \operatorname{Im} \omega &= \frac{1}{2} (\exp [\operatorname{Im} \omega] + \exp [-\operatorname{Im} \omega]) \end{aligned}$$

Hereafter, $\exp [\operatorname{Im} \omega] \equiv X_\omega$

The ν MSM [Asaka, Blanchet, and Shaposhnikov (2005)] [Asaka and Shaposhnikov (2005)]

- Baryogenesis via neutrino oscillation

Sakharov's criteria

Baryon number
violation

B+L violation by anomaly

$(T \gtrsim 100\text{GeV})$ [Kuzmin, Rubakov and Shaposhnikov (1969)]

C and CP
violation

Complex phase in the CKM matrix
as well as in the PMNS matrix.

[Maki, Nakagawa and Sakata (1962) ; Pontecorvo (1967)]

Departure from
thermal
equilibrium

RH ν s are departure from thermal
equilibrium from the beginning

$$F \sim 4 \times 10^{-8} \left(\frac{M_N}{\text{GeV}} \right)^{1/2} \left(\frac{\sqrt{\Delta m_{\text{atm}}^2}}{2.5 \times 10^{-3} \text{eV}} \right)^{1/4}$$

All of the criteria can be satisfied in the ν MSM!

The ν MSM [Asaka, Blanchet, and Shaposhnikov (2005)]

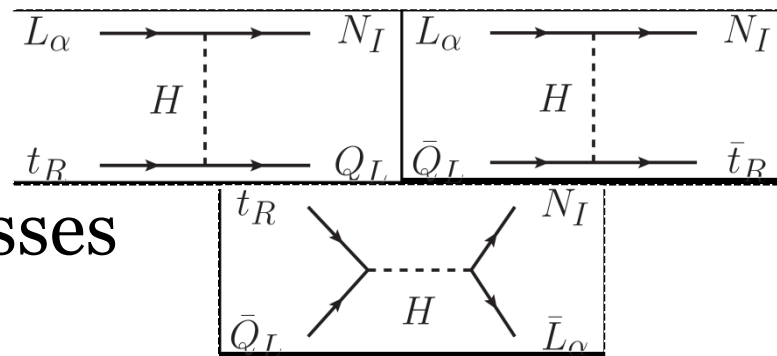
• Baryogenesis via neutrino oscillation

[Akhmedov, Rubakov, and Smirnov ('98)]

[Asaka and Shaposhnikov (2005)]

Initial condition : **No $RH\nu$**

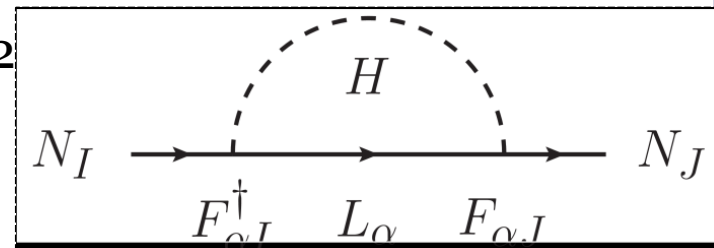
Produced by scattering processes



Depart from thermal equilibrium

$RH\nu$ s start to oscillate at T_L @ F^2

$$V_N = \frac{T}{8} [F^\dagger F]_{IJ}$$



Typical temperature to oscillate

$$T_L = 320 \text{ GeV} \left(\frac{M_N}{3 \text{ GeV}} \right)^{2/3} \left(\frac{\Delta M^2 / M_N^2}{10^{-10}} \right)^{1/3}$$

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Through oscillation, CPV occurs via Yukawa couplings

$$A_{32}^{\alpha} = \text{Im} \left[F_{\alpha I} \left[F^{\dagger} F \right]_{IJ} F_{\alpha J}^{\dagger} \right] \neq 0 .$$

Asymmetries are stored in each active flavor

however, $\sum_{\alpha} A_{32}^{\alpha} = 0$



No net asymmetry in the end @F⁴ order

Asymmetry is produced @F⁶ order effects

The ν MSM [Asaka, Blanchet, and Shaposhnikov (2005)] [Asaka and Shaposhnikov (2005)]

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Important fact : total lepton number is conserved



Lepton number separation

$$\Delta L_{\text{tot}} = \sum_{\alpha} \Delta L_{\alpha} + \sum_I \Delta N_I = 0,$$



$$\sum_{\alpha} \Delta L_{\alpha} = - \sum_I \Delta N_I \neq 0.$$

$$\Delta N_I \neq 0$$

$$\Delta L_{\alpha} \neq 0$$

Baryon number is produced through sphaleron

$$\Delta B = -\frac{28}{79} \sum_{\alpha} \Delta L_{\alpha} \quad \begin{array}{l} \text{[Khlebnikov; Shaposhnikov(1988)]} \\ \text{[Harvey; Turner(1990)]} \end{array}$$

The νMSM [Asaka, Blanchet, and Shaposhnikov (2005)] [Asaka and Shaposhnikov (2005)]

