

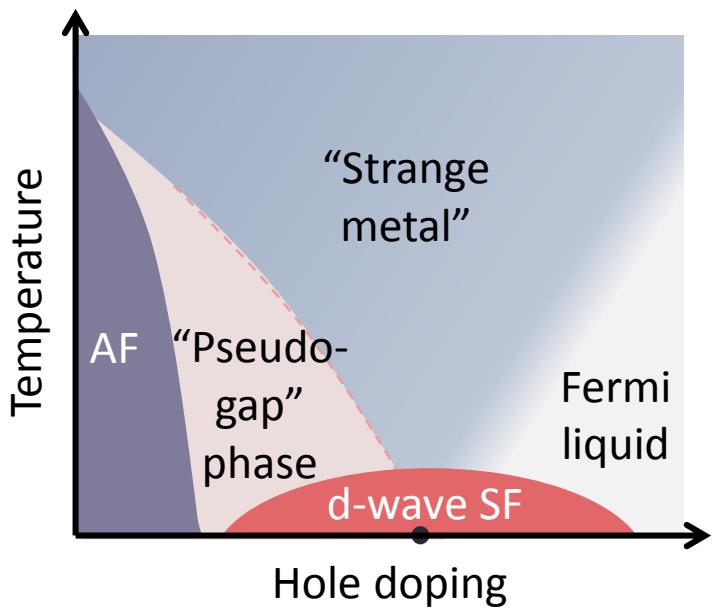
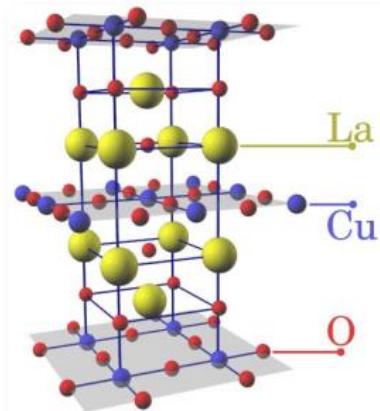
# Antiferromagnetic long-range order in the Fermi-Hubbard model with ultracold atoms



Christie Chiu  
Markus Greiner, Harvard University

# Fermions in optical lattices

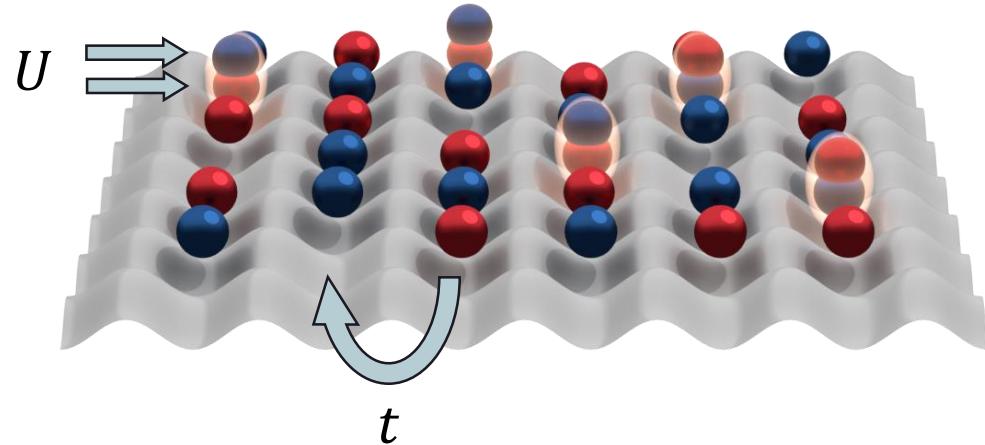
High  $T_c$  superconductivity



Fermi-Hubbard model

P.W. Anderson:  
minimal model for cuprate superconductors

$$\hat{H} = \underbrace{-t \sum_{\langle i,j \rangle, \sigma} \left( c_{i,\sigma}^\dagger c_{j,\sigma} + \text{H.c.} \right)}_{\text{tunneling}} + \underbrace{U \sum_i \hat{n}_{i\uparrow} \hat{n}_{i\downarrow}}_{\text{On-site interaction}}$$



# Fermions in optical lattices

## High T<sub>C</sub> superconductivity



Cold atom proposal: 2002

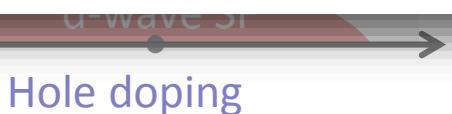
W. Hofstetter, J. I. Cirac, P. Zoller, E. Demler,  
and M. D. Lukin PRL 89, 220407



Fermi-Hubbard with cold atoms: 2008  
Essligner, Bloch, Hulet, Takahashi, ...

- R. Jördens, et.al., Nature 455, 204 (2008)
- U. Schneider, et al., Science 322, 1520 (2008)
- S. Taie, et al., Nature Physics 8, 825 (2012)
- T. Uehlinger, et al., PRL 111, 185307 (2013)
- M. Messer, et al., PRL 115, 115303 (2015)
- P. M. Duarte, et al., PRL 114, 070403 (2015)
- C. Hofrichter, et al., PRX 6 021030 (2016)

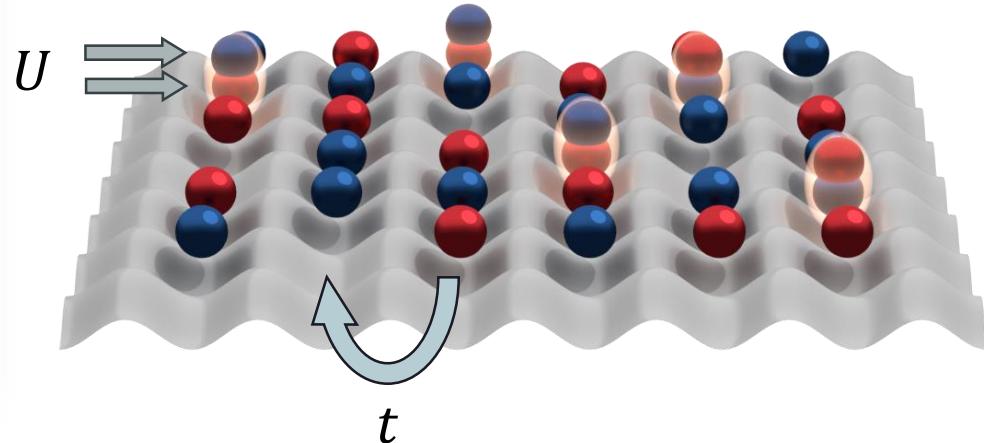
....



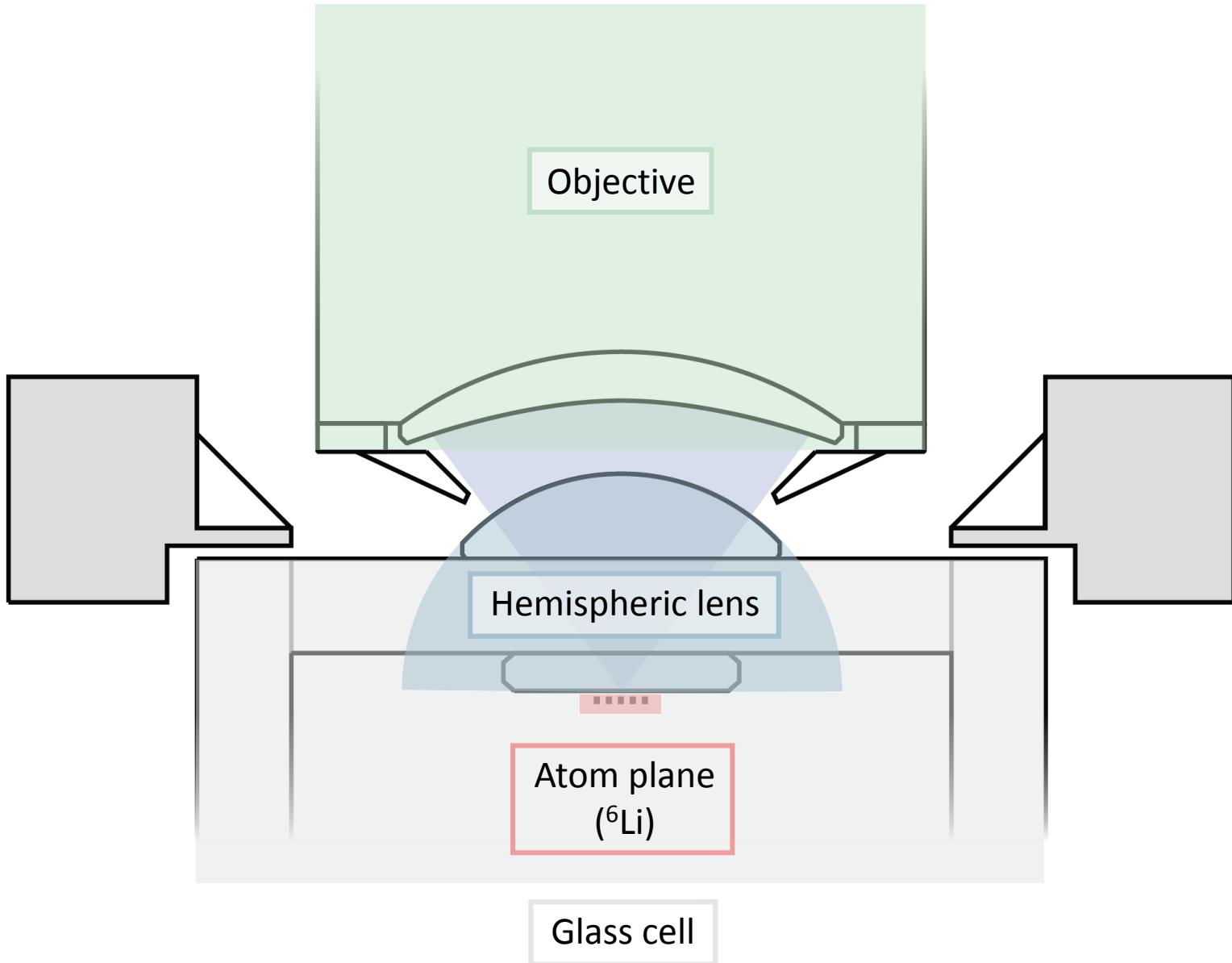
## Fermi-Hubbard model

P.W. Anderson:  
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$$\hat{H} = \underbrace{-t \sum_{\langle i,j \rangle, \sigma} \left( c_{i,\sigma}^\dagger c_{j,\sigma} + \text{H.c.} \right)}_{\text{tunneling}} + \underbrace{U \sum_i \hat{n}_{i\uparrow} \hat{n}_{i\downarrow}}_{\text{On-site interaction}}$$

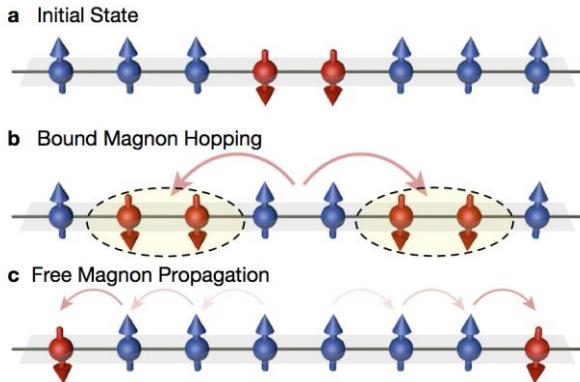


# Quantum gas microscopy



# Quantum gas microscopy

## Detection



## Out of equilibrium

Hole propagation

Correlation propagation

Spin waves

M. Cheneau, *et al.*, *Nature* 481, 484 (2012)

T. Fukuhara, *et al.*, *Nature Phys.* 9, 235 (2013)

T. Fukuhara, *et al.*, *Nature* 502, 76 (2013)

S. Hild, *et al.*, *PRL* 113, 147205 (2014)

P. Preiss, *et al.*, *Science* 347, 1229 (2015)

A. Kaufman, *et al.*, *Science* 353, 794 (2016)

## Novel probing tools

Local observables

Spin/Density correlator

Full information

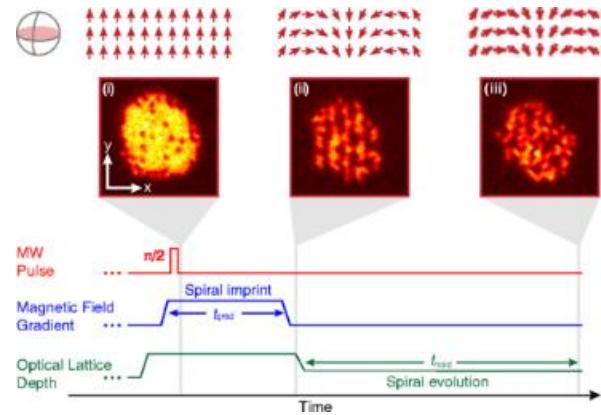
M. Endres, *et al.*, *Nature* 487, 454 (2012)

R. Islam, *et al.*, *Nature* 528, 77 (2015)

P. Preiss, *et al.*, *PRA* 91, 041602 (2015)

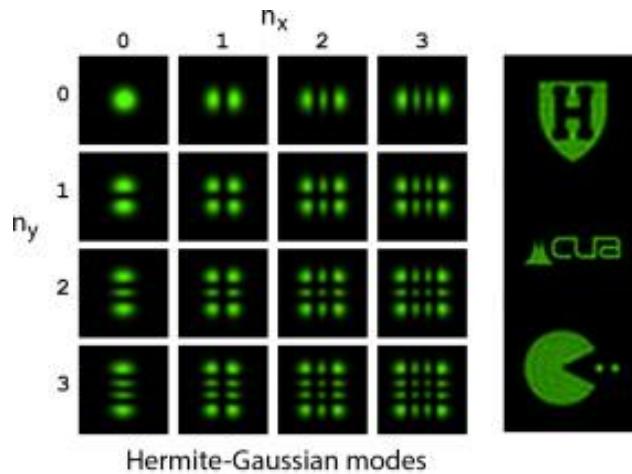
T. Fukuhara, *et al.*, *PRL* 115, 035302 (2015)

...



# Quantum gas microscopy

## Control



## Arbitrary Potentials

Digital Micromirror Device (DMD)

Boxes/ Edges

Site addressing

C. Weitenberg, et al., Nature 471, 319 (2011)

P. Zupancic et al., Opt. Express 24, 13881 (2016)

...

## Lower temperatures

Lattice loading

Equilibrium

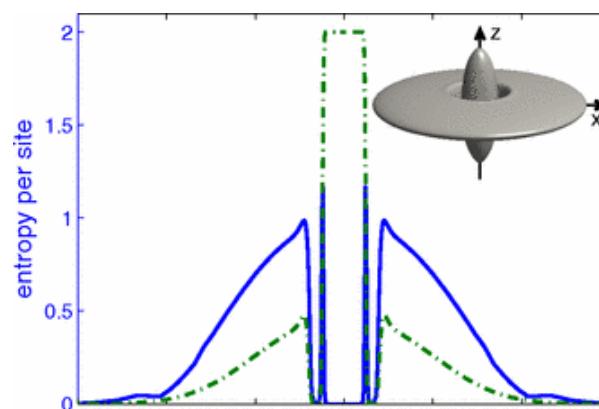
Entropy redistribution

T.-L. Ho, et al., PNAS 106, 6916 (2009)

