



Non-uniform and anisotropic dielectric constant of ultrathin Si(001)

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Motivation



➤ Dielectric constant

$$\varepsilon = \varepsilon_0 \varepsilon_r = \varepsilon_0 \begin{bmatrix} \varepsilon_{xx} & \varepsilon_{xy} & \varepsilon_{xz} \\ \varepsilon_{yx} & \varepsilon_{yy} & \varepsilon_{yz} \\ \varepsilon_{zx} & \varepsilon_{zy} & \varepsilon_{zz} \end{bmatrix}$$

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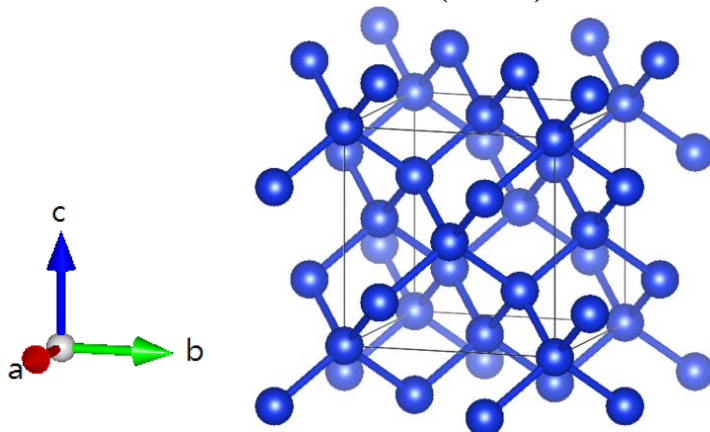
homogeneous and isotropic



Si ($\varepsilon_r \approx 12$)

$$\varepsilon = \varepsilon_0 \varepsilon_r = \varepsilon_0 \varepsilon_r \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Cubic diamond lattice structure
(bulk)



Motivation

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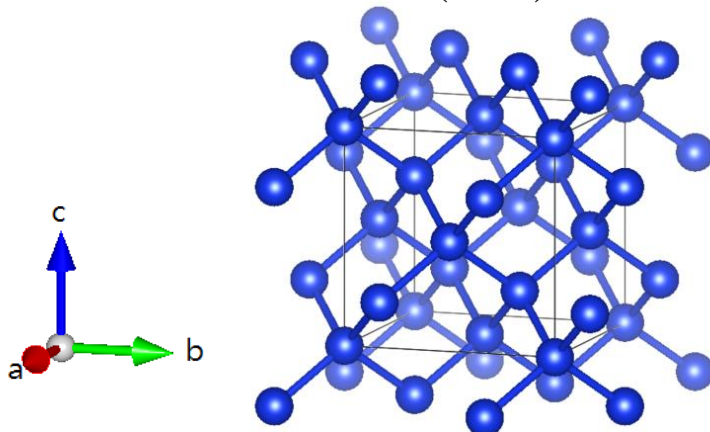
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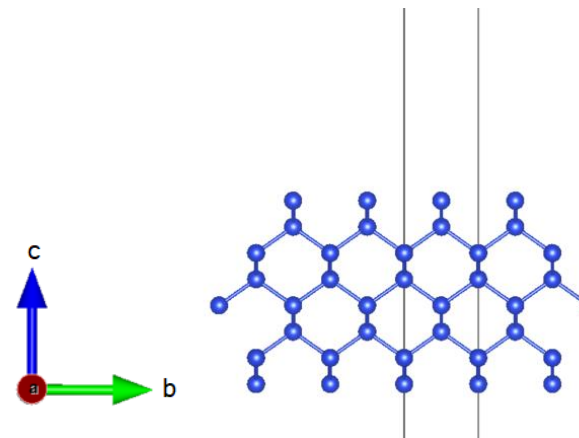
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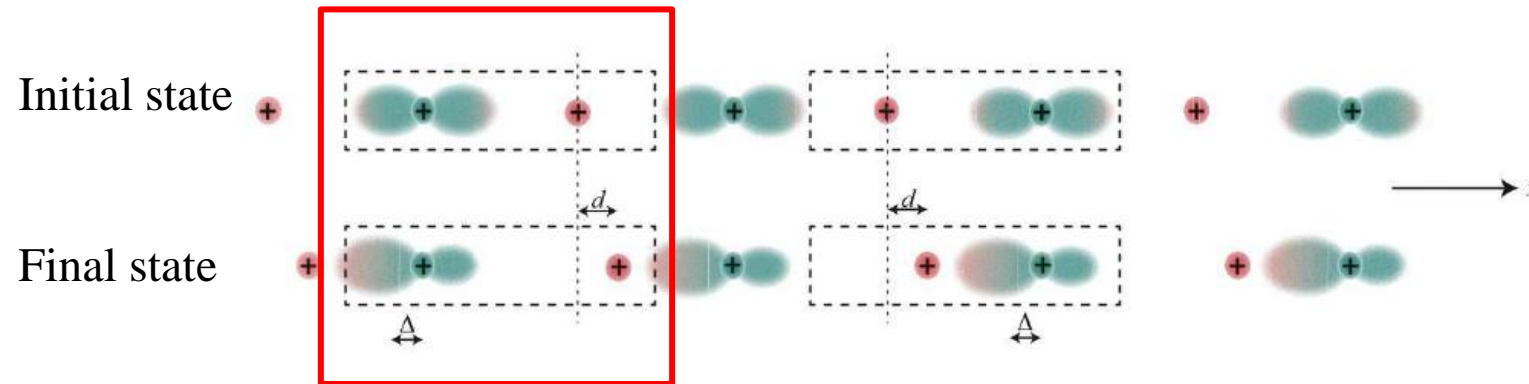
Ultrathin slab