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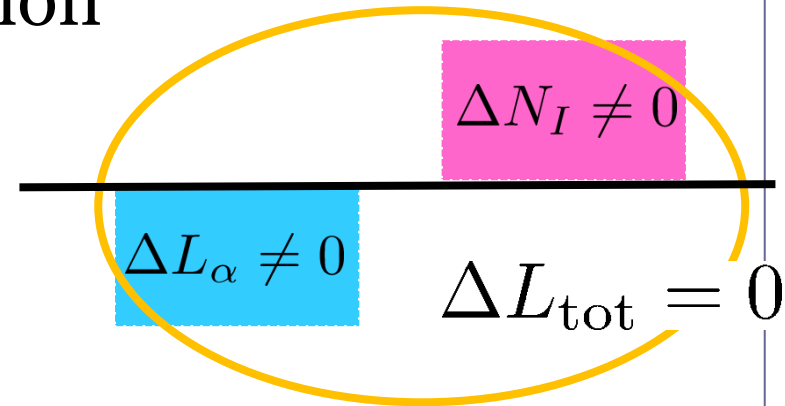
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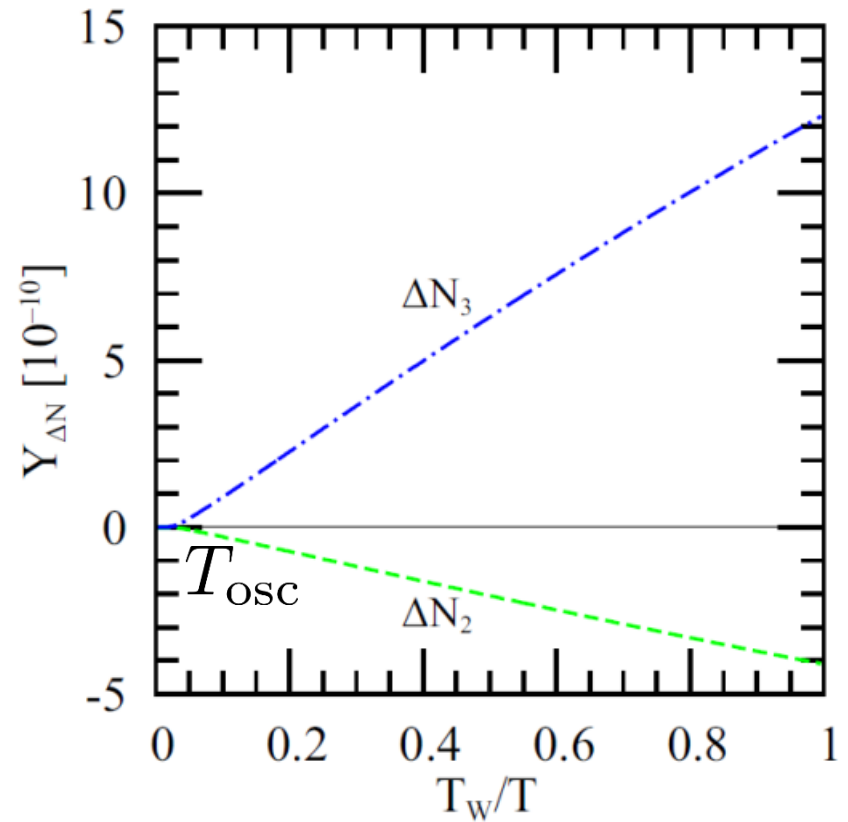
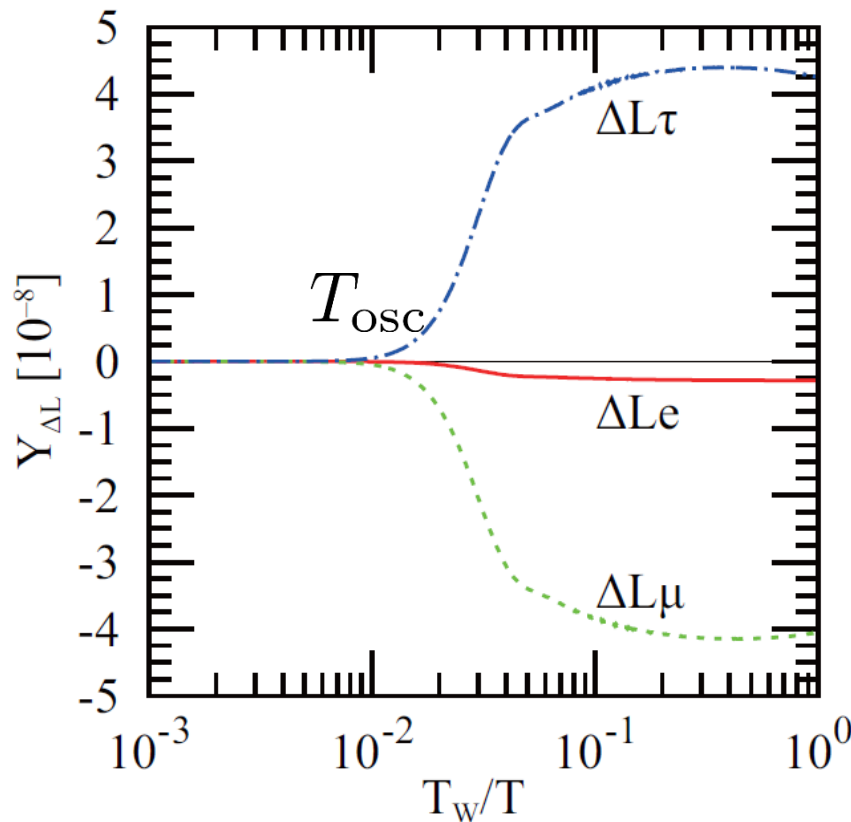
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Evolution of asymmetries(Each flavor)



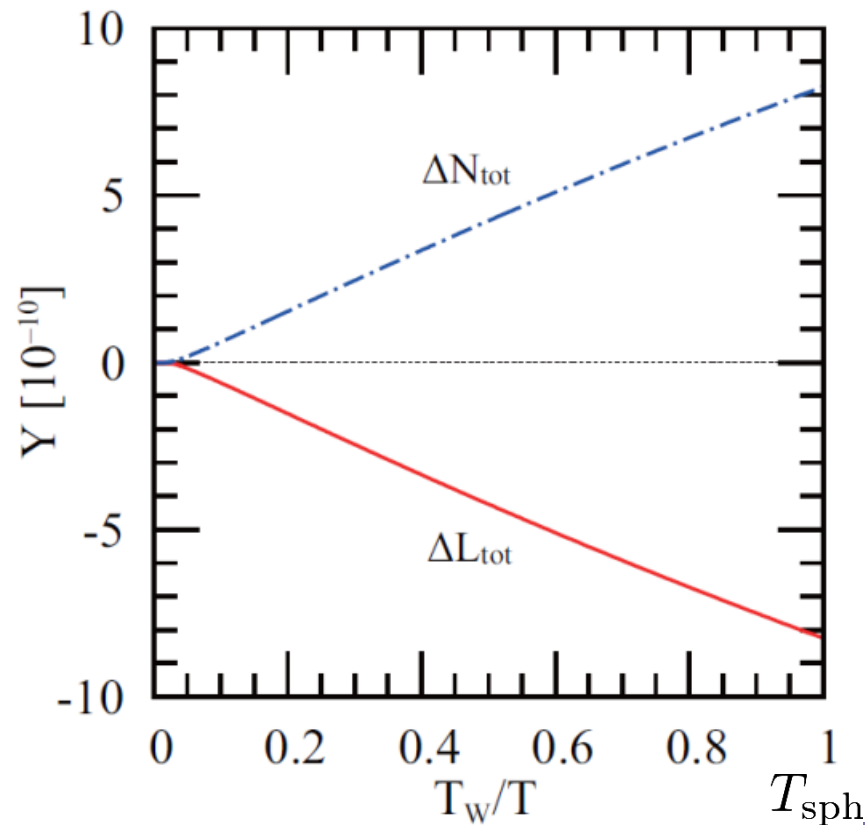
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Evolution of asymmetries(Total)



The ν MSM [Asaka, Blanchet, and Shaposhnikov (2005)] [Asaka and Shaposhnikov (2005)]

- Kinetic equations point of view [Asaka, Eijima, and HI (2012)]

$$\frac{d\rho_N(k_N)}{dt} = -i [H_N^0 + V_N, \rho_N] - \frac{1}{2} \{ \Gamma_N^d, \rho_N \} \\ - \frac{1}{2} \{ \Gamma_N^p, \mathbf{1} - \rho_N \} \left(\rho_N = \begin{pmatrix} [\rho_N]_{22} & [\rho_N]_{23} \\ [\rho_N]_{32} & [\rho_N]_{33} \end{pmatrix} \right)$$

Usual initial condition : $\rho_N^I = 0$



Question : Is there really NO other source than the scatterings?