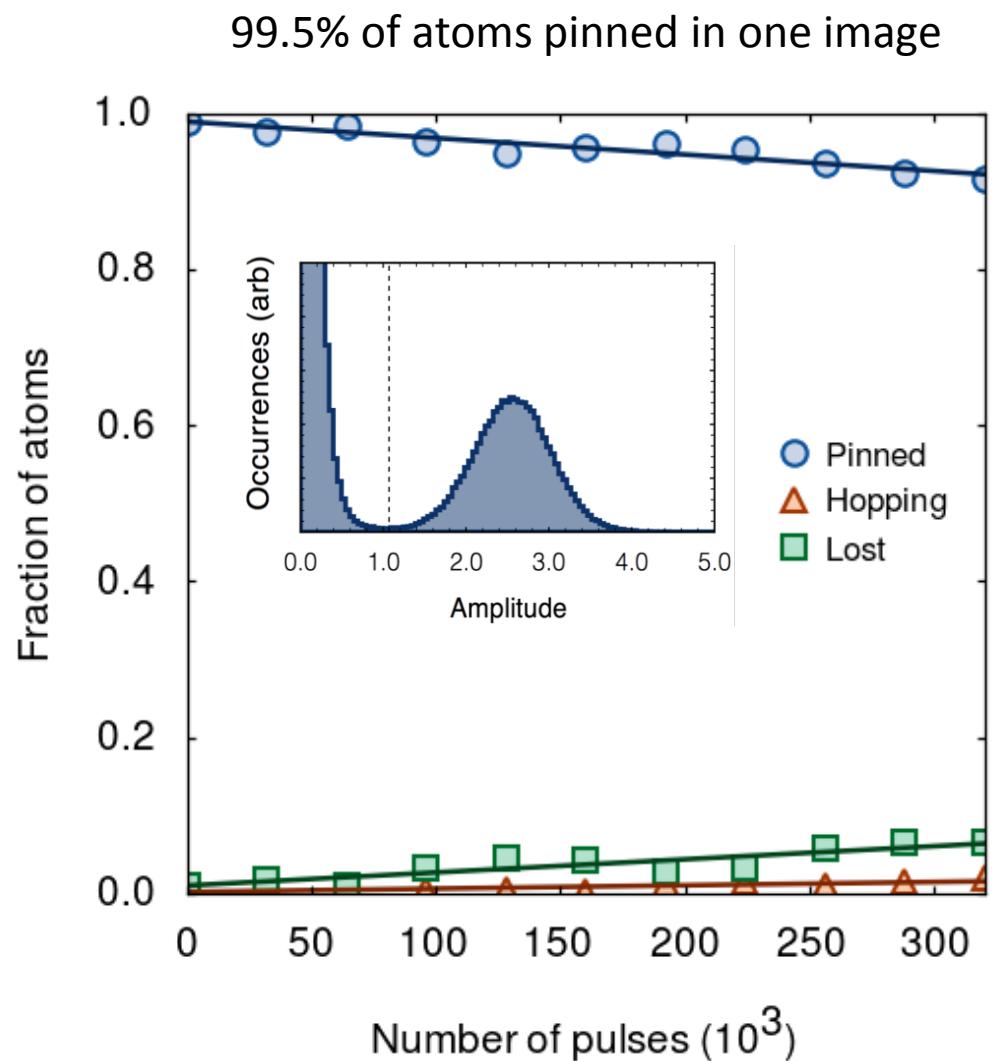
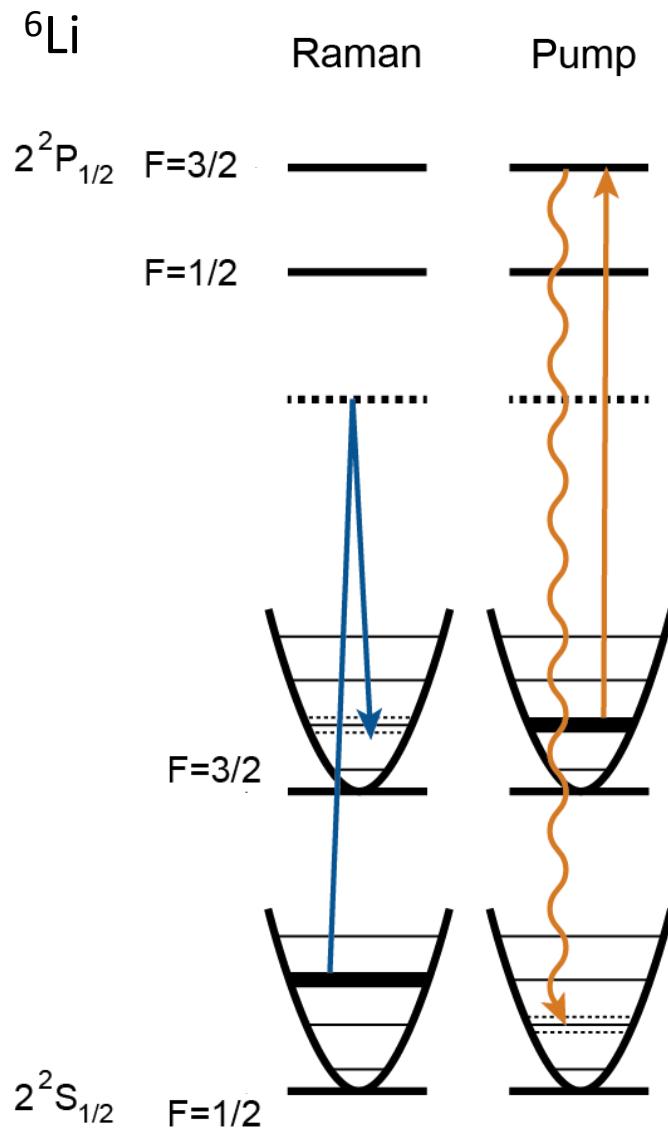
J.-S. Bernier, et al., PRA 79, 061601 (2009)

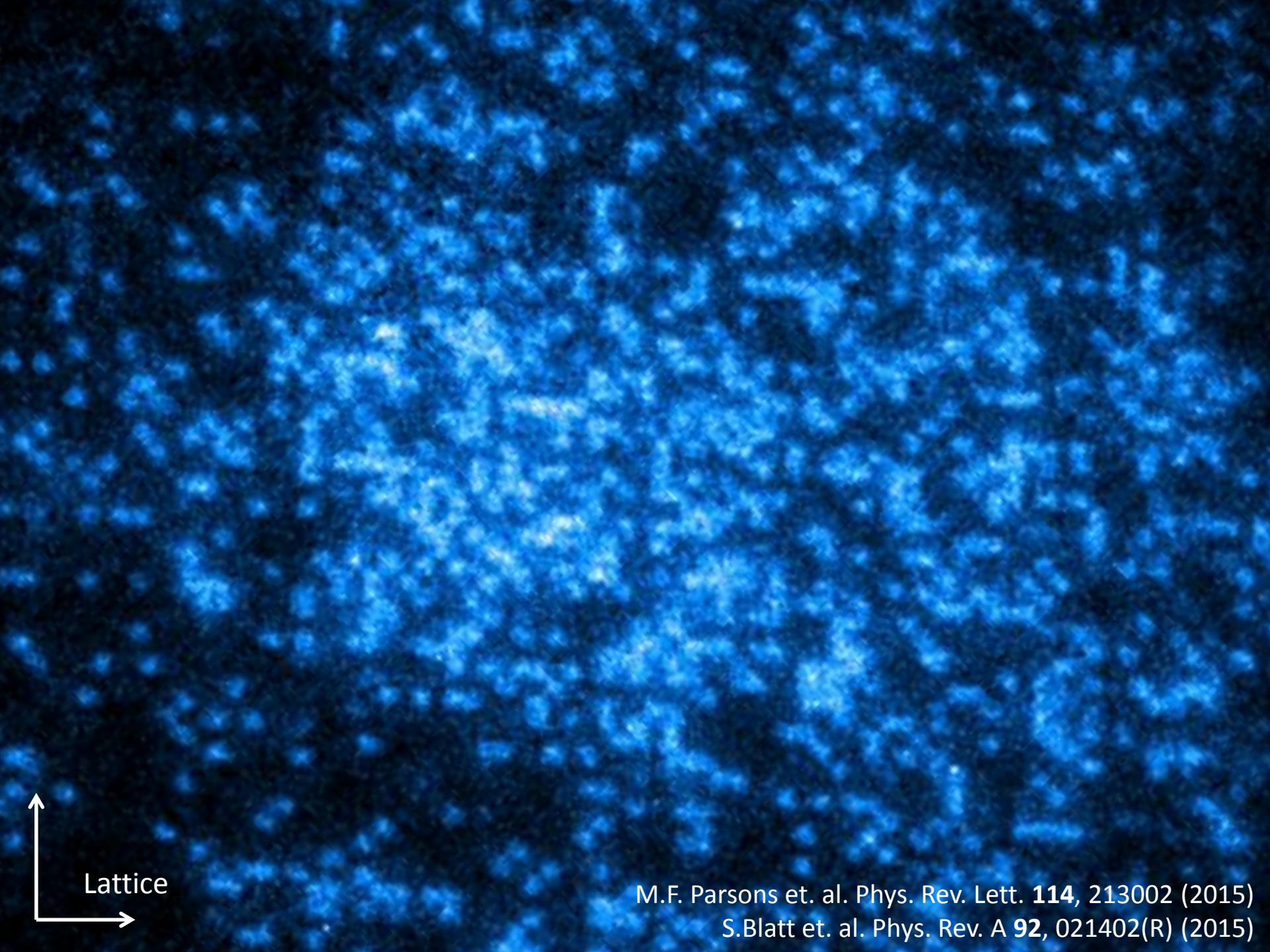
W. Bakr et al., Nature 480, 500 (2011)

...



# Raman sideband imaging





Lattice

M.F. Parsons et. al. Phys. Rev. Lett. **114**, 213002 (2015)  
S.Blatt et. al. Phys. Rev. A **92**, 021402(R) (2015)

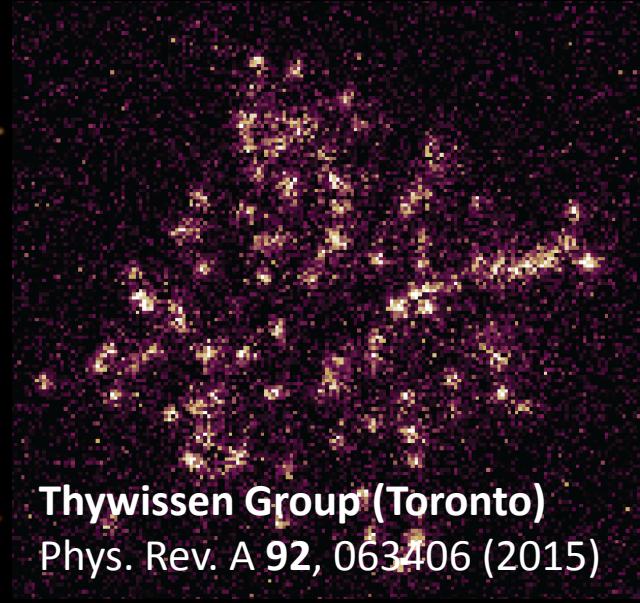
# 2015 in Fermi Gas Microscopy



**Kuhr Group (Glasgow)**  
Nature Physics **11**, 738 (2015)



**Zwierlein Group (MIT)**  
Phys. Rev. Lett. **114**, 193001(2015)



**Thywissen Group (Toronto)**  
Phys. Rev. A **92**, 063406 (2015)

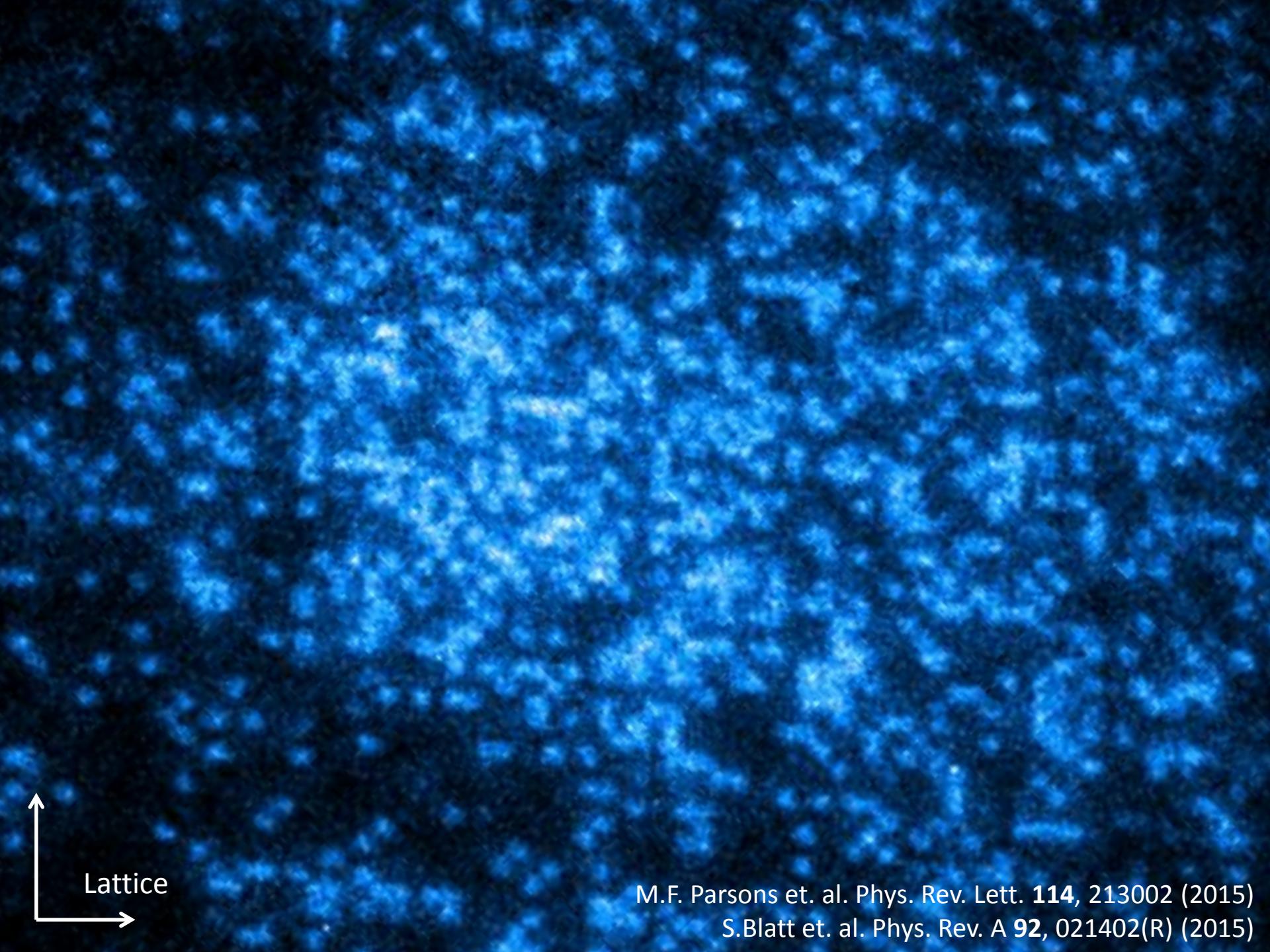


**Gross/Bloch Group (Munich)**  
Spin Polarized Band Insulator  
Phys. Rev. Lett. **115**, 263001 (2015)



**Greiner Group (Harvard)**  
Phys. Rev. Lett. **114**, 213002 (2015)

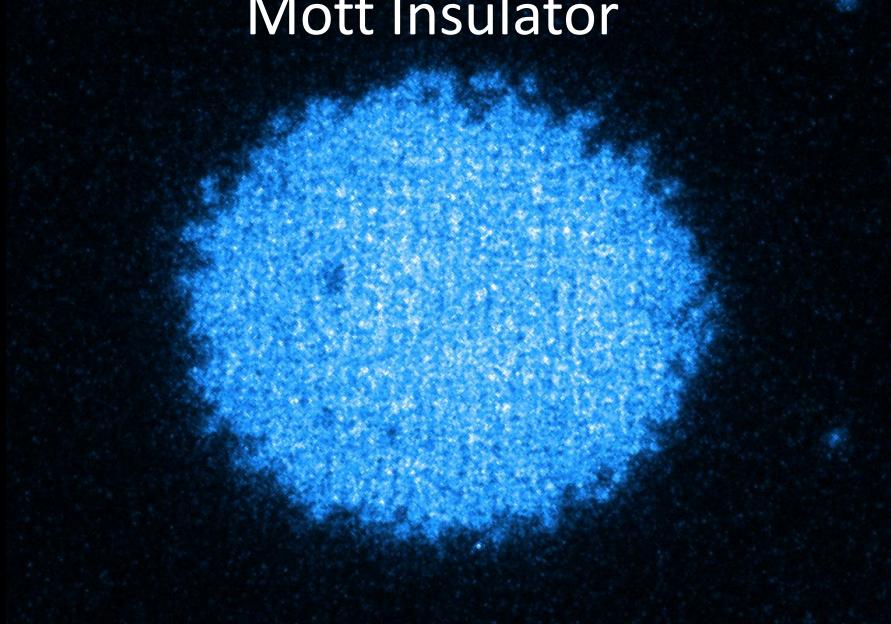
Also:  
**Bakr group**  
**(Princeton)**  
and many  
more (10+)



Lattice

M.F. Parsons et. al. Phys. Rev. Lett. **114**, 213002 (2015)  
S.Blatt et. al. Phys. Rev. A **92**, 021402(R) (2015)