$$\varepsilon_r = \varepsilon_{xx} (= \varepsilon_{yy}) = \varepsilon_{zz} ?$$

Methodology

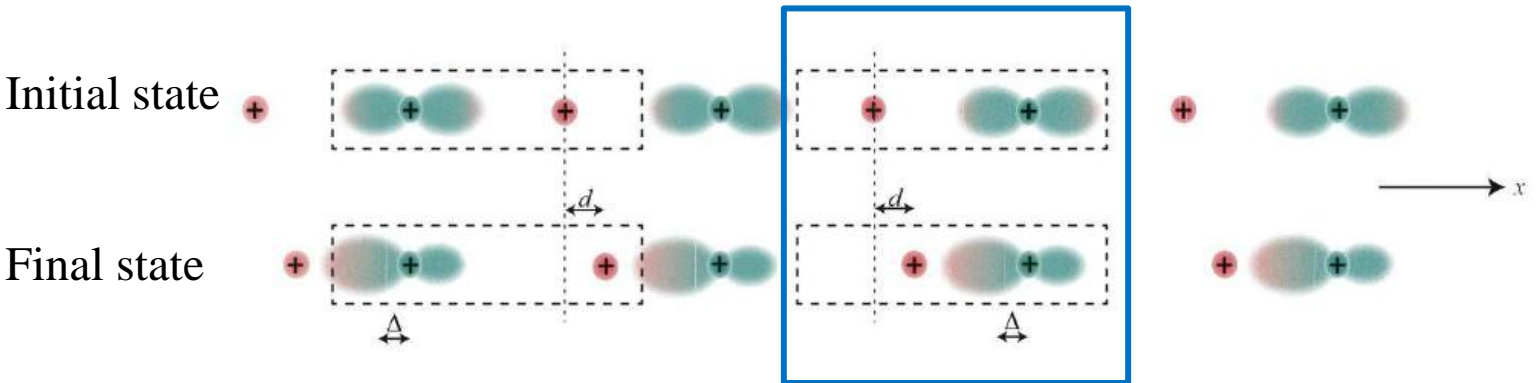
➤ Modern theory of polarization : a well definition in periodic solid



	Red cell	Blue cell
Initial state	$+\frac{1}{2}$	
Final state	$+\frac{1}{2} + dip$	