Previous work : [Bezrukov, Gorbunov, and Shaposhnikov

Higgs-driven inflation are low energy phenomena, having nothing to do with inflation. We study then a modification of the ν MSM, adding to its Lagrangian higher dimensional operators suppressed by the Planck scale. The role of these operators in Higgs-driven inflation is clarified. We find that these operators do not contribute to the production of *Warm Dark Matter* (WDM) and to baryogenesis. We also demonstrate that the sterile neutrino with

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Higher dimensional operator effect

- Effects on the baryogenesis

$$\delta Y_B \equiv \frac{Y_B|_{[\rho_N]_{IJ}^I \neq 0} - Y_B|_{[\rho_N]_{IJ}^I = 0}}{Y_B|_{[\rho_N]_{IJ}^I = 0}}$$

- Oscillation temperature

$$T_L = 320 \text{ GeV} \left(\frac{M_N}{3 \text{ GeV}} \right)^{2/3} \left(\frac{\Delta M^2 / M_N^2}{10^{-10}} \right)^{1/3}$$

- ΔM  -Oscillation temperature 

$T_L \simeq T_{\text{sph}}$ is given $\Delta M \simeq 10^{-10} \text{ GeV}$

Higher dimensional operator effect

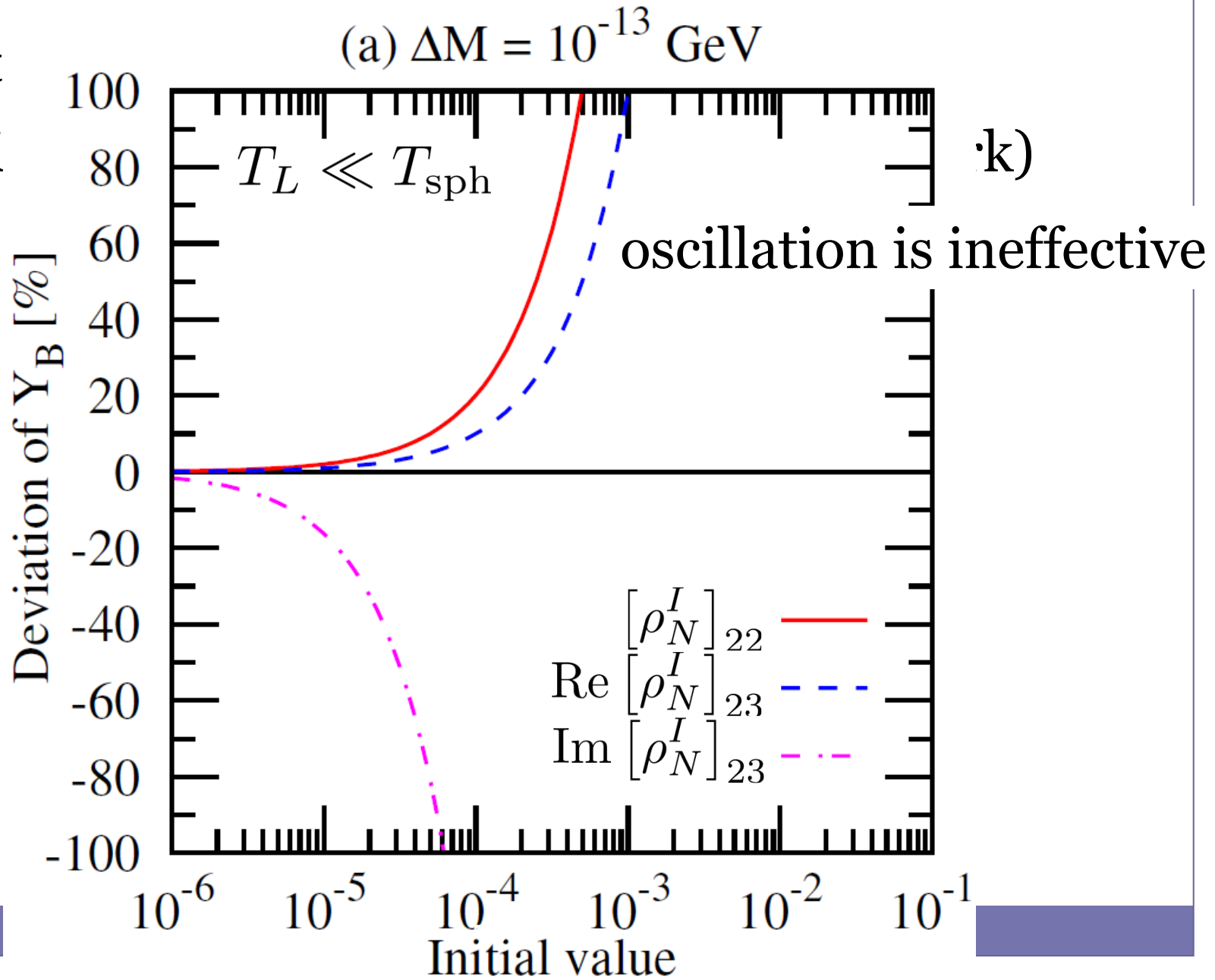
- Effects on the baryogenesis

We fix $X_\omega = 1$ (washout effect does not work)