## Mott Insulator

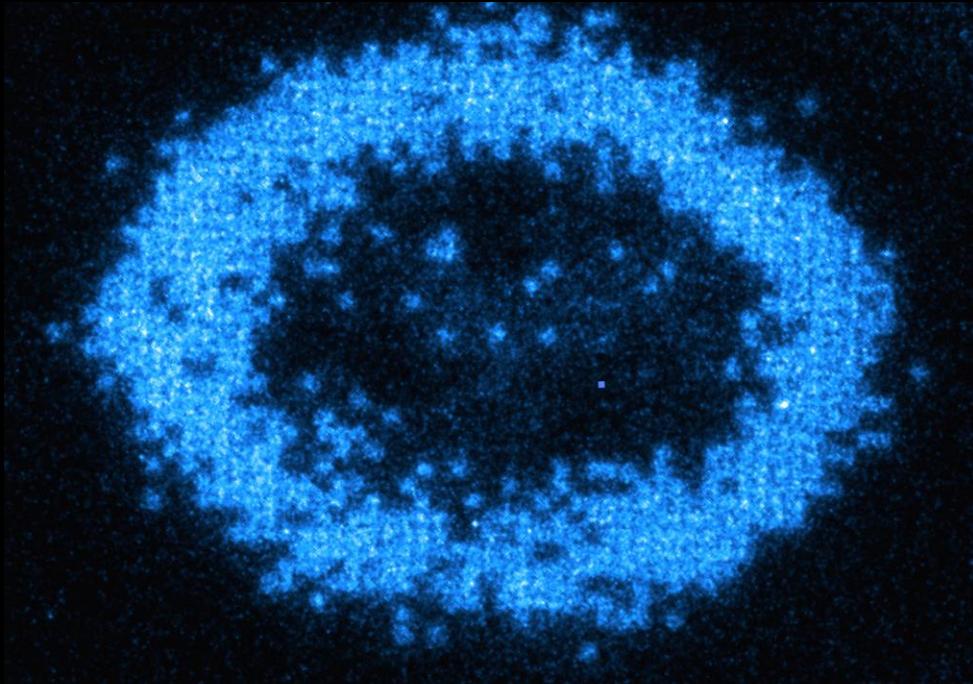
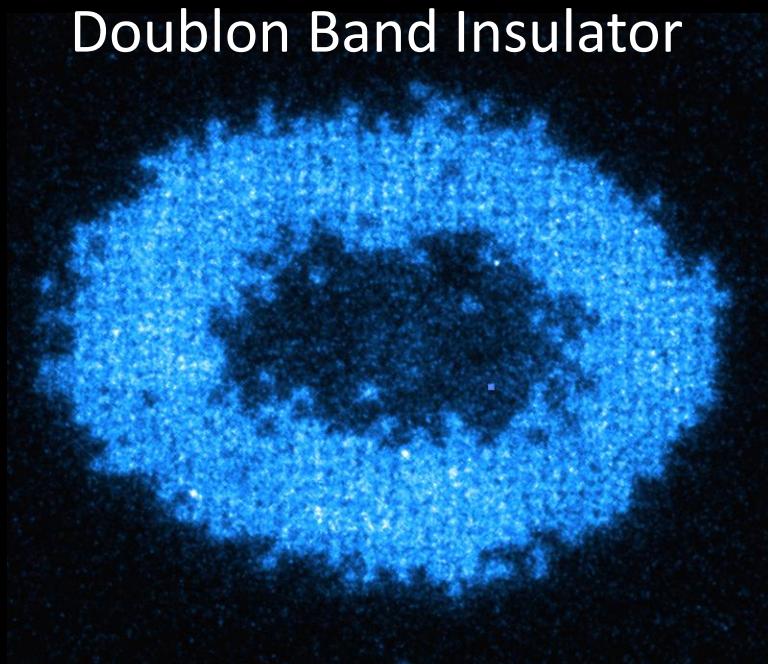


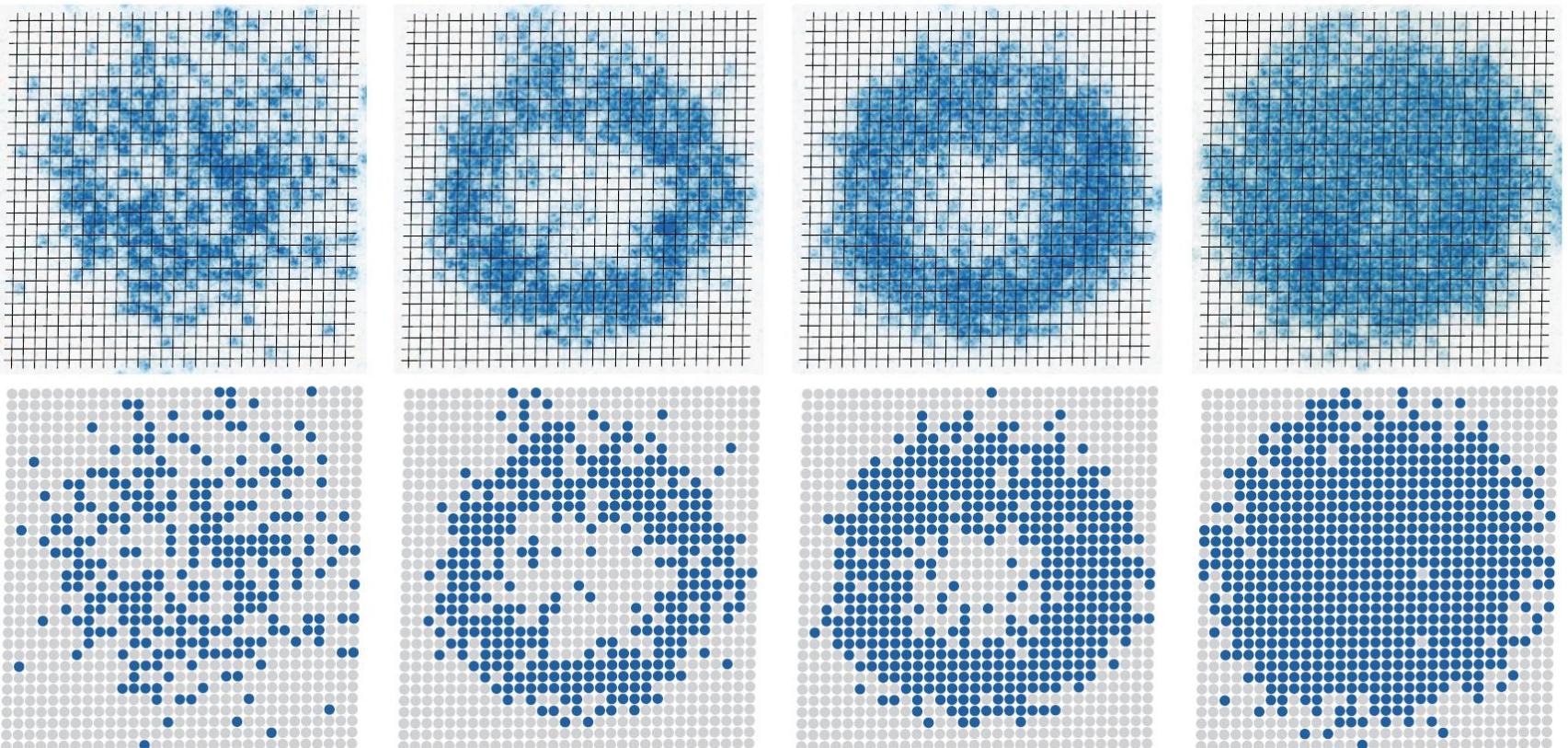
## Experimental Parameters

- Balanced two-component spin mix of Li-6 in hyperfine  $|1\rangle$  and  $|2\rangle$  states
- Atom numbers:  $N = 100\text{-}1000$
- Repulsive interactions:  $a = 37\text{-}515 a_0$
- 1064nm optical lattice
- Lattice depth:  $7\text{--}16 E_R$

## Large Doublon Band Insulator

## Doublon Band Insulator





Increasing Interactions  $U/t$



Metal



Band Insulator



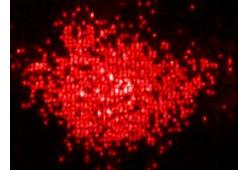
Mott Insulator

Gross/Bloch group (Munich)

Non-int. Band insulator:

A. Ohmran et al.,

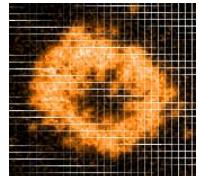
PRL 115, 263001 (2015)



Zwierlein group (MIT)

L. Cheuk et al.,

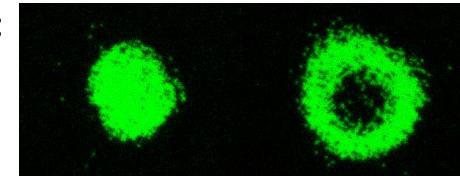
PRL 116, 235301 (2016)



Bakr group (Princeton)

W. Bakr et al.:

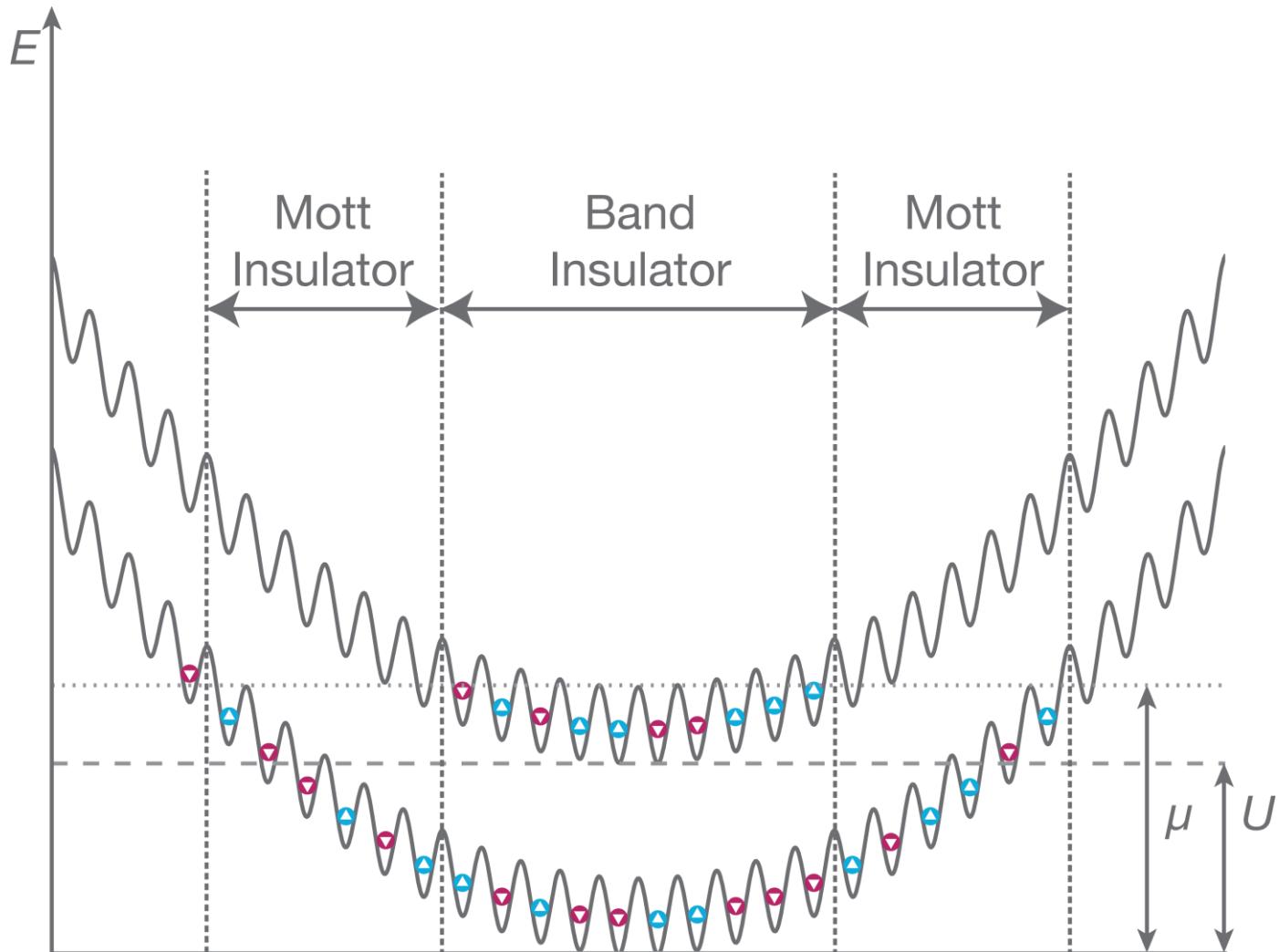
unpublished



D. Greif et al., Science 351, 953 (2016)

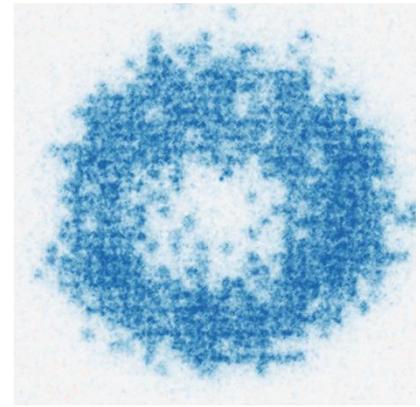
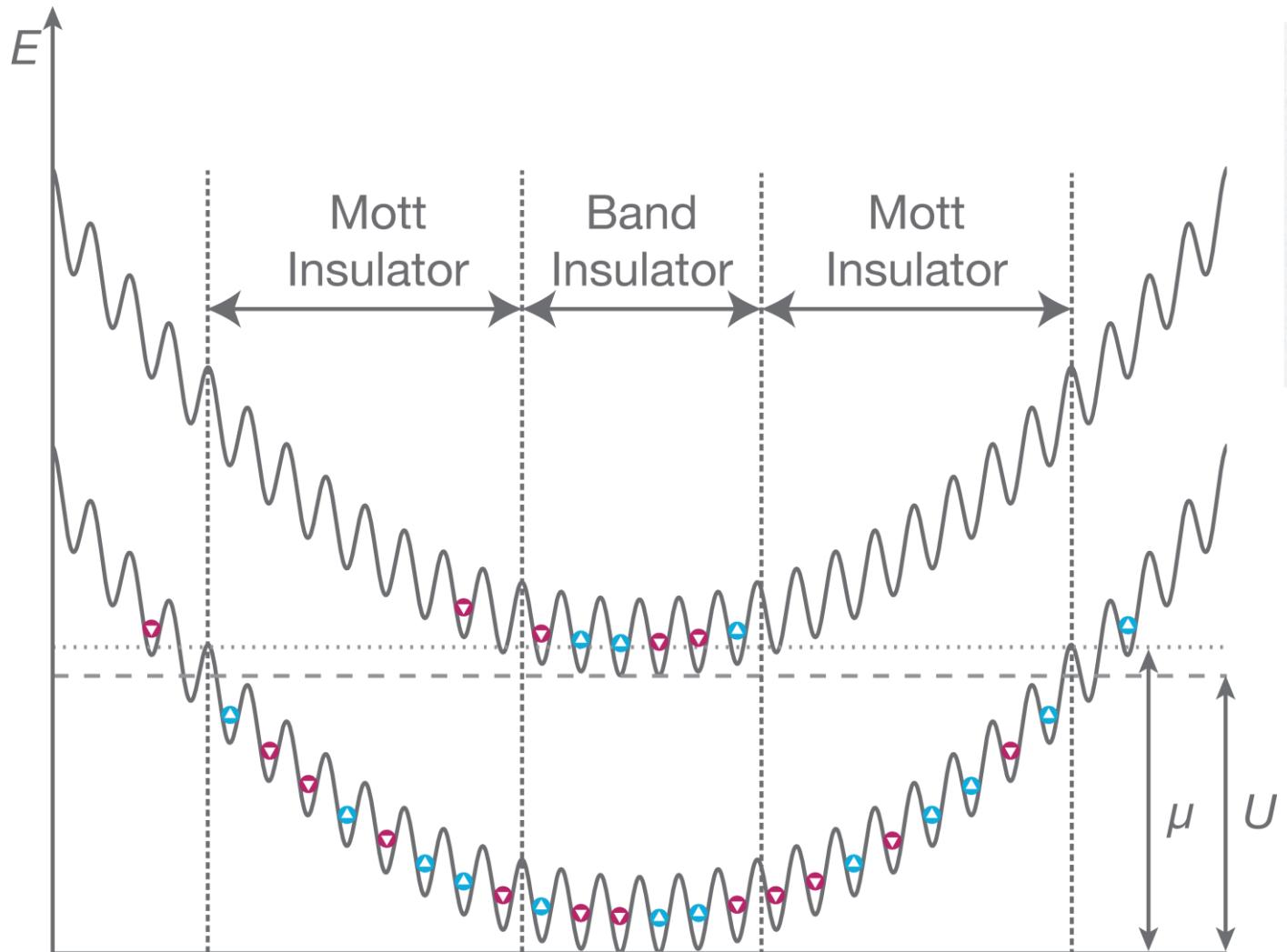