Methodology

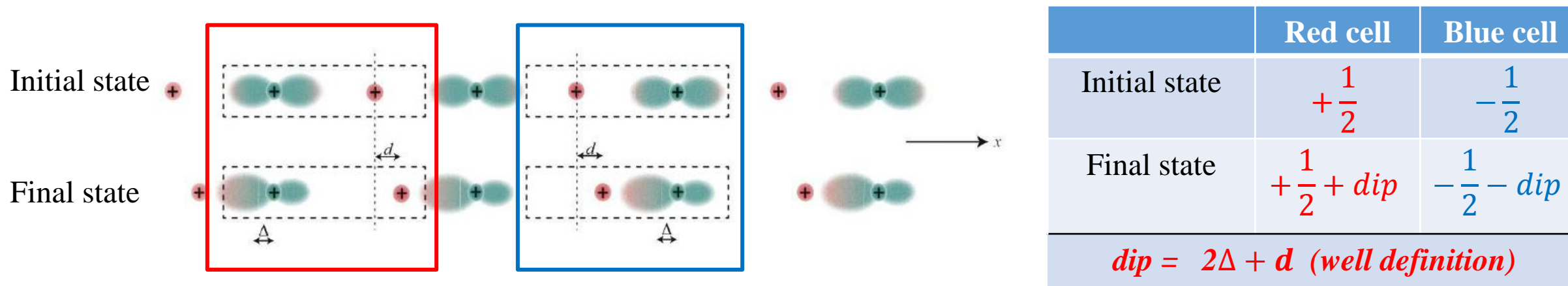
➤ Modern theory of polarization : a well definition in periodic solid



	Red cell	Blue cell
Initial state		$-\frac{1}{2}$
Final state		$-\frac{1}{2} - dip$

Methodology

➤ Modern theory of polarization : a well definition in periodic solid



The polarization of each state is a relative property.

$$\Delta \mathbf{P}_e = \mathbf{P}_e^{(\lambda_2)} - \mathbf{P}_e^{(\lambda_1)}$$

The change in polarization is well definition in periodic solid.

$$\epsilon_{ij} - \delta_{ij} = \frac{4\pi}{\epsilon_0} \frac{\partial P_i}{\partial E_j}; i, j = x, y, z$$

Methodology

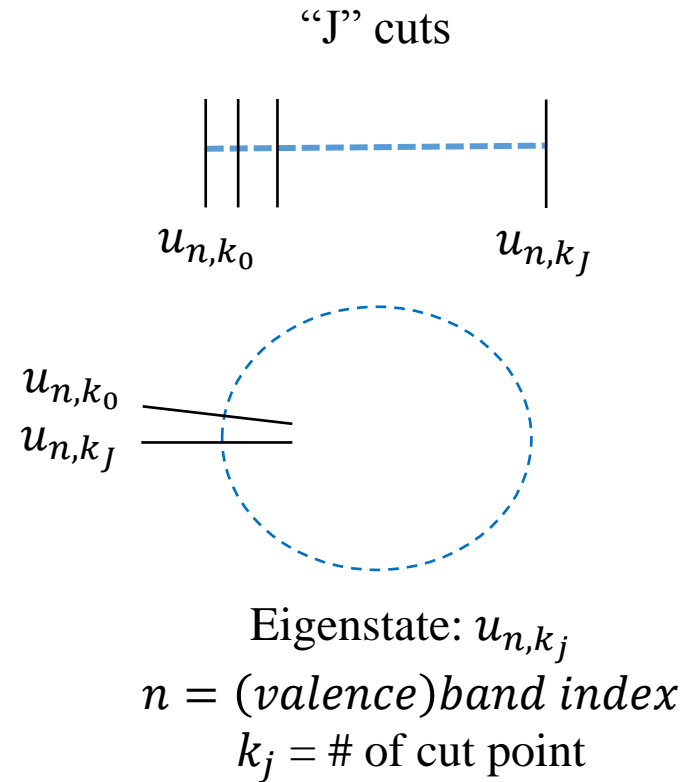
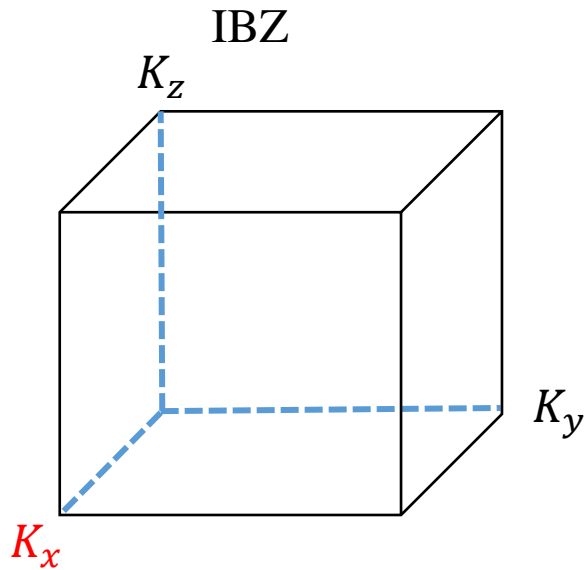
➤ Modern theory of polarization: berry phase method