Higher dimensional operator effect

• Effect

We find

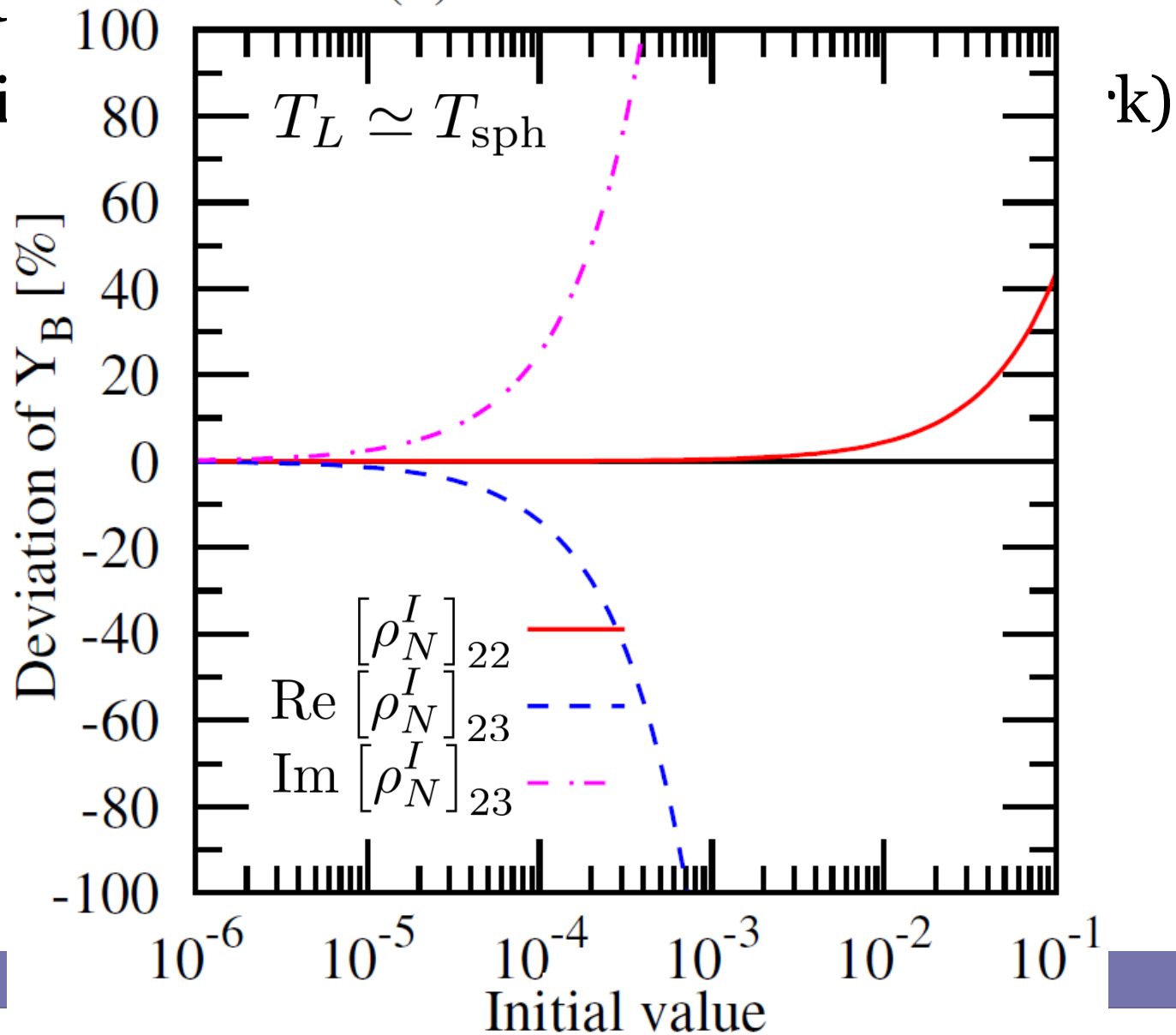


Higher dimensional operator effect

• Effect

We find

(b) $\Delta M = 10^{-10}$ GeV

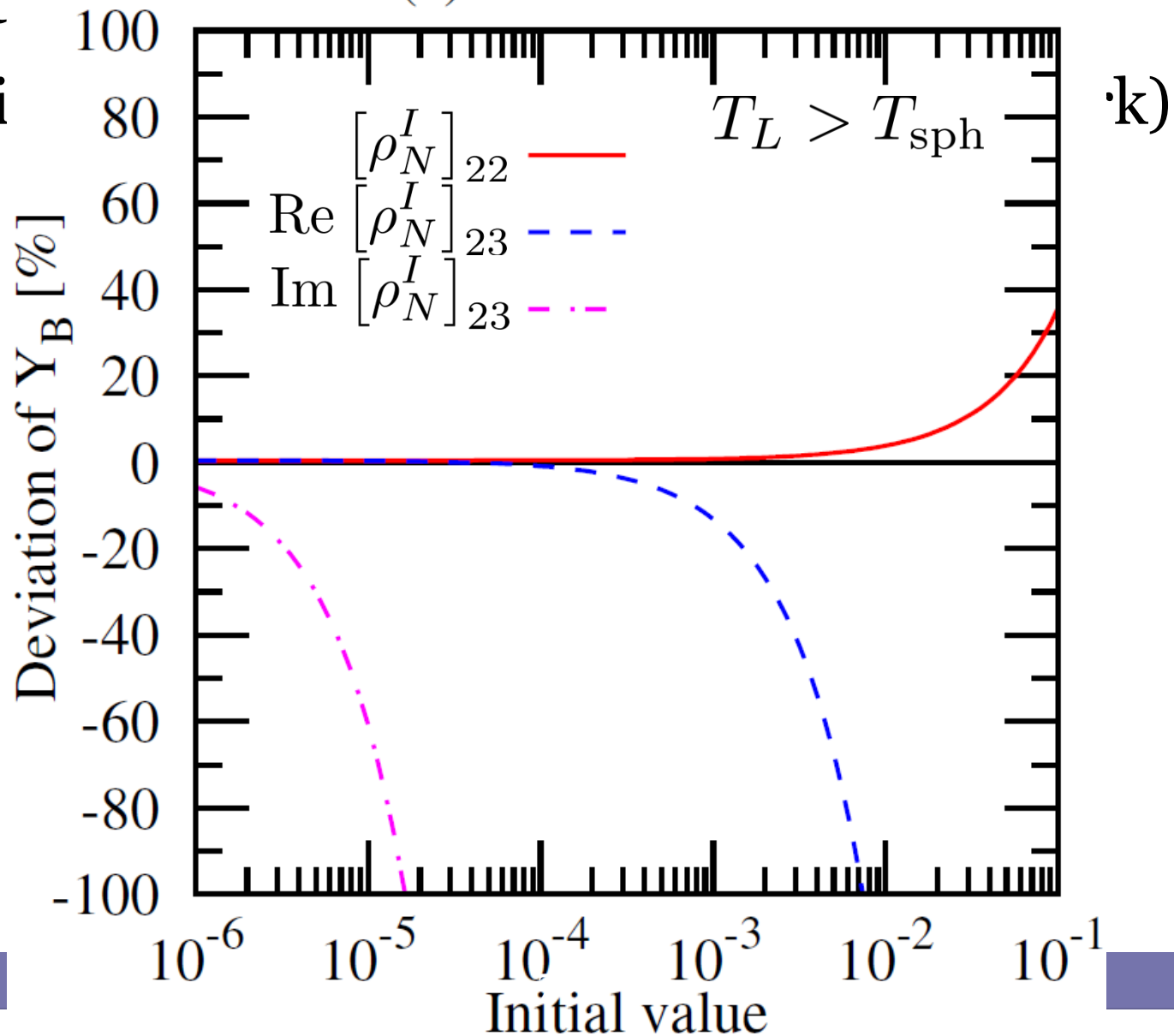


Higher dimensional operator effect

• Effect

We fi

(c) $\Delta M = 10^{-7}$ GeV



Higher dimensional operator effect

- Effects on the baryogenesis : summary

Imaginary part of off-diagonal element is important!

Higher dimensional operator effect

- Effects on the baryogenesis : summary

Imaginary part of off-diagonal element is important!



to create asymmetry



to enhance oscillation

Higher dimensional operator effect

- Effects on the baryogenesis : summary

Imaginary part of off-diagonal element is important!

to create asymmetry

to enhance oscillation

- Only if $\Delta M \ll 10^{-10} \text{ GeV}$ ($T_L \ll T_{\text{sph}}$)

Diagonal element also becomes significant!