# From metals to Mott insulators



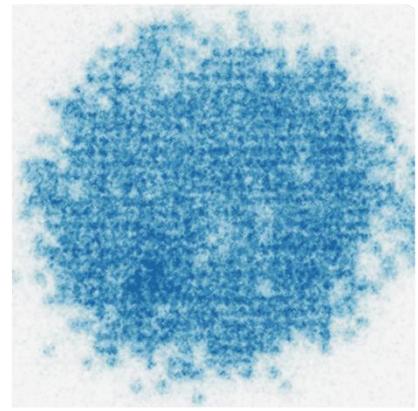
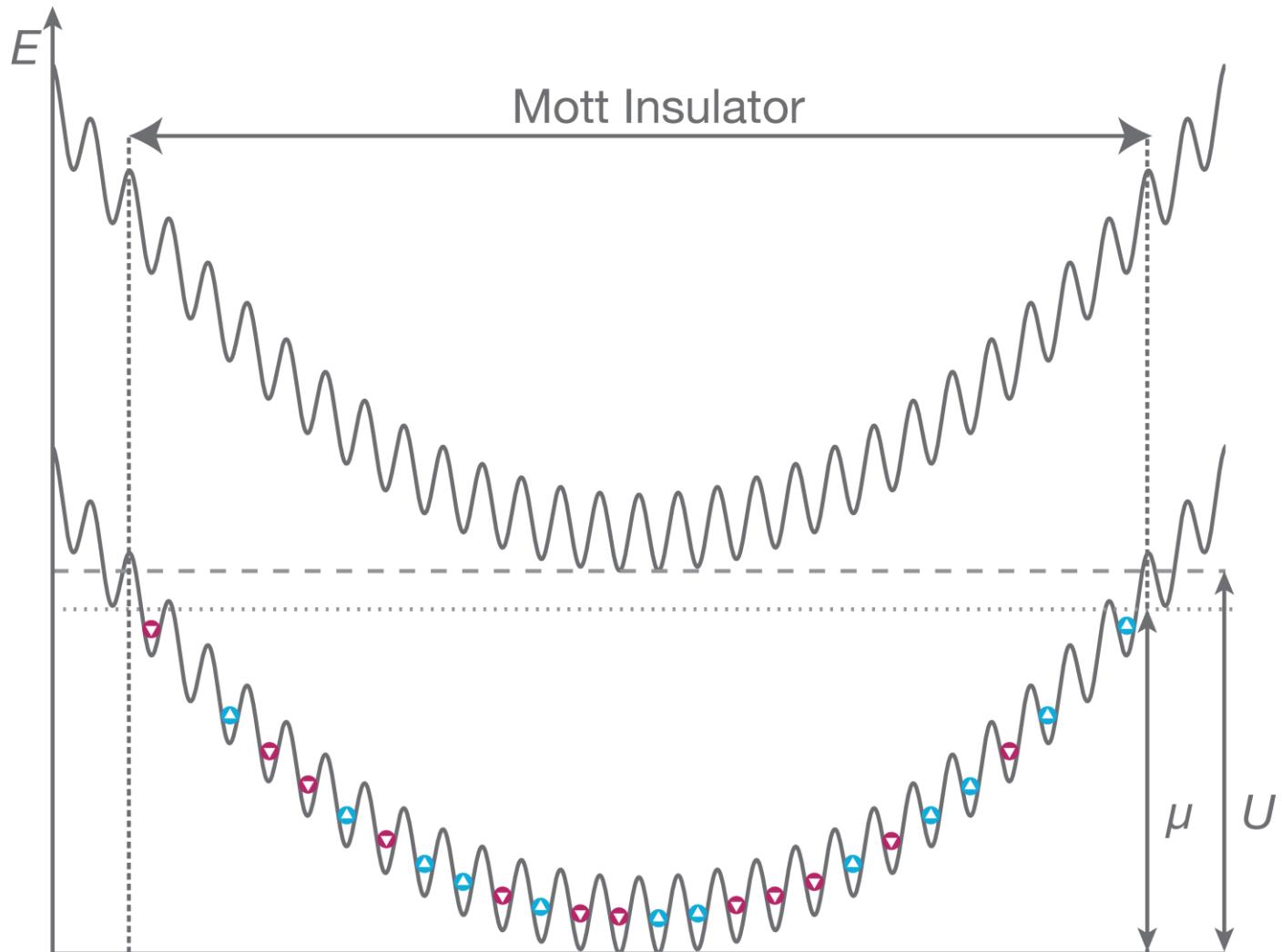


# From metals to Mott insulators

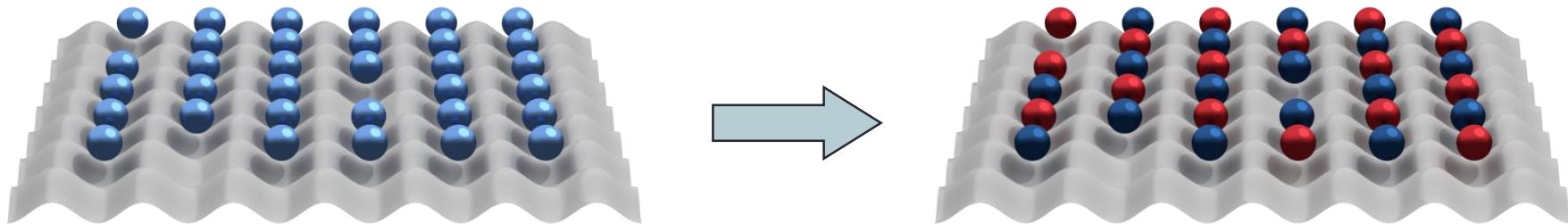




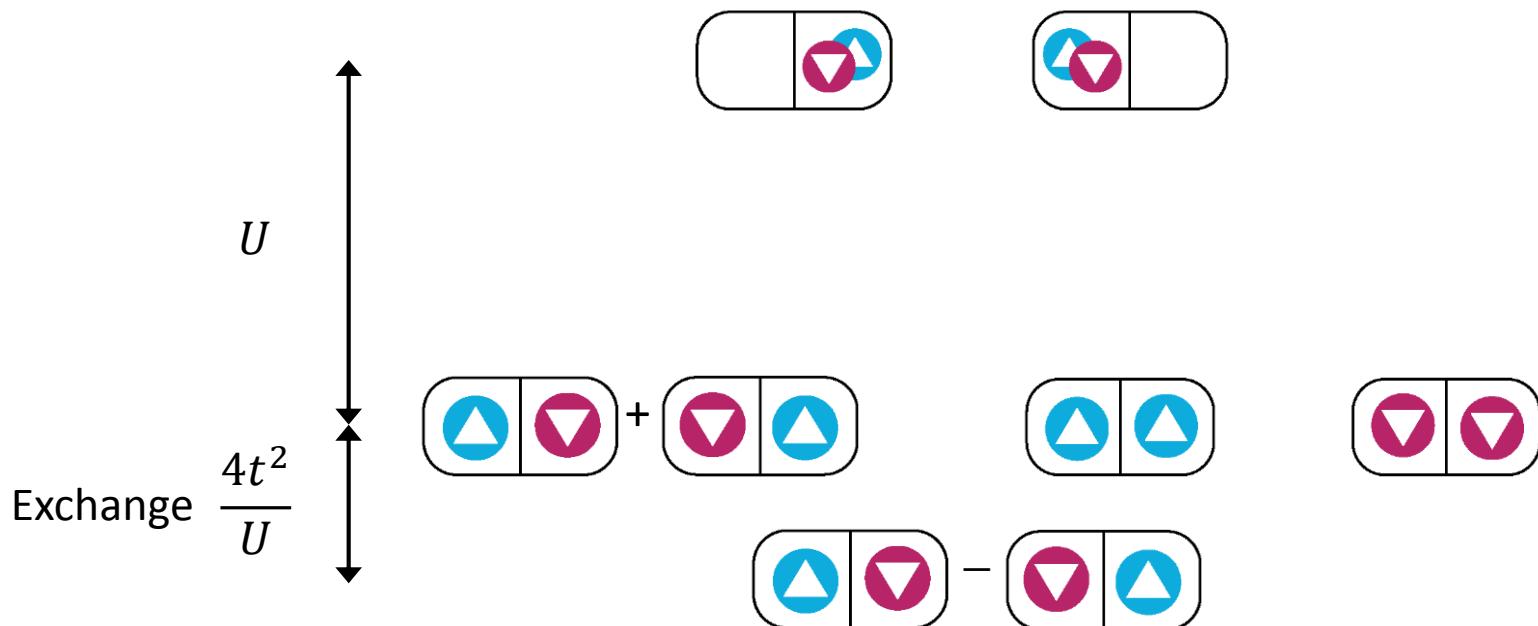
# From metals to Mott insulators



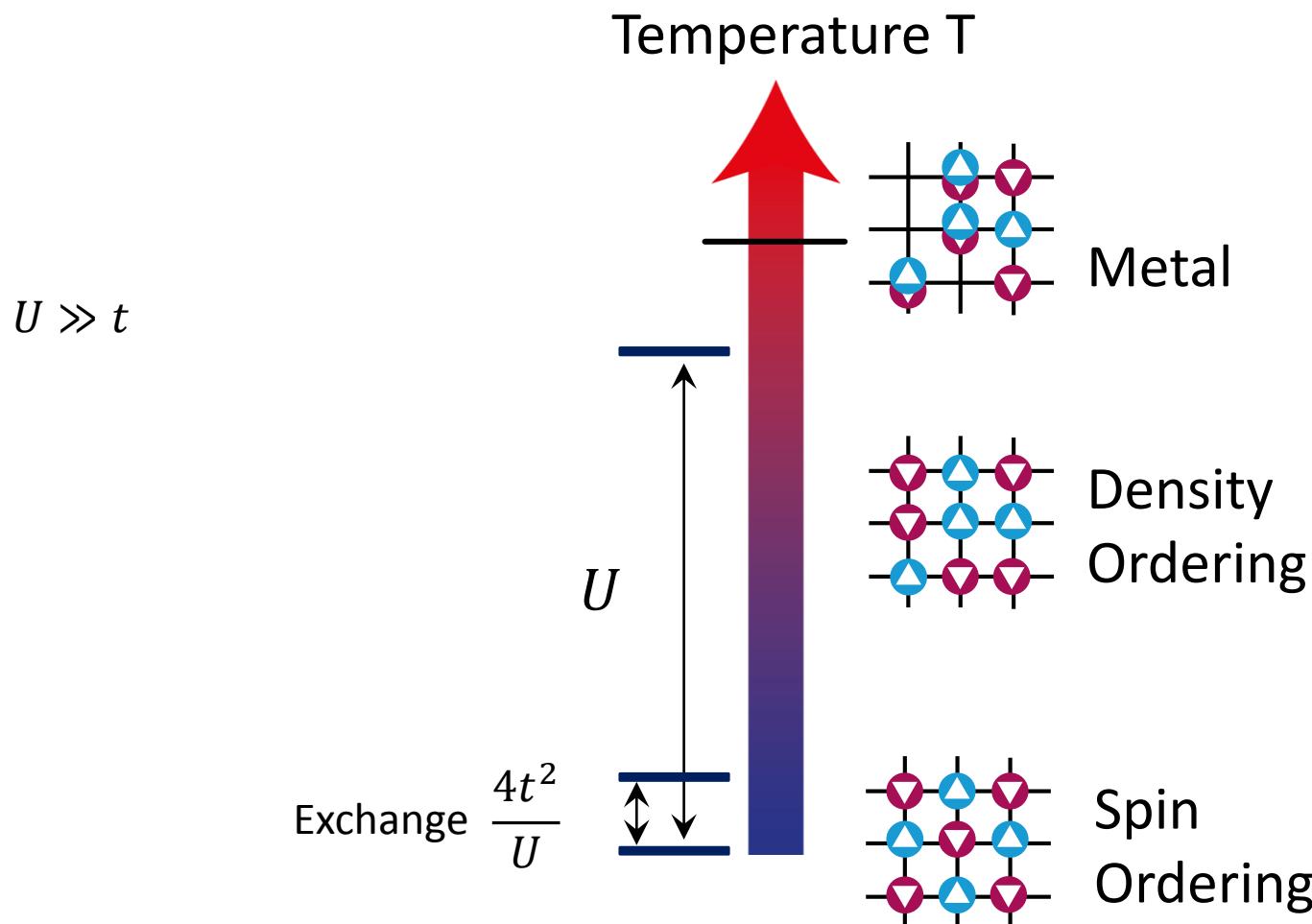
# Antiferromagnetism in the Fermi-Hubbard model



$$U \gg t$$



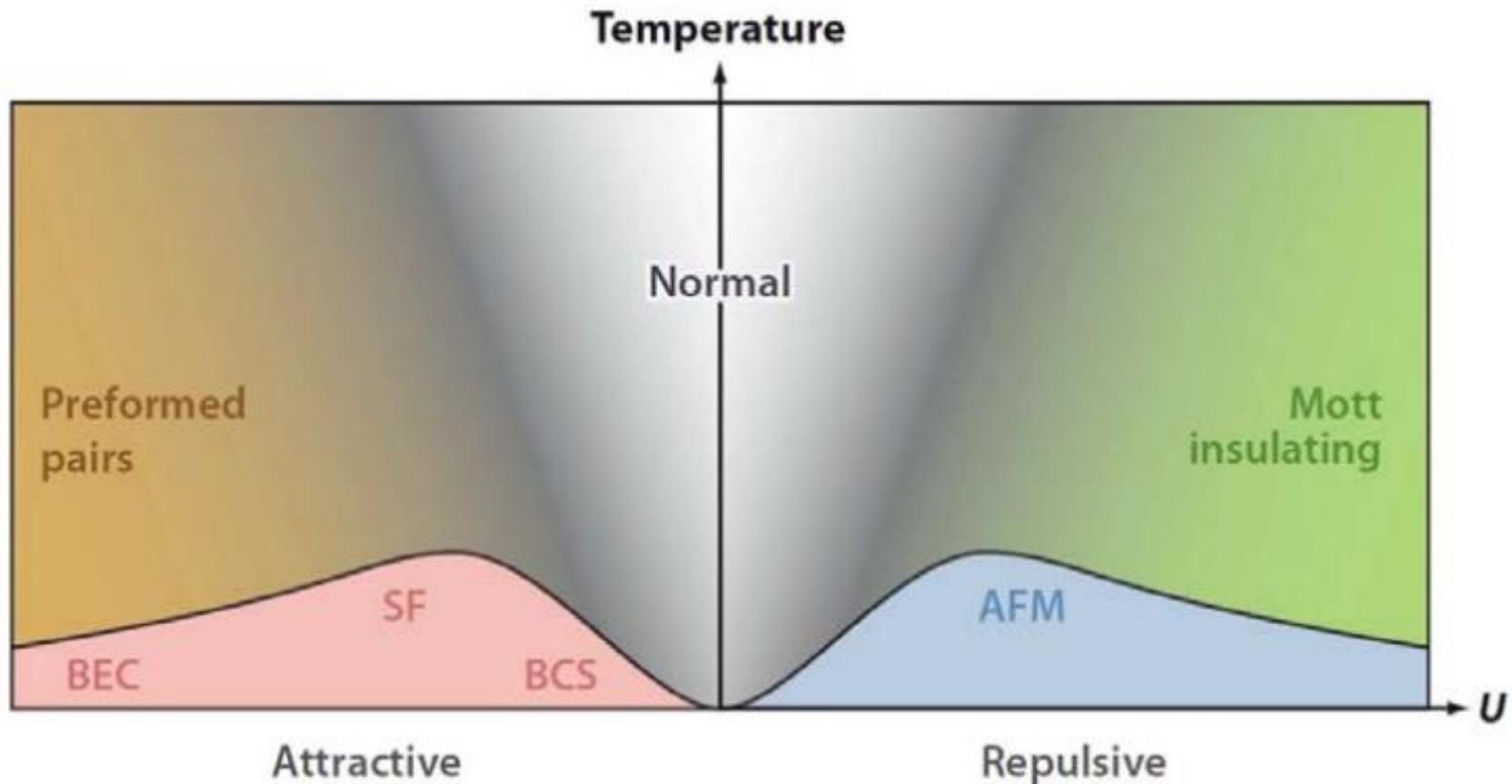
# Antiferromagnetism in the Fermi-Hubbard model