$$\mathbf{P}_e^{(\lambda)} = -\frac{if|e|}{8\pi^3} \sum_{n=1}^M \int_{BZ} d^3k \langle u_{n\mathbf{k}}^{(\lambda)} | \nabla_{\mathbf{k}} | u_{n\mathbf{k}}^{(\lambda)} \rangle$$

Methodology

➤ Modern theory of polarization: berry phase method

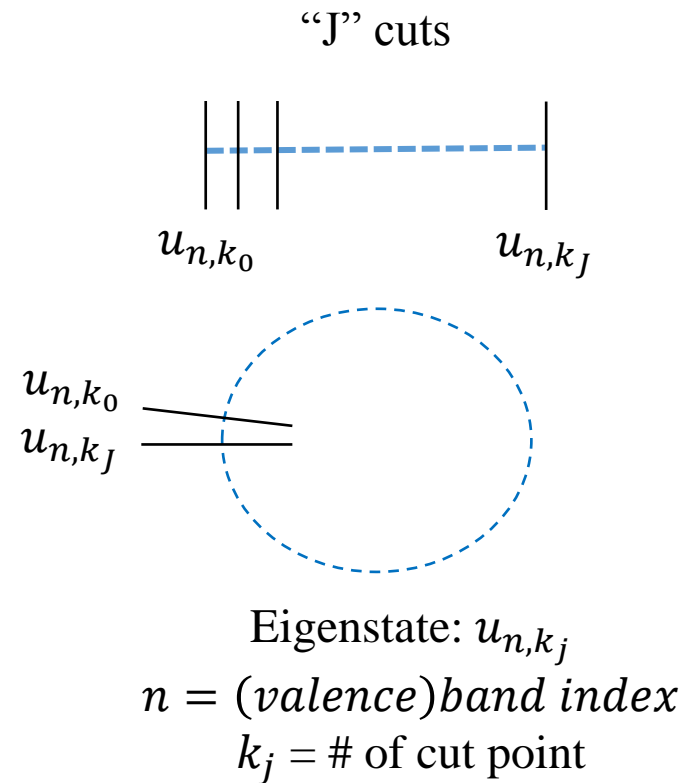
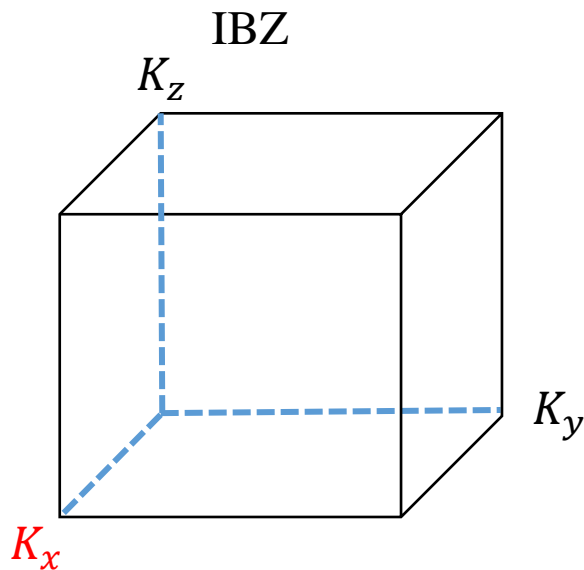
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$$u_{n,k_0}(r) = e^{-i\mathbf{G} \cdot \mathbf{r}} u_{n,k_J}(r)$$