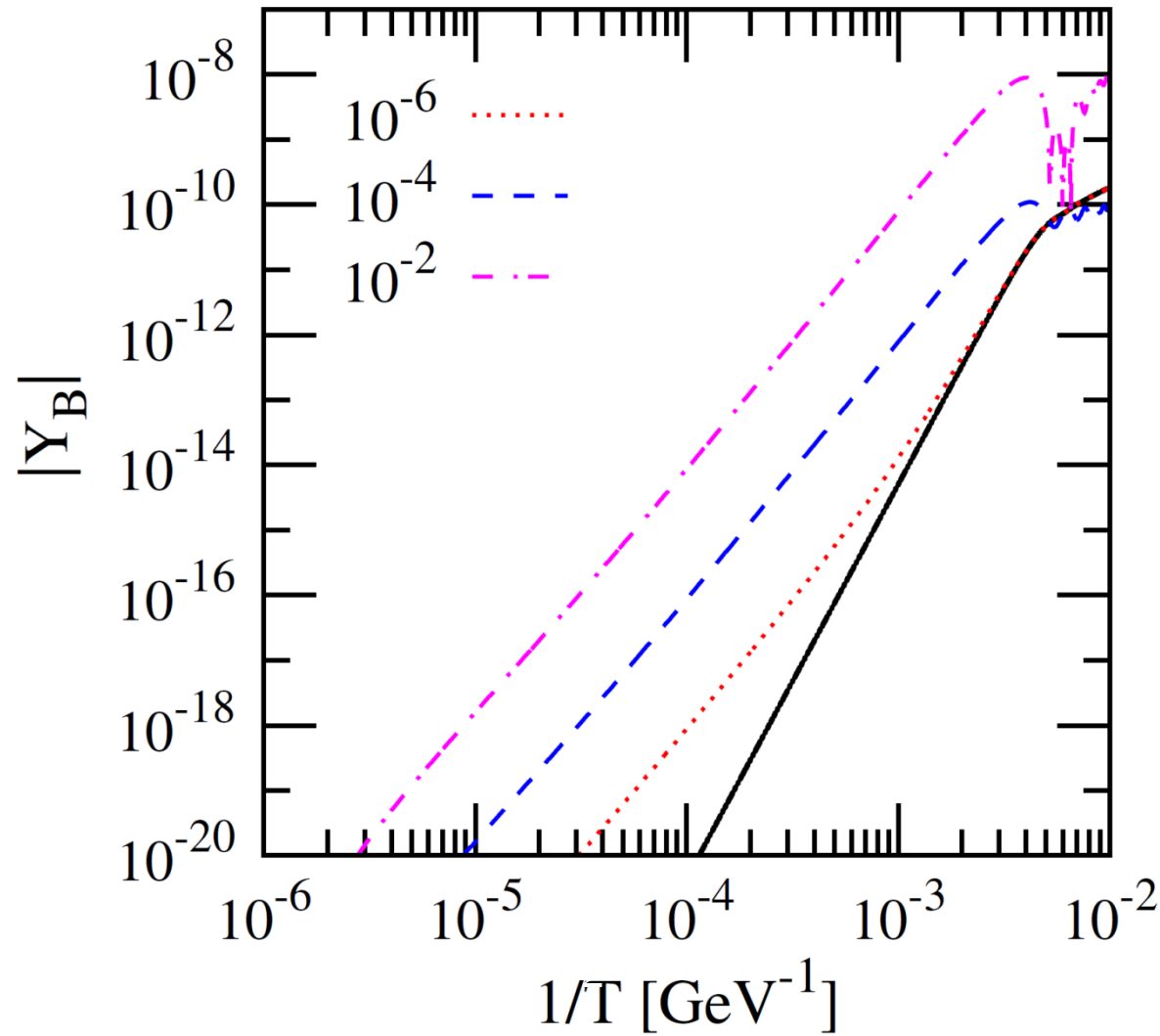
- Even if $\text{Im} [\rho_N^I]_{23} = 10^{-5}$ ($T_R \sim 10^{13} \text{ GeV}$)

Y_B can be changed  New discovery!!

Higher dimensional operator effect

- Detail evolution of Y_B ($\Delta M = 10^{-10} \text{ GeV}$, $X_\omega = 1$)

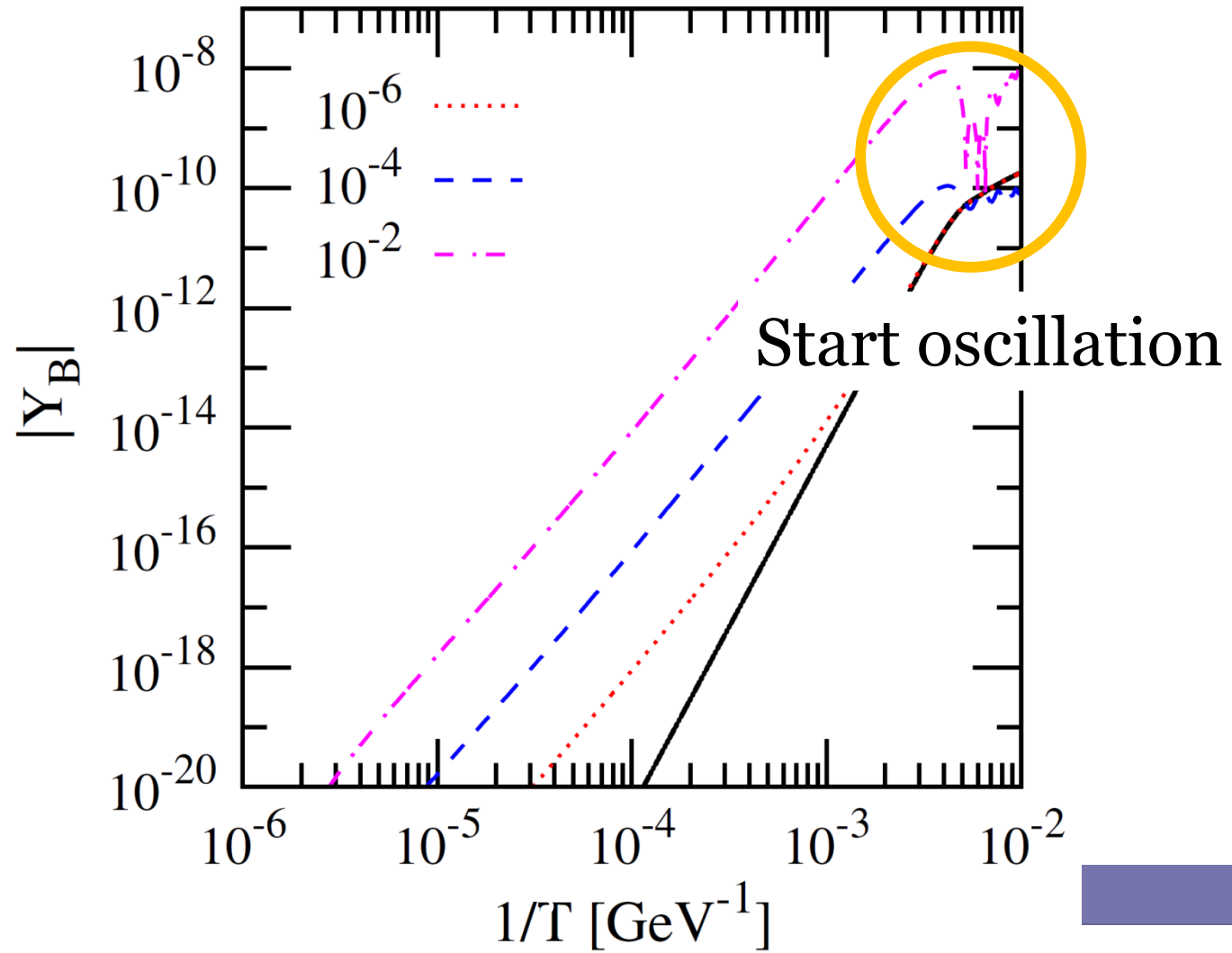
(d) $\text{Im}[r_N]_{23}^I$



Higher dimensional operator effect

- Detail evolution of Y_B ($\Delta M = 10^{-10} \text{ GeV}$, $X_\omega = 1$)