# Antiferromagnetism in the Fermi-Hubbard model



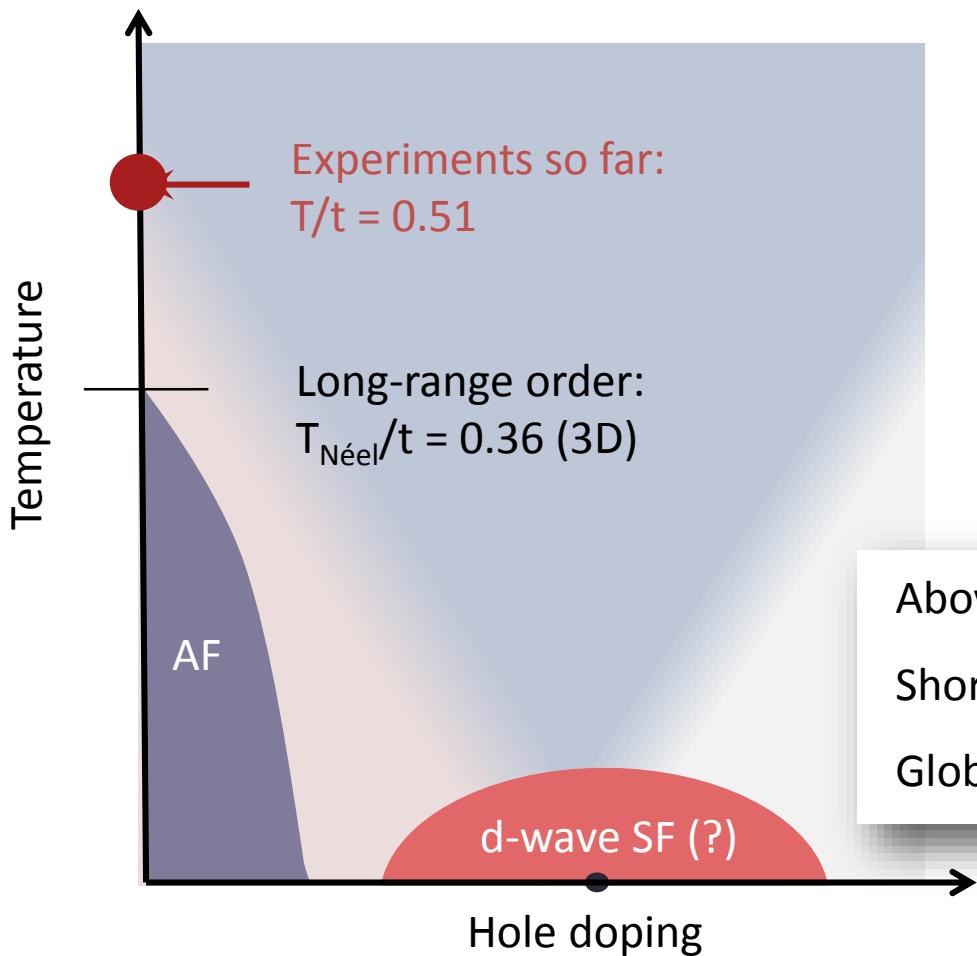
## 3D Fermi-Hubbard model



# Antiferromagnetism in the Fermi-Hubbard model



## 3D Fermi-Hubbard model



### Theory:

- Lee et al., Rev. Mod. Phys. 78, 17 (2006)
- Varma et al., Nature 468, 184 (2010)
- Paiva et al., PRL 107, 086401 (2011)
- Kozik et al., PRB 87, 205102 (2013)

Detection via local singlets: Zurich

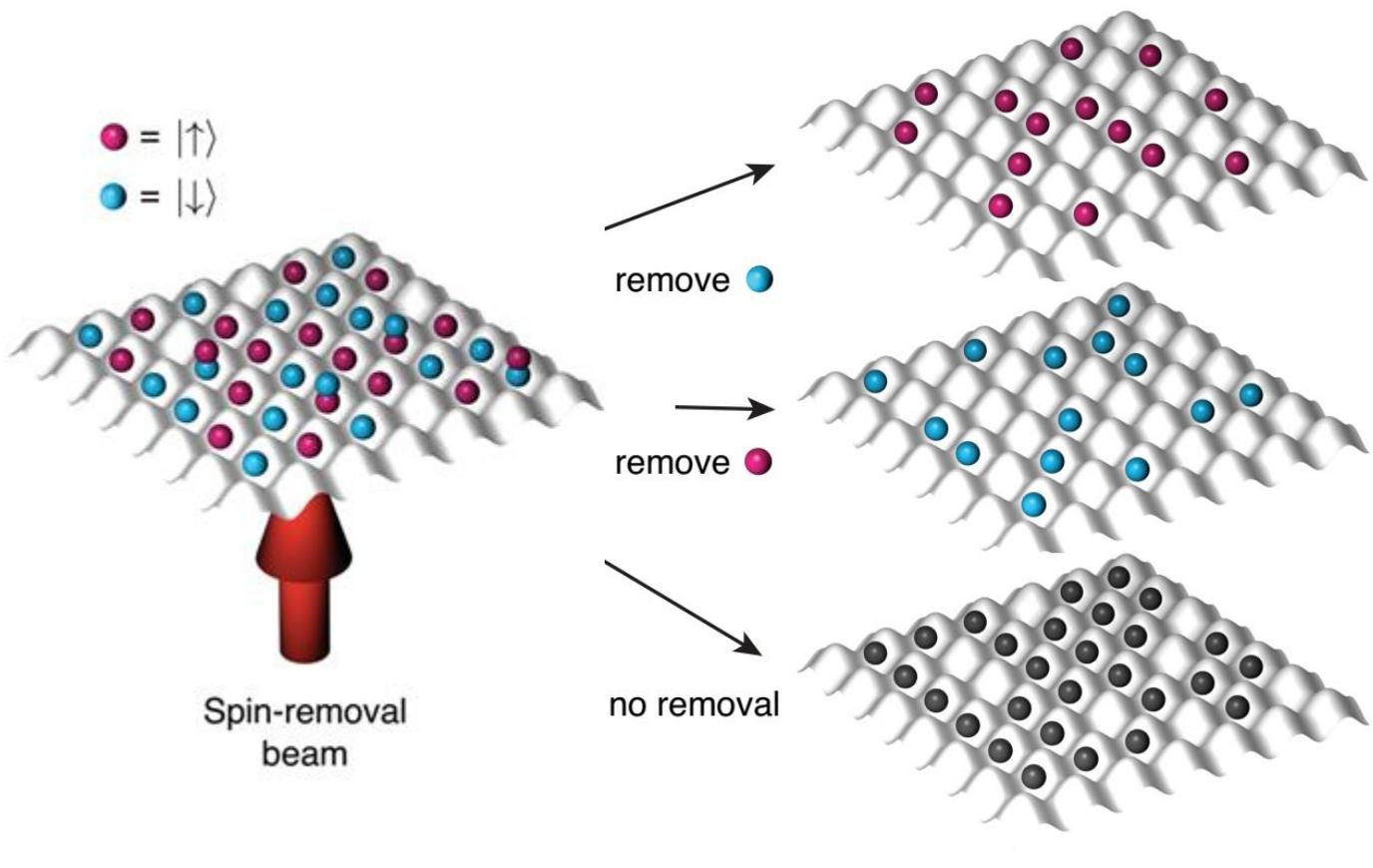
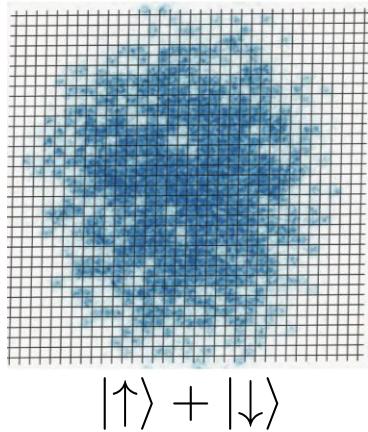
D. Greif, et al. Science, 340, 1307 (2013)

Detection via Bragg scattering: Rice

R. Hart, et al. Nature, 519, 211 (2015)

Above long-range ordering temperature  $T_{\text{N\'eel}}$   
Short-range antiferromagnetic correlations  
Globally averaged observables

# Measuring the spin correlator

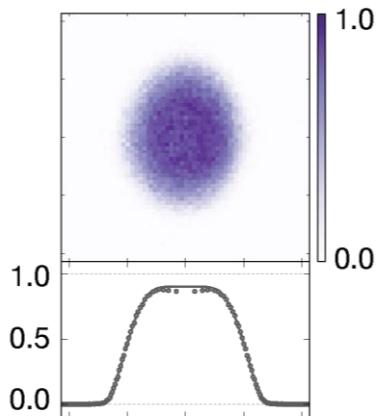


$$\langle S_i^z S_{i+d}^z \rangle = \text{[diagram with two up-spins]} + \text{[diagram with two down-spins]} - \text{[diagram with one up and one down spin]} - \text{[diagram with one down and one up spin]}$$

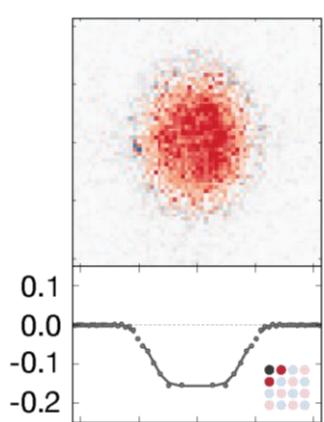
# Antiferromagnetic correlations



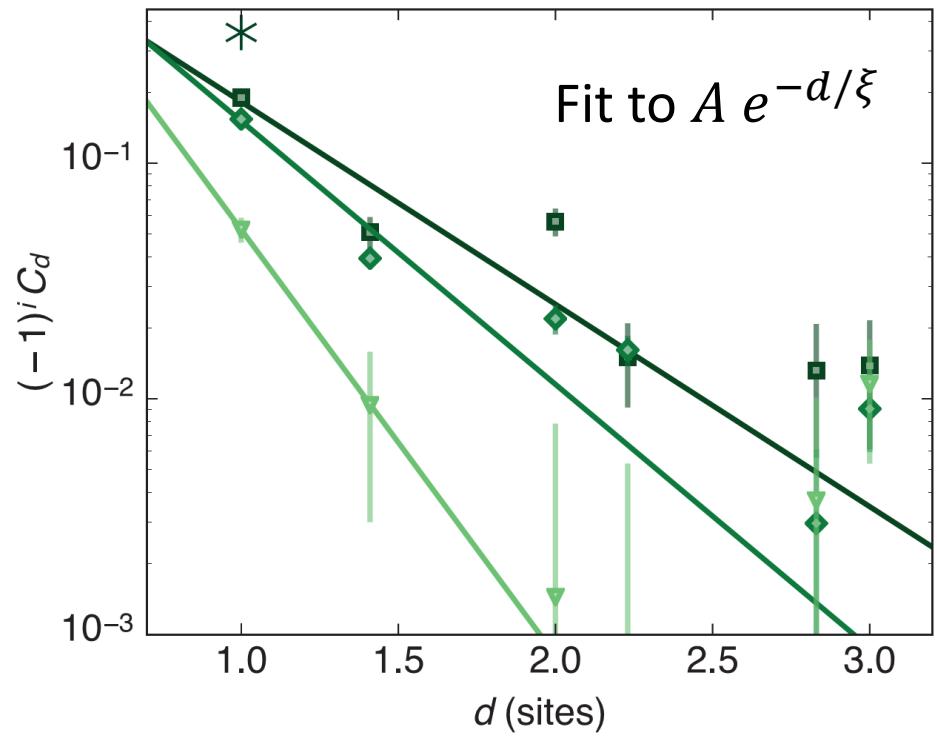
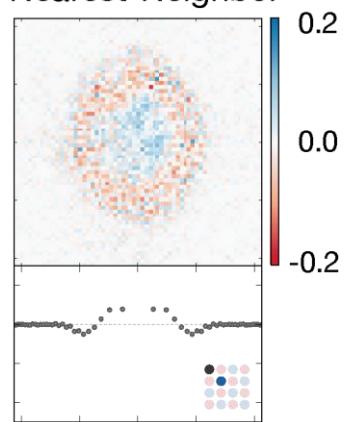
Density



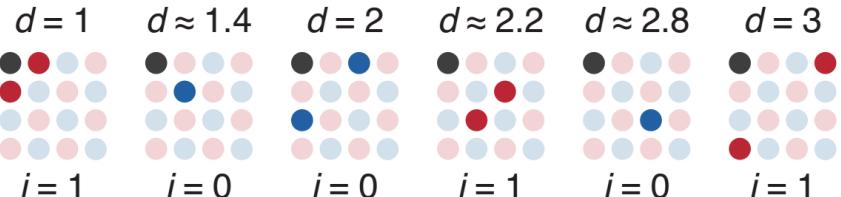
Nearest-Neighbor



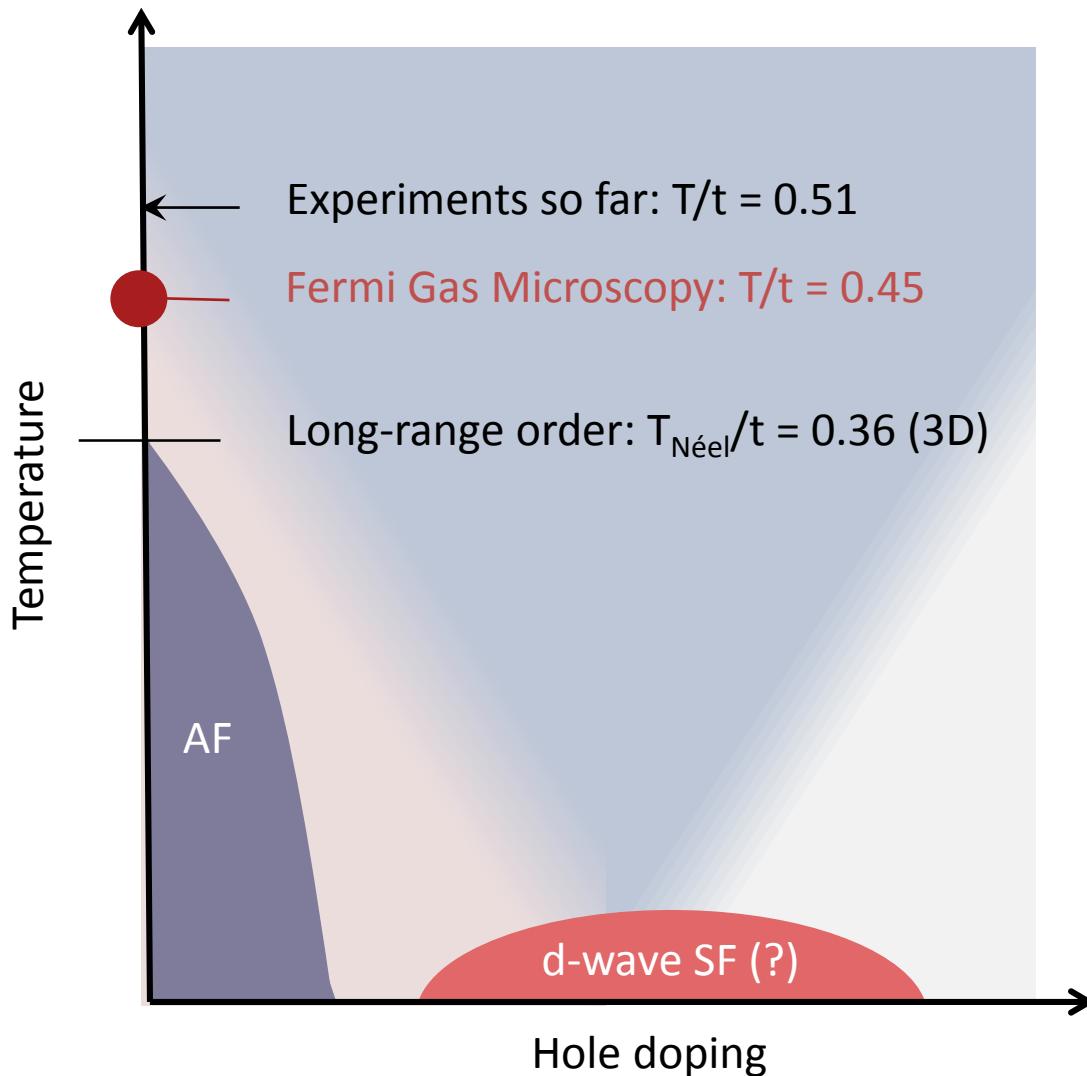
Next  
Nearest-Neighbor



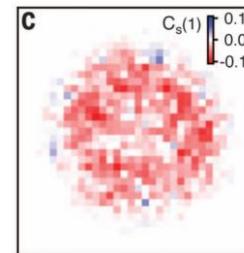
...