$$\phi_J^{(\lambda)}(\mathbf{k}_{\perp}) = \text{Im} \left\{ \ln \prod_{j=0}^{J-1} \det \left(\langle u_{m\mathbf{k}_j}^{(\lambda)} | u_{n\mathbf{k}_{j+1}}^{(\lambda)} \rangle \right) \right\}$$

**position of electron clouds center
in 2π unit.**

$$(\mathbf{P}_e)_i = \frac{f|e|R_i}{2\pi\Omega_0} \phi_J$$

Methodology

➤ Tool: VASP 5.4.4

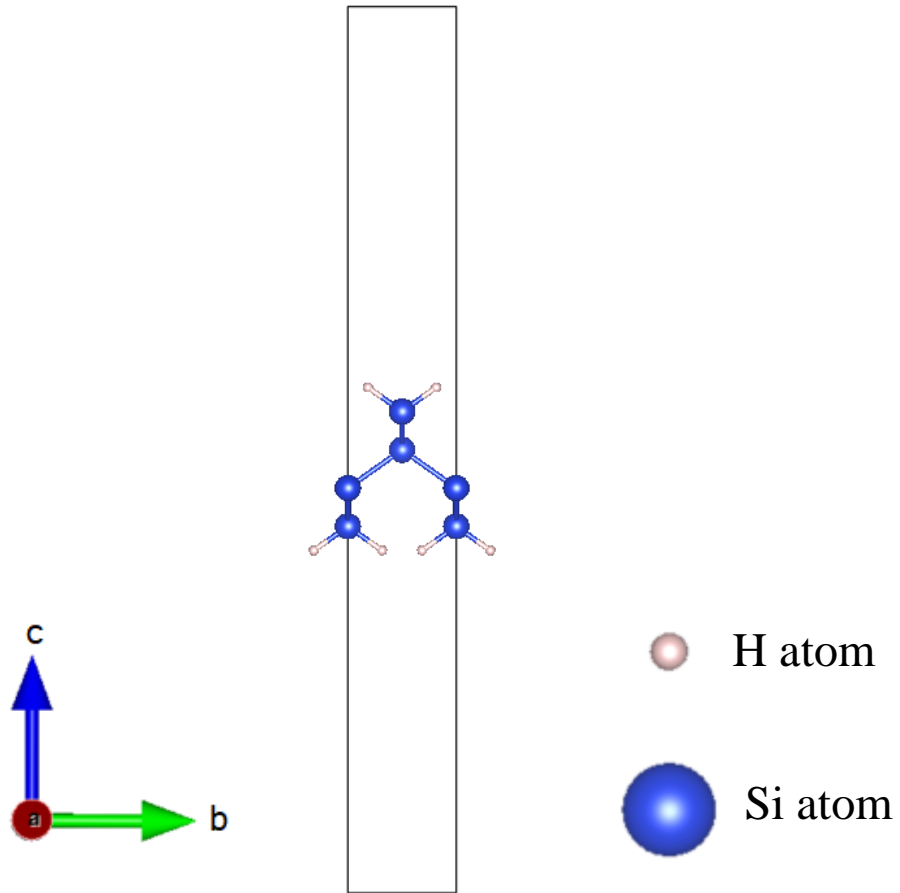


- Generalized gradient approximation(GGA) of the Perdew-Burke-Enzerhof (PBE) form.
- The plane wave cutoff energy is taken as 500 eV.
- $13 \times 13 \times 13$ for bulk($13 \times 13 \times 1$ for slab) Gamma-centered k-mesh.

Methodology