(d) $\text{Im}[r_N]_{23}^I$



Higher dimensional operator effect

- Impact of $\text{Im} [\rho_N^I]_{23}$

Off-diagonal element is unique source of CPV

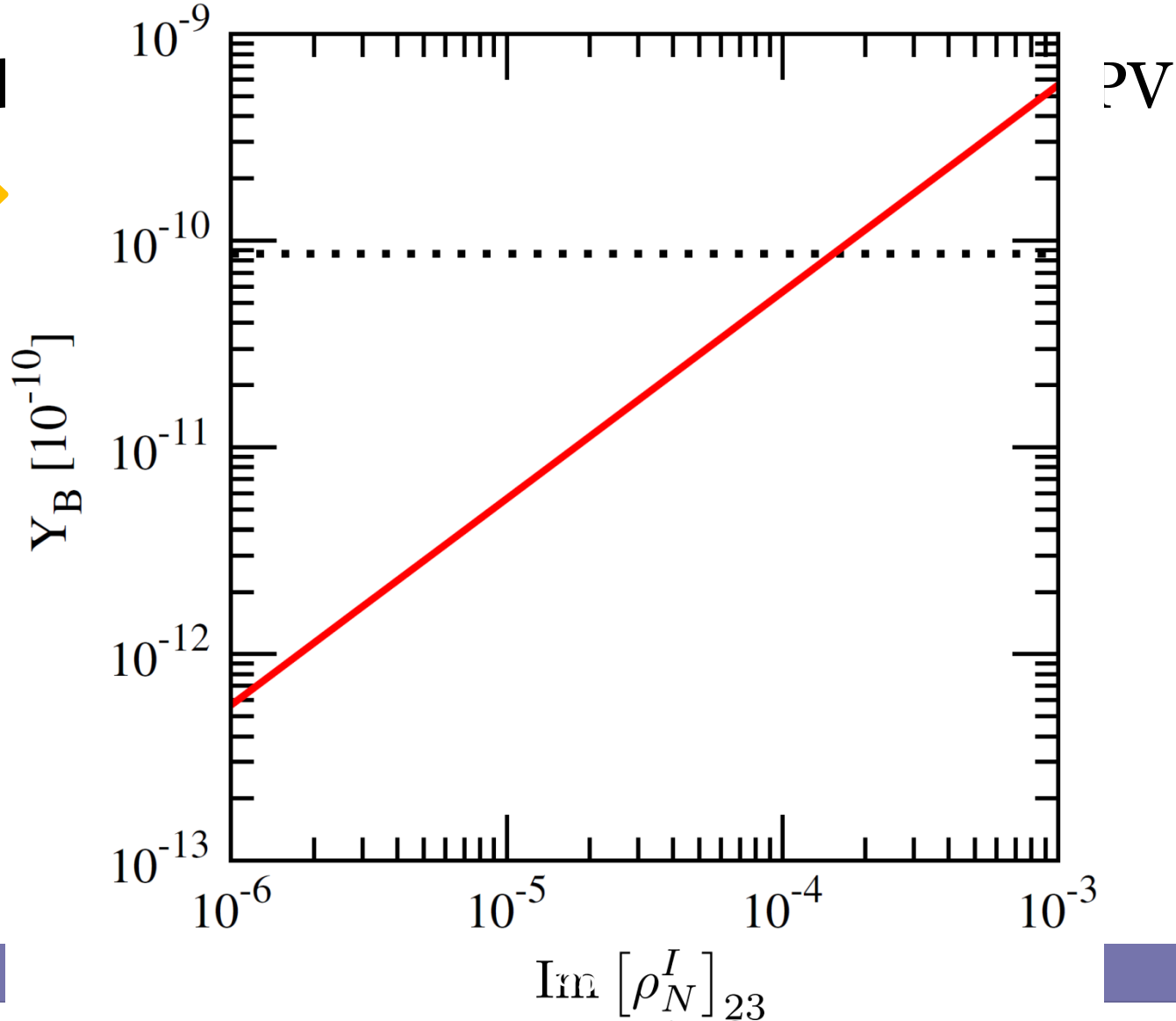


$$\delta = \eta = \text{Im}\omega = 0$$

Higher dimensional operator effect

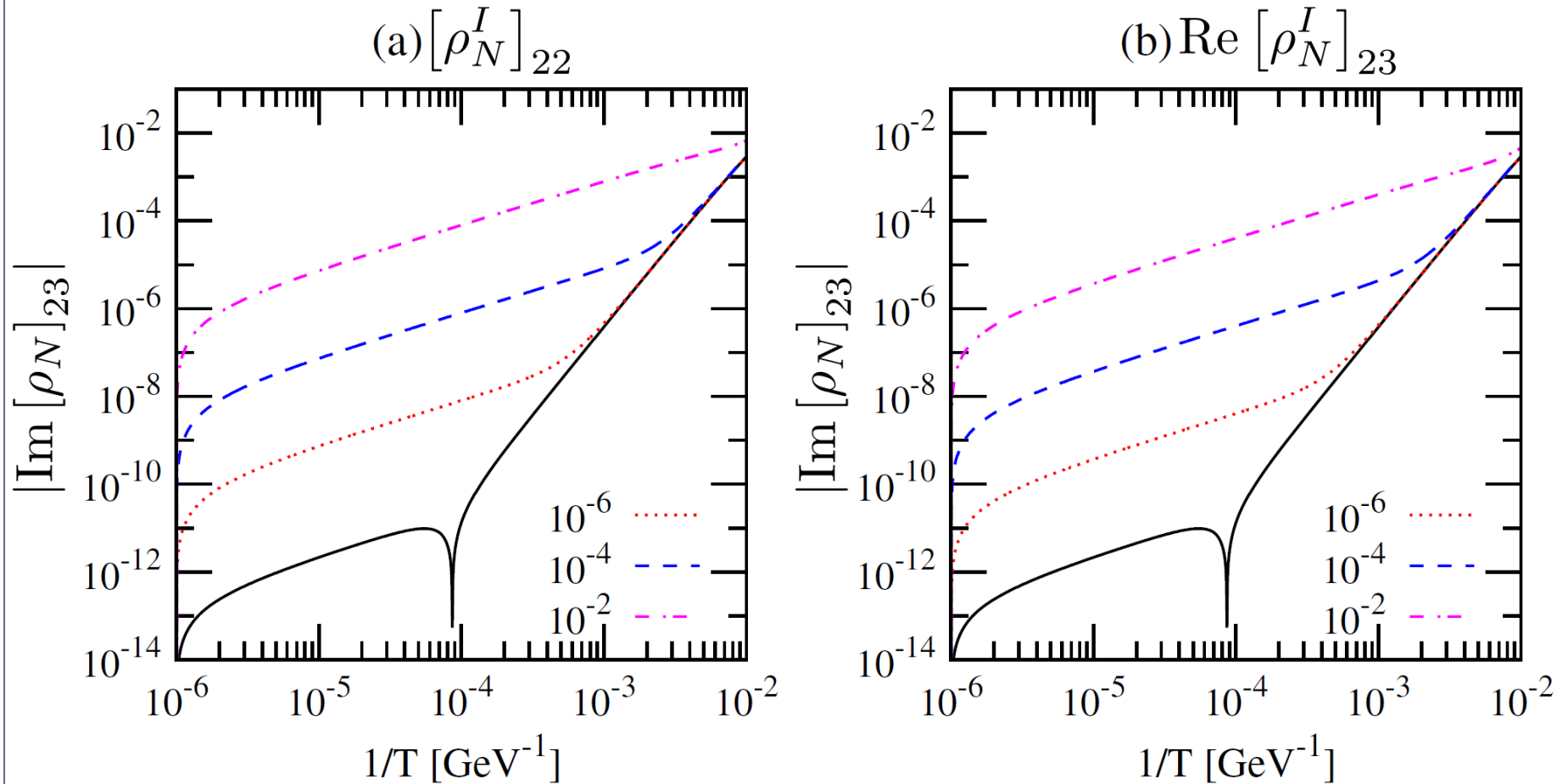