# Towards long-range order



Gross/Bloch group (Munich)  
1D AFM chains  
M. Boll et al.,  
*Science* 353, 1257 (2016)



Zwierlein group (MIT)  
Charge & spin correlations  
L. Cheuk et al.,  
*Science* 353, 1257 (2016)

Theory:  
Maier et al., PRL 95, 237001 (2005)  
Gull et al., PRL 110, 216405 (2013)

# Entropy engineering



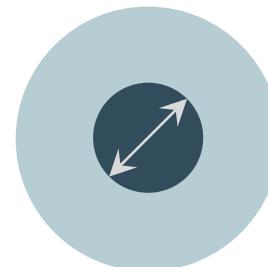
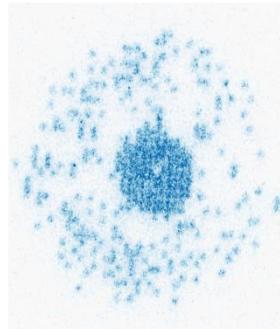
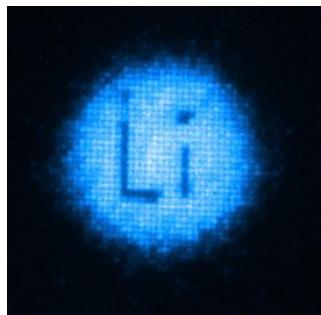
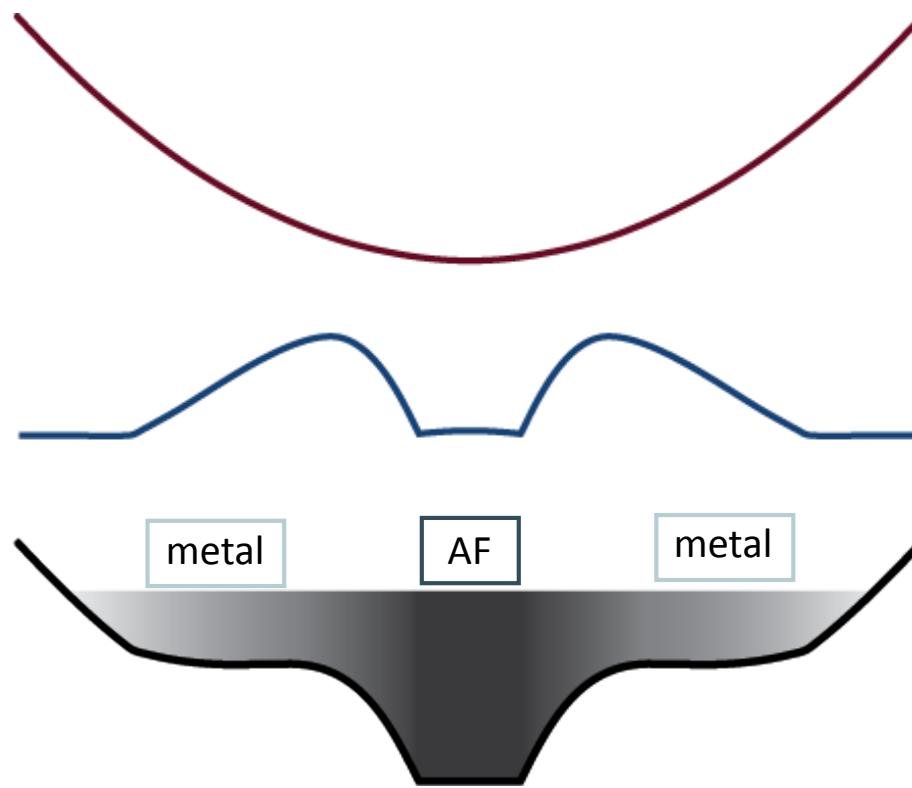
Harmonic potential  
(lattices)

+

DMD potential

=

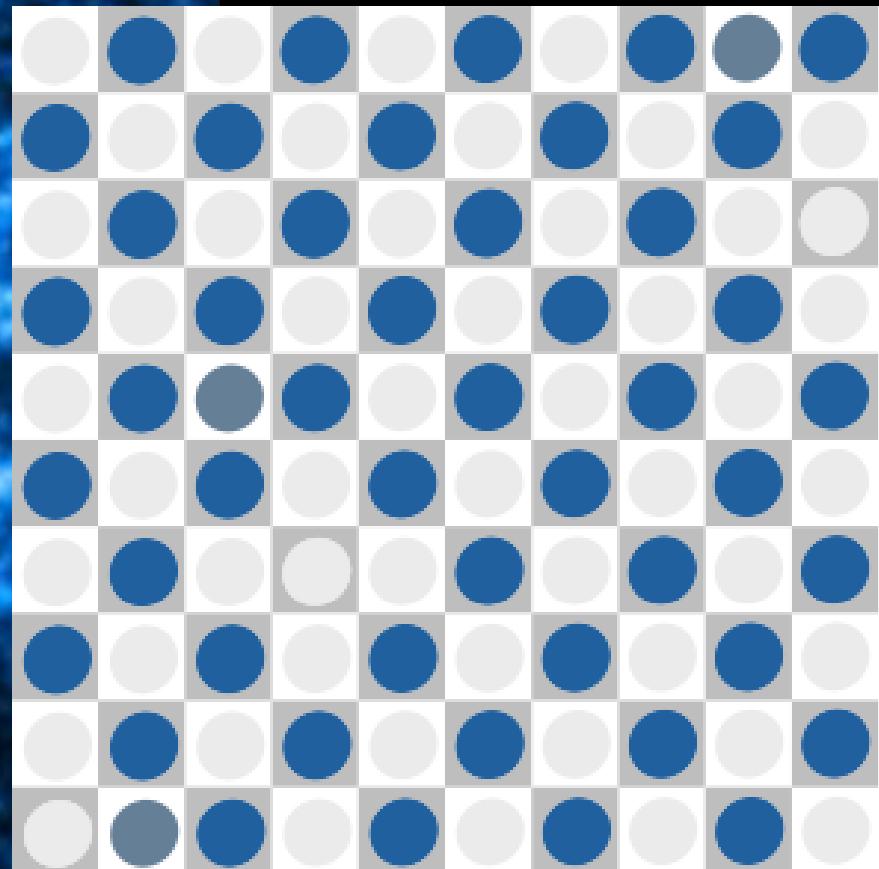
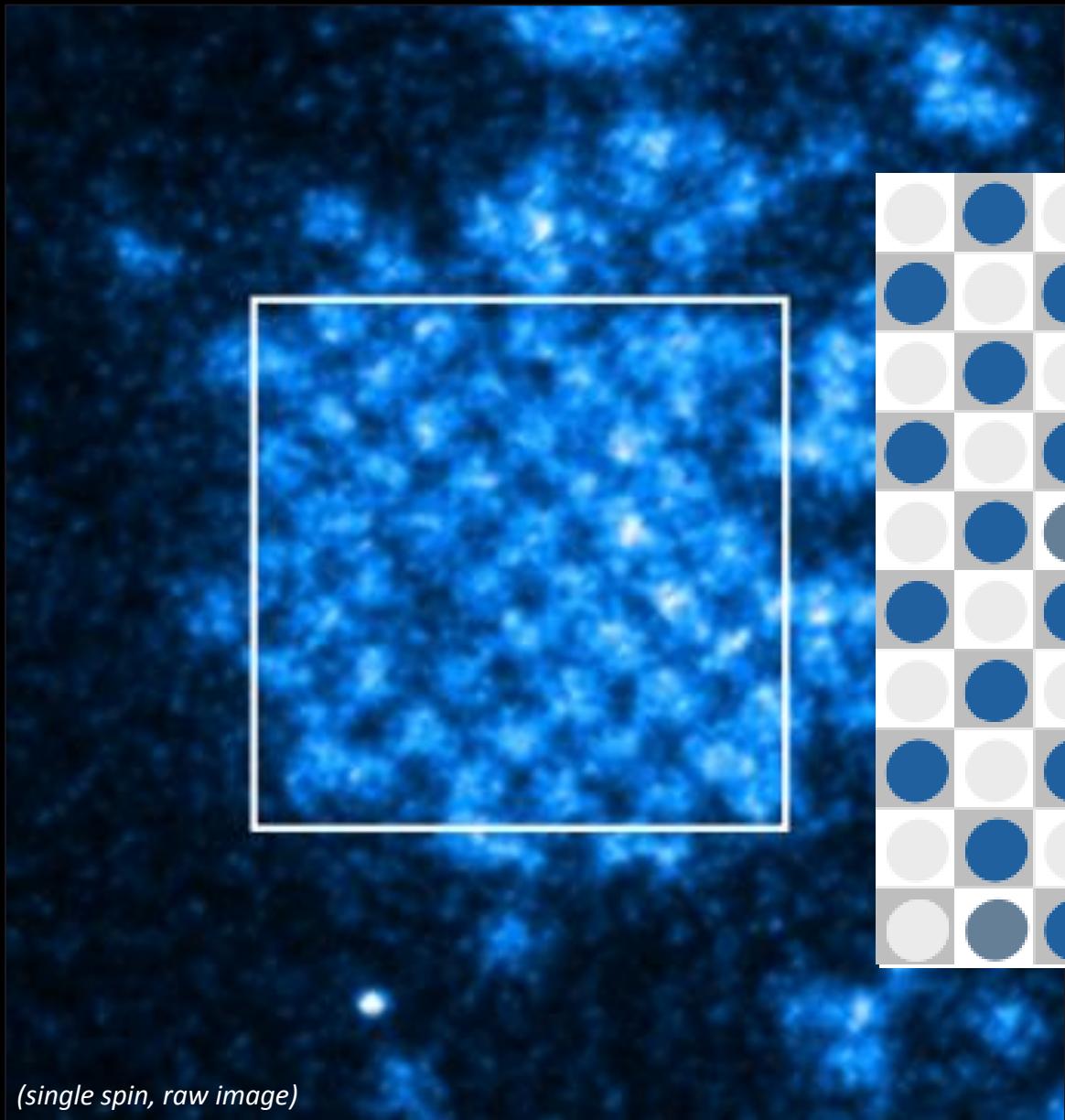
Total potential



Entropy Reservoir

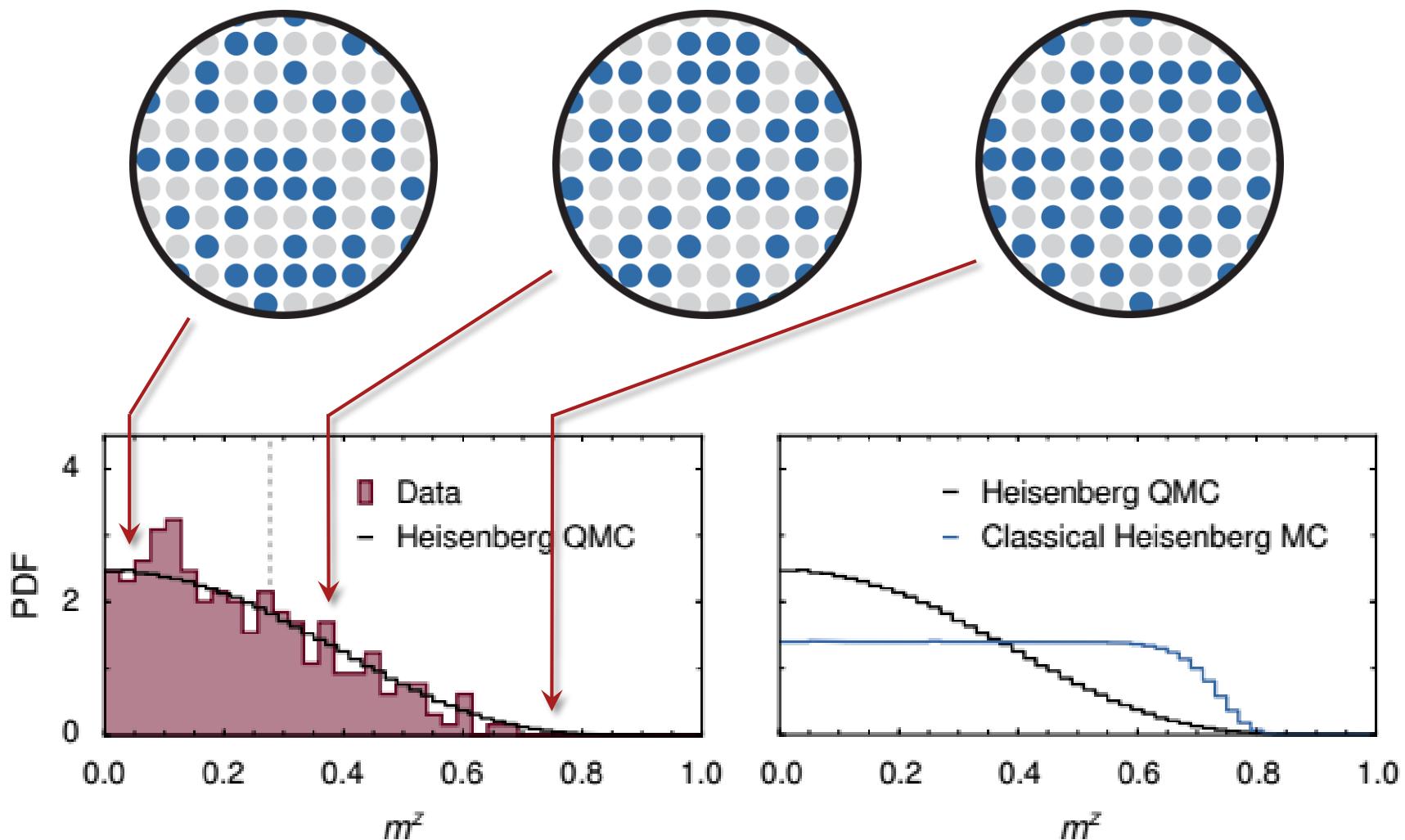
System  
10 sites across

# 2D Antiferromagnetic order



(single spin, raw image)