- Impact of $\text{Im} [\rho_N^I]_{33}$

Off-d



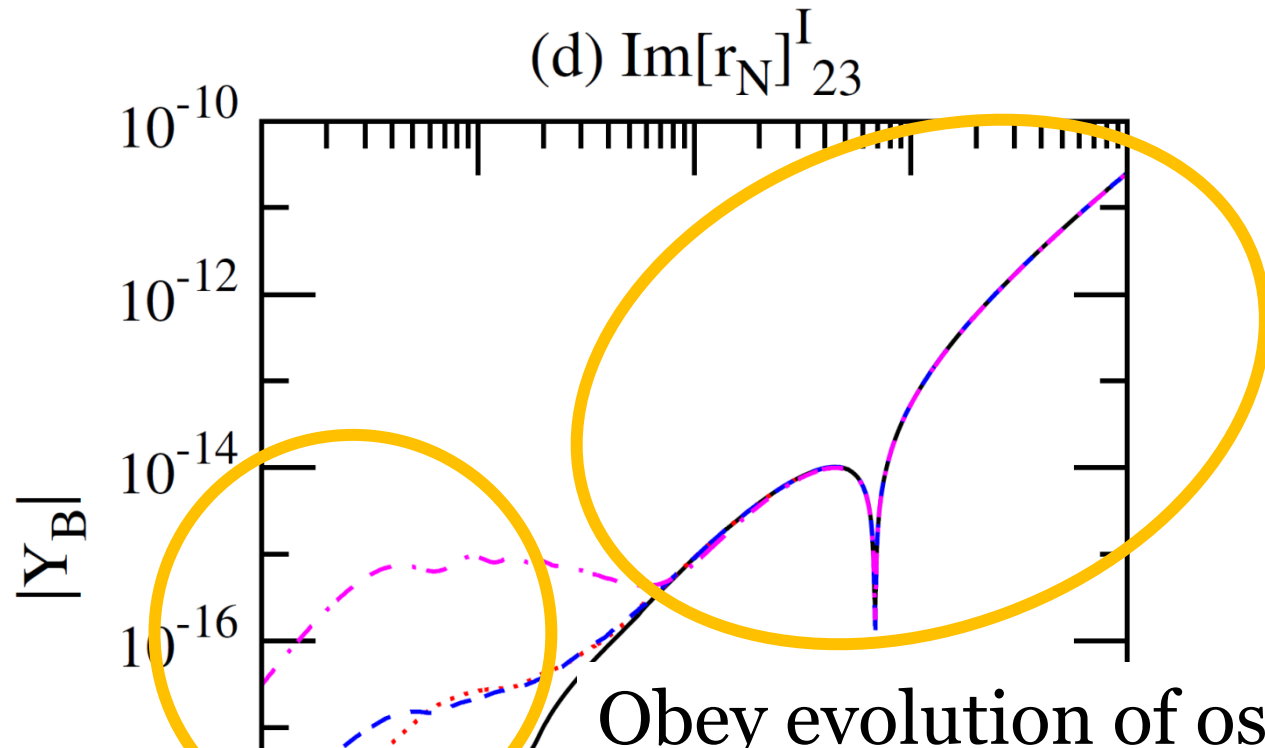
Higher dimensional operator effect

- Detail evolution of $\text{Im} [\rho_N]_{23}$

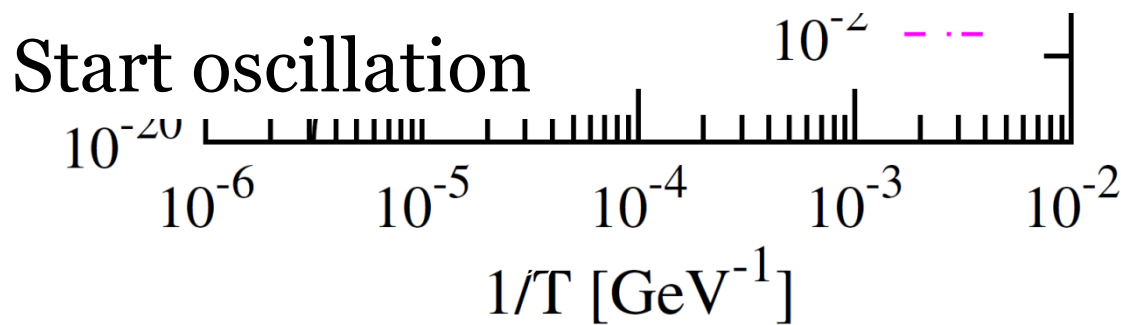


Higher dimensional operator effect

- Detail evolution of Y_B ($\Delta M = 10^{-10} \text{ GeV}$, $X_\omega \gg 1$)

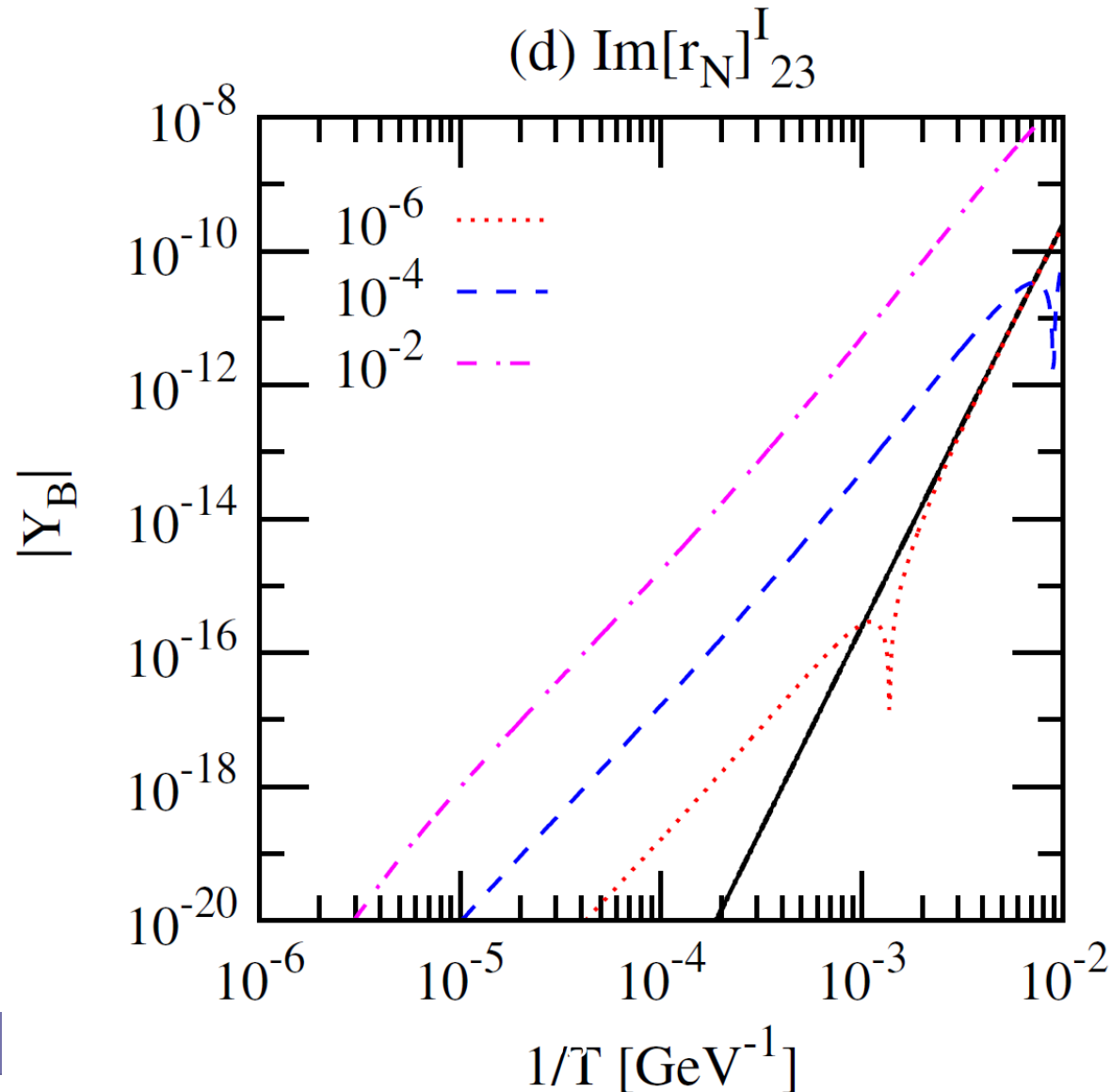


Information of initial condition is lost



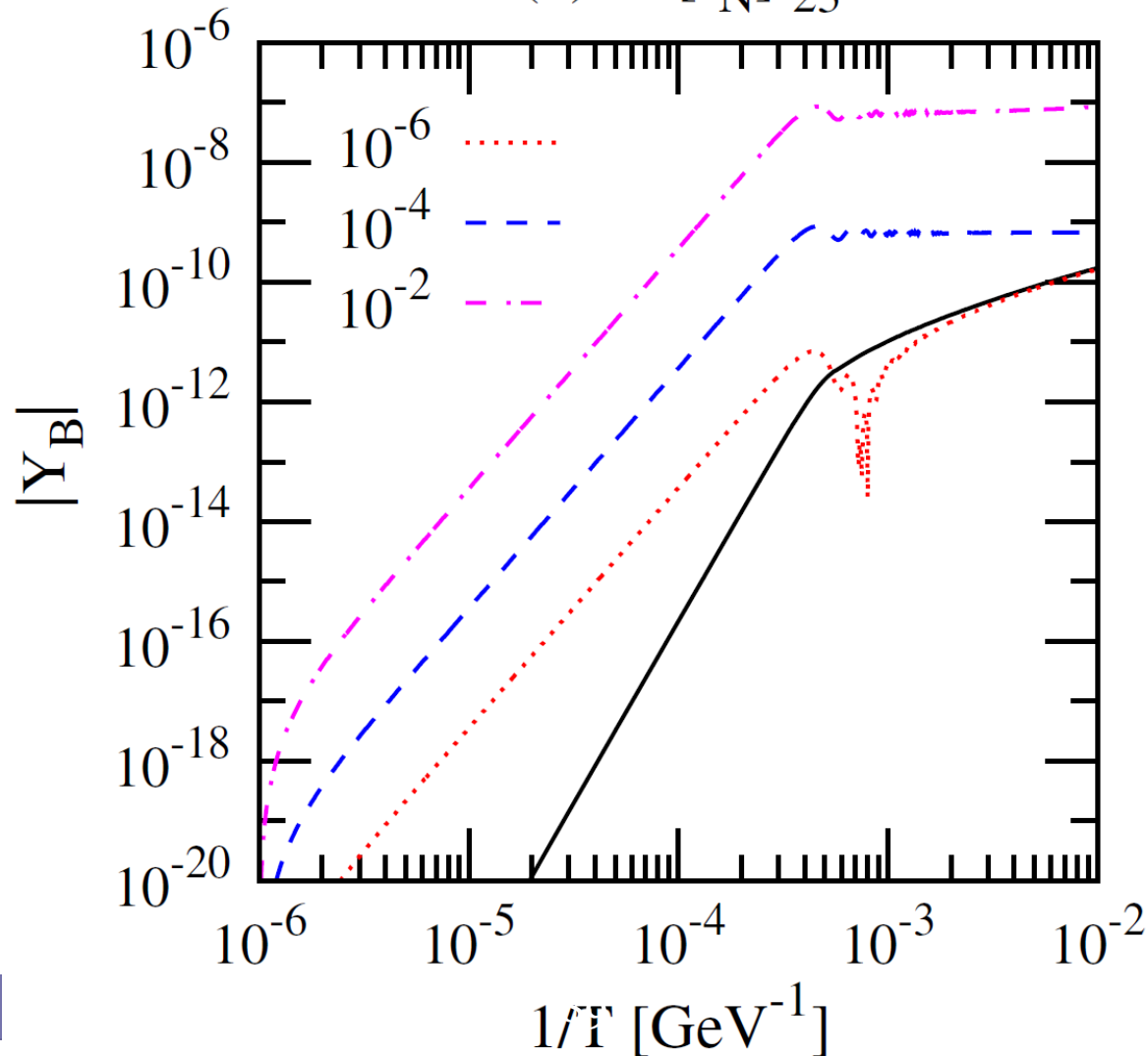
Higher dimensional operator effect

- Detail evolution of Y_B ($\Delta M = 10^{-13}\text{GeV}$, $X_\omega = 1$)



Higher dimensional operator effect

- Detail evolution of Y_B ($\Delta M = 10^{-7} \text{ GeV}$, $X_\omega = 1$)
(d) $\text{Im}[r_N]_{23}^I$



Conclusions

- Future works

- Including LNV processes [Eijima and Shaposhnikov (2017)]
[Chiglieri and Laine (2017)]

- Including CPV Higgs decay processes [Hambye and Tresi (2017)]

When Yukawa is big enough ($X_\omega \gg 1$),
these effects take place

- Detail analysis of indirect effect on DM production