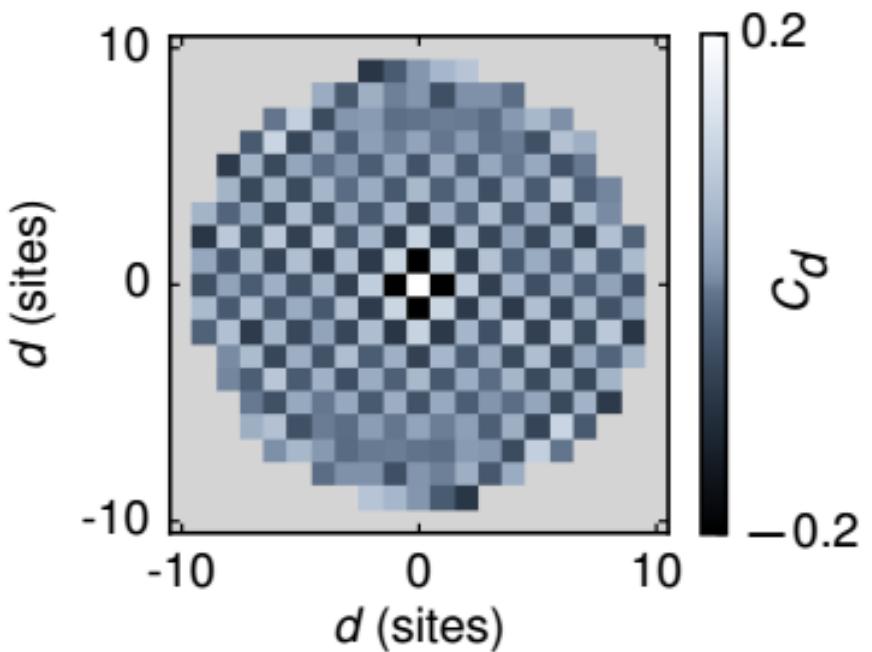
# 2D Antiferromagnetic order



# 2D Antiferromagnetic order

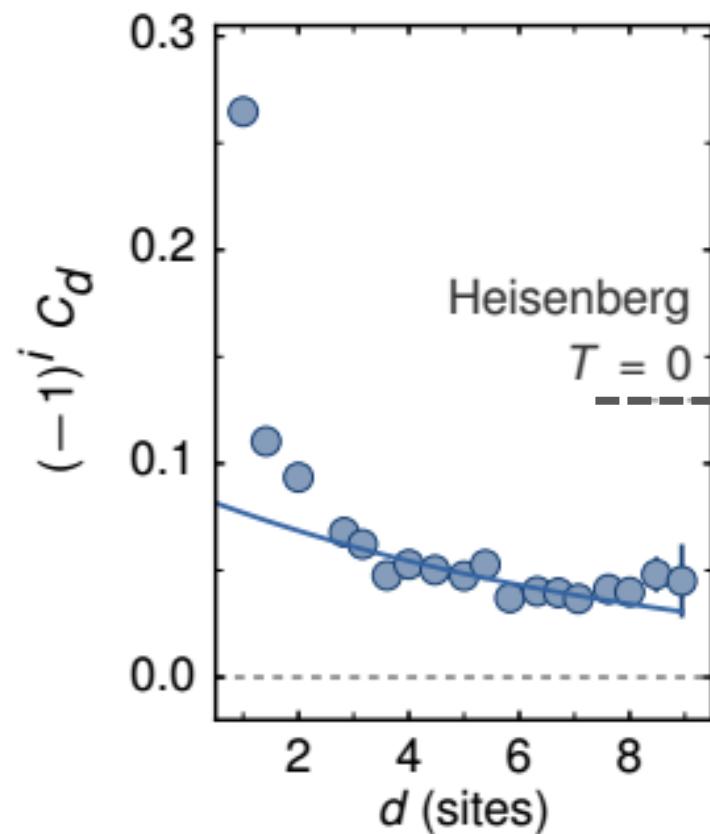


Spin correlator

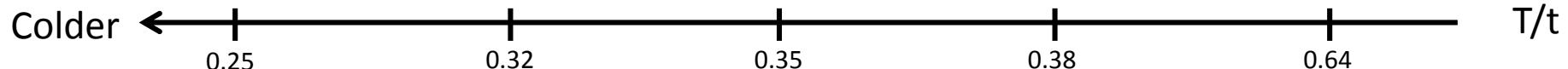
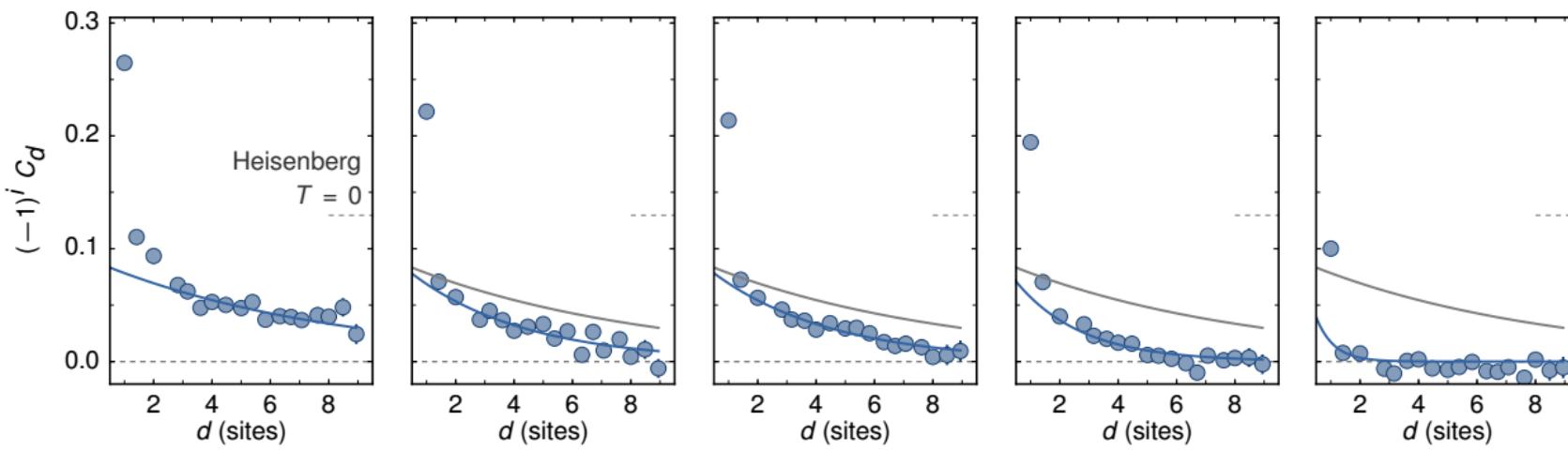
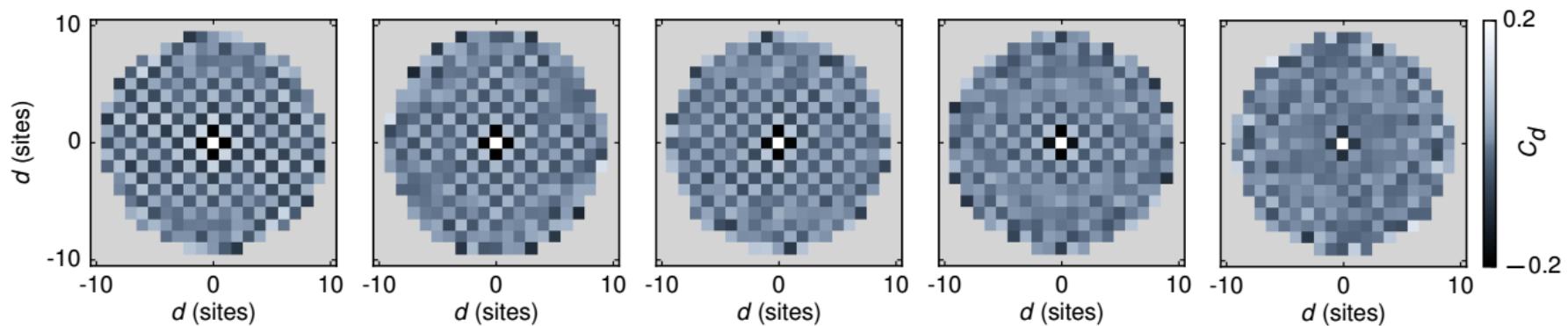


Azimuthal average

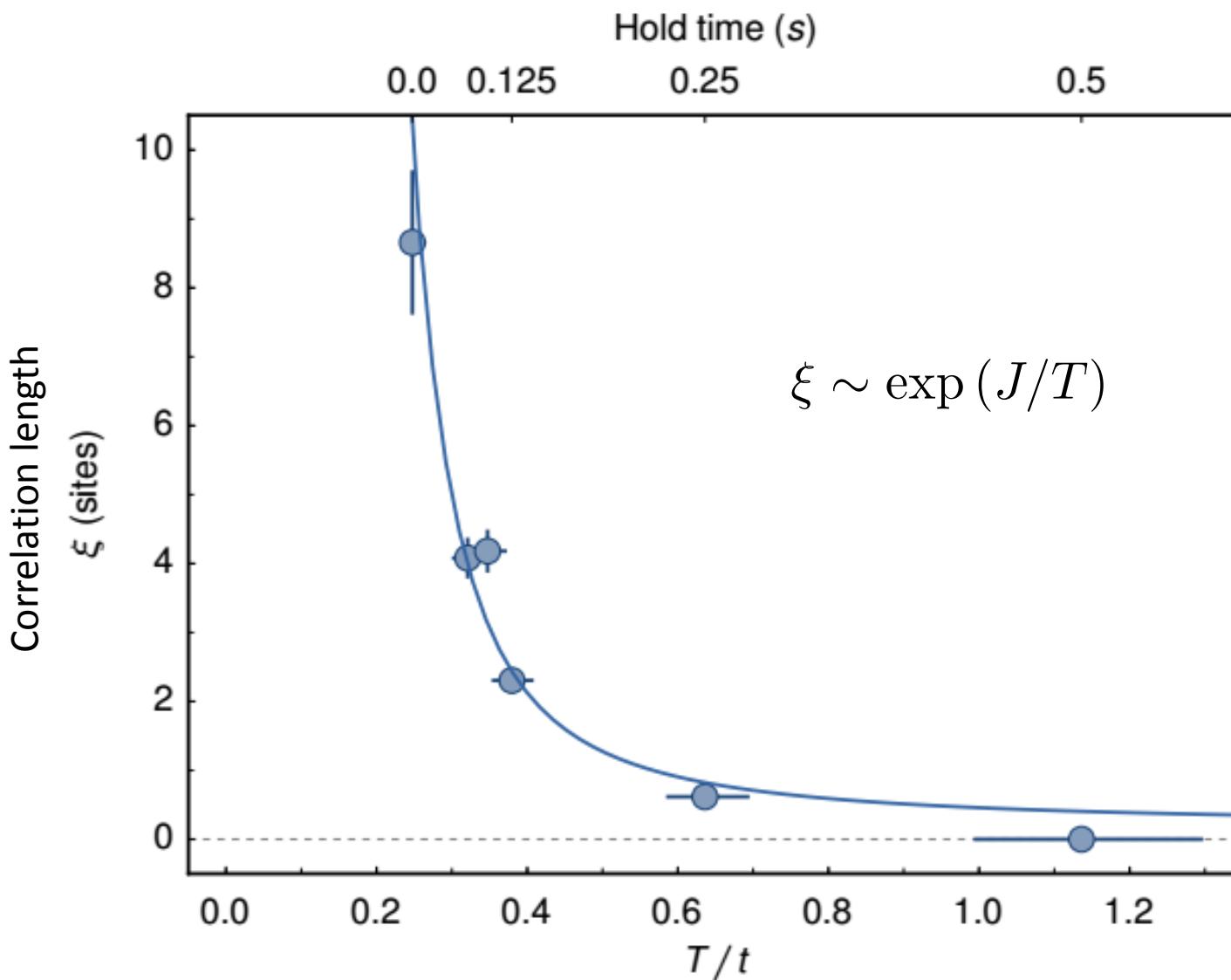
Spin correlation function



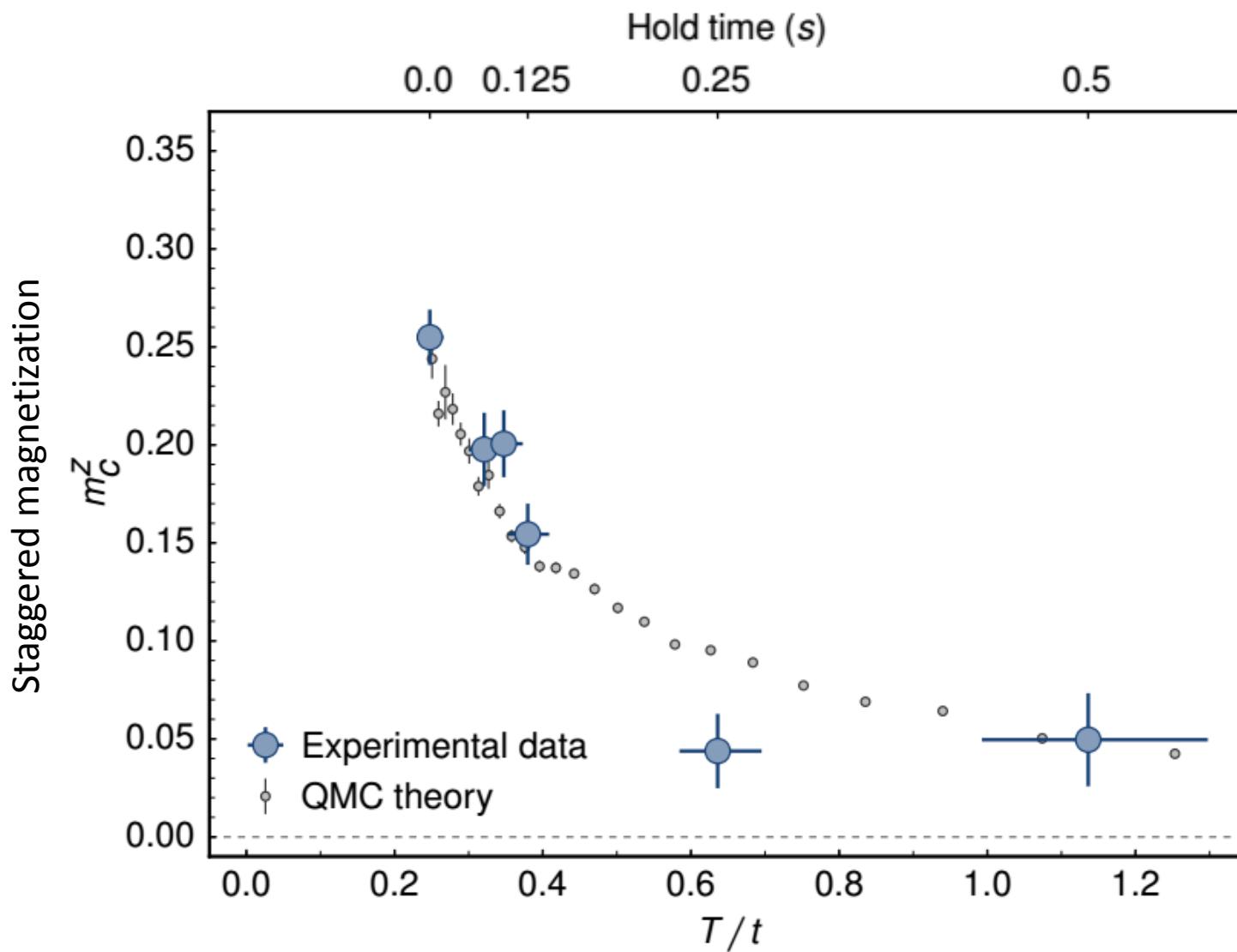
# 2D Antiferromagnetic order



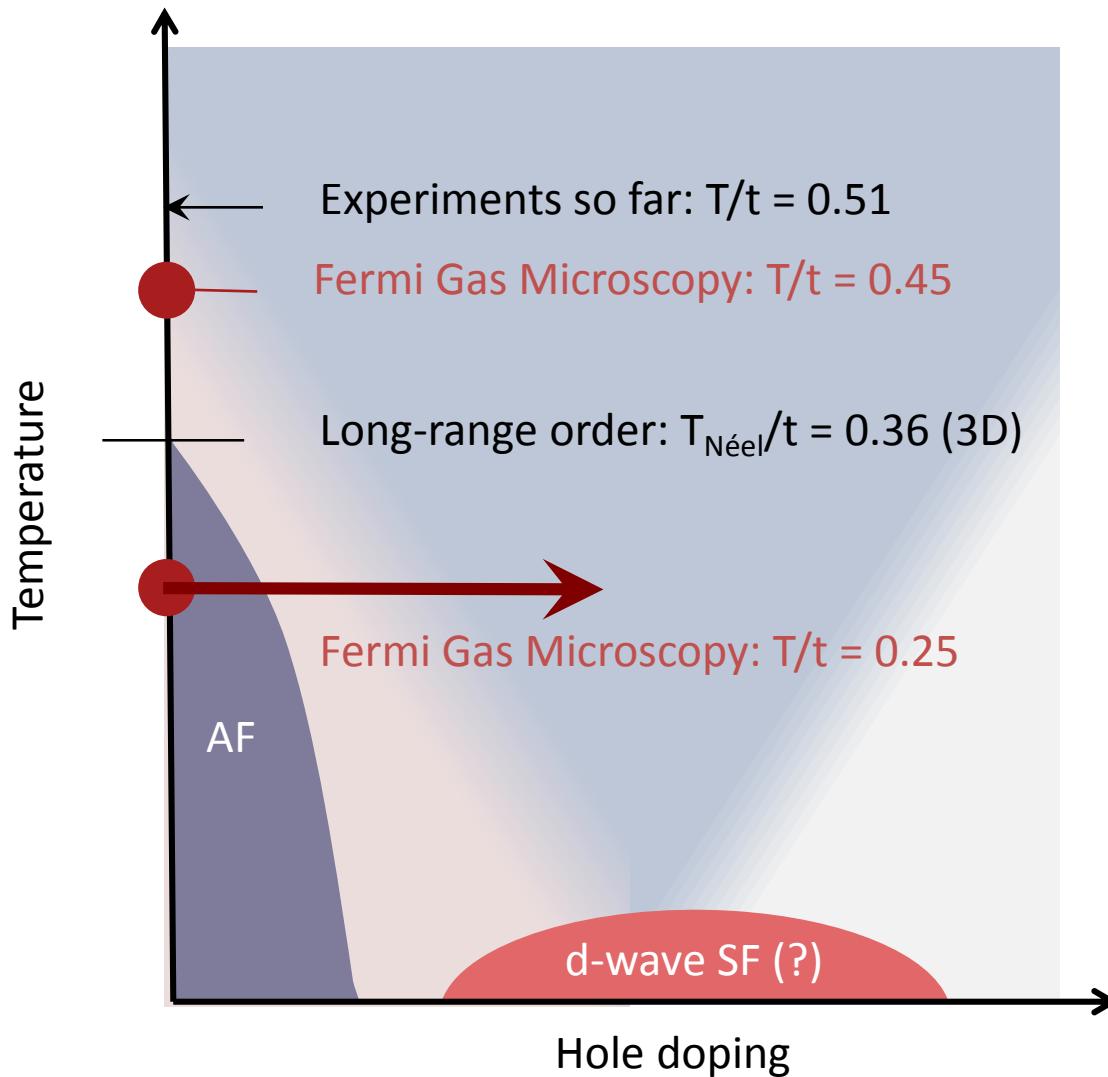
# 2D Antiferromagnetic order



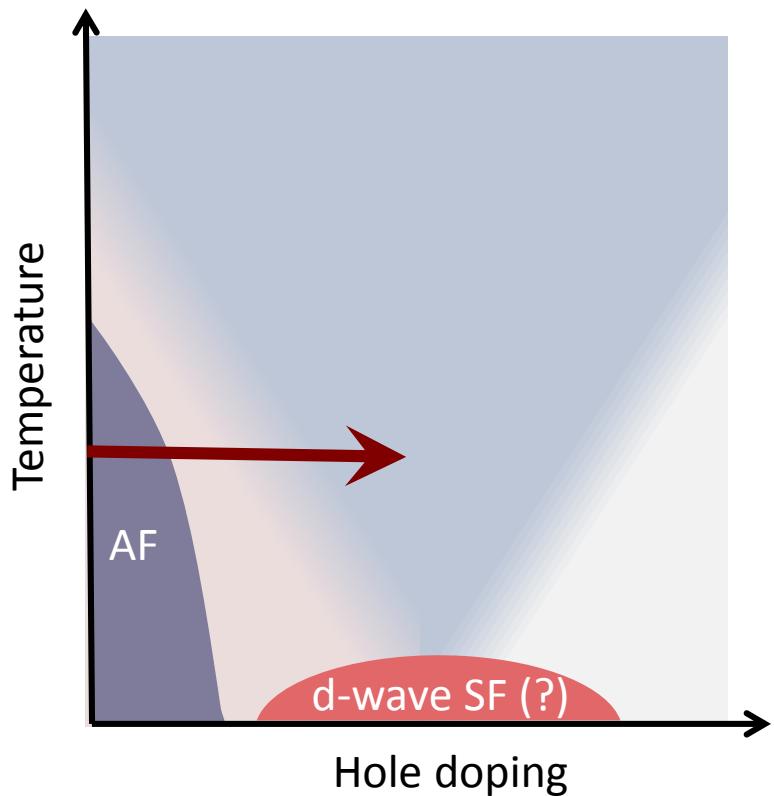
# 2D Antiferromagnetic order



# 2D Antiferromagnetic order

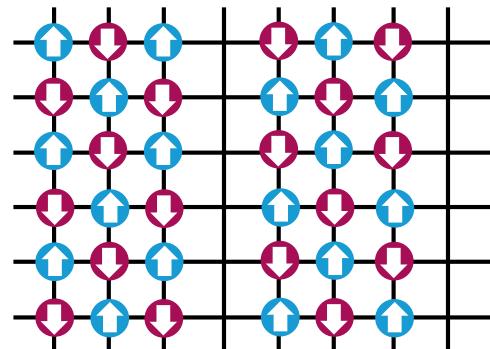


# Doping in the Hubbard model



Candidates:

Stripe Order



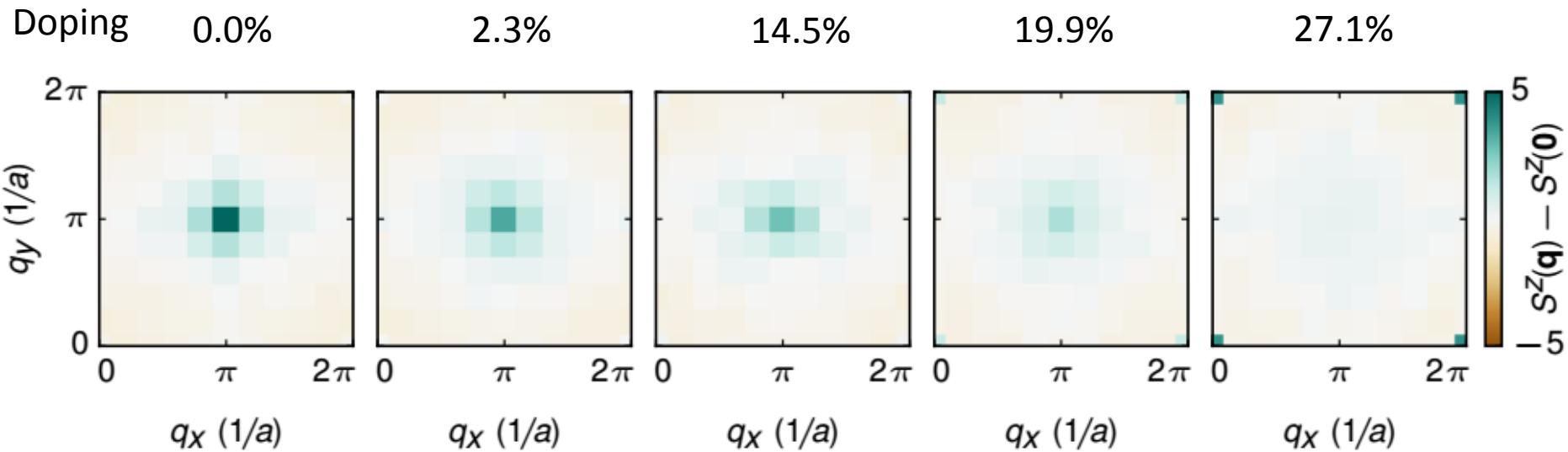
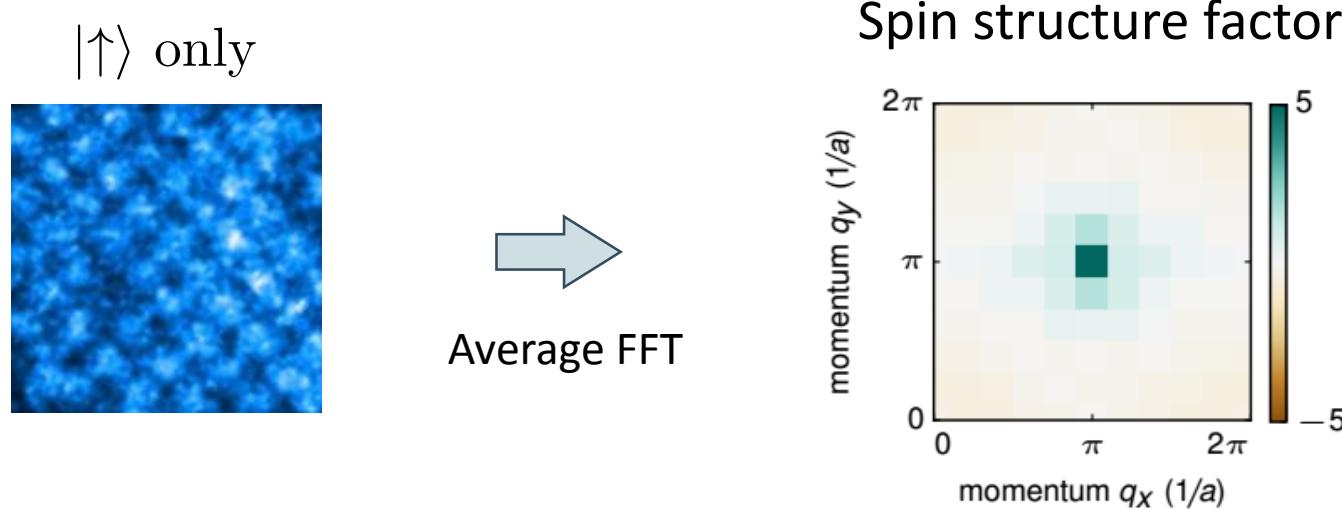
Incommensurate AFM Order



Pseudo-gap states  
Spin liquid

...

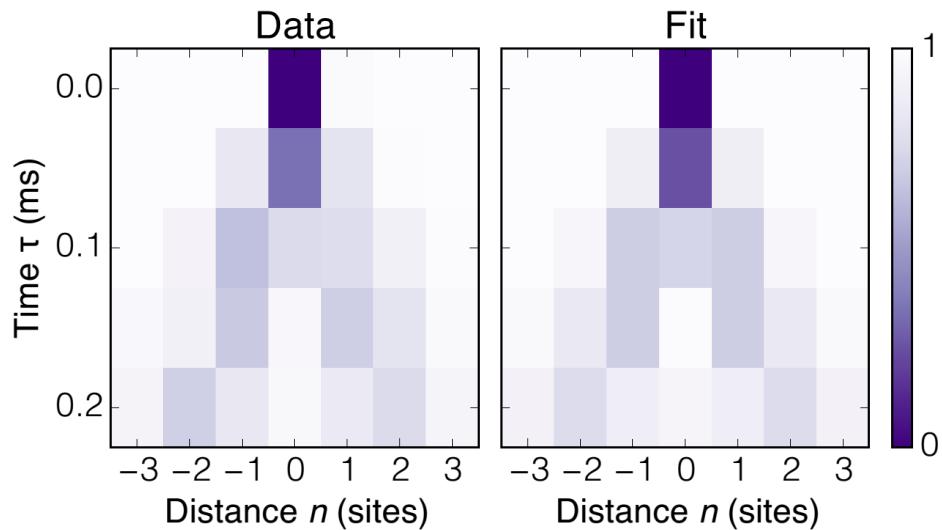
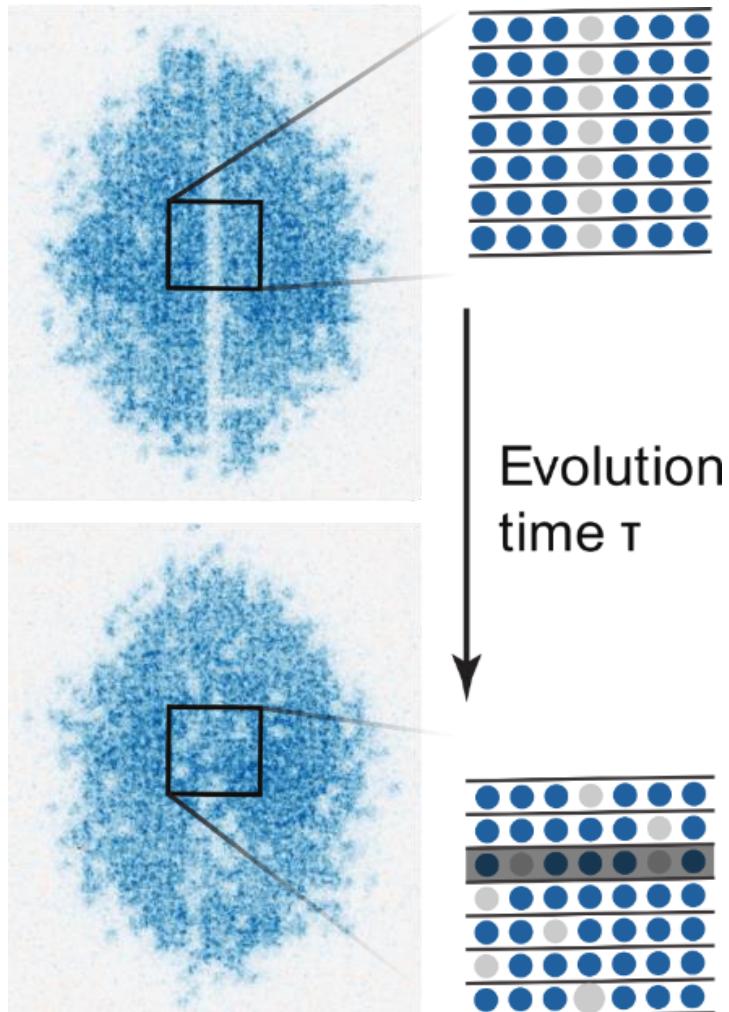
# Doping in the Hubbard model



(preliminary)

# Outlook: hole dynamics

## Single Hole in 1D

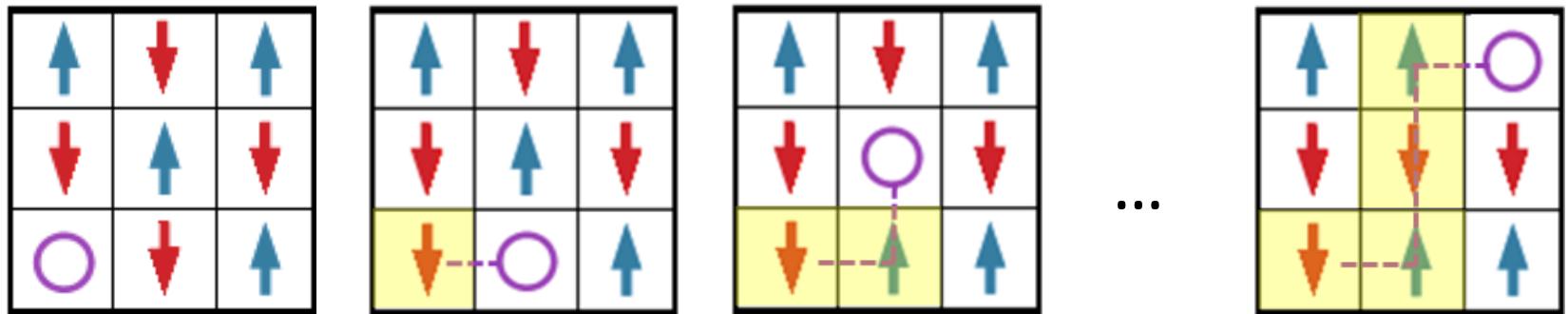


Theory collaboration with Eugene Demler, Fabian Grusdt,  
Annabelle Bohrdt, Marton Kanasz-Nagy, Michael Knap

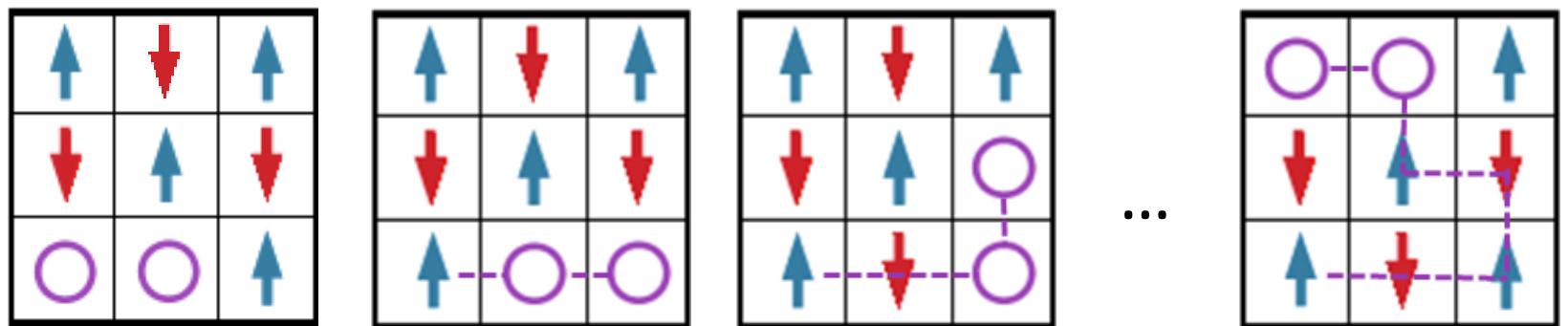
Theory: Carlström et. al. PRL **116**, 247202 (2016)

# Outlook: hole dynamics

Single Hole in 2D, AFM background



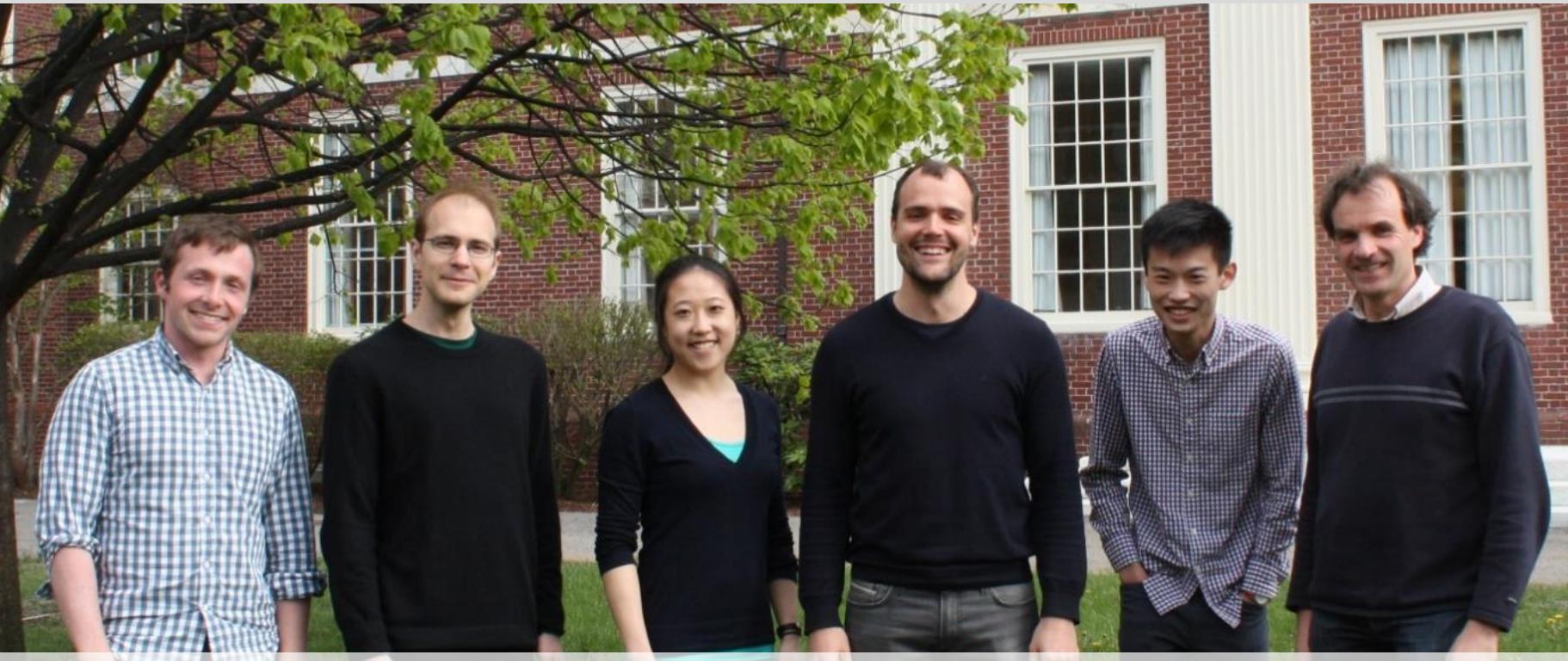
Two Holes in 2D, AFM background



Theory collaboration with Eugene Demler, Fabian Grusdt,  
Annabelle Bohrdt, Marton Kanasz-Nagy, Michael Knap

Theory: Carlström et. al. PRL **116**, 247202 (2016)

# Thank you

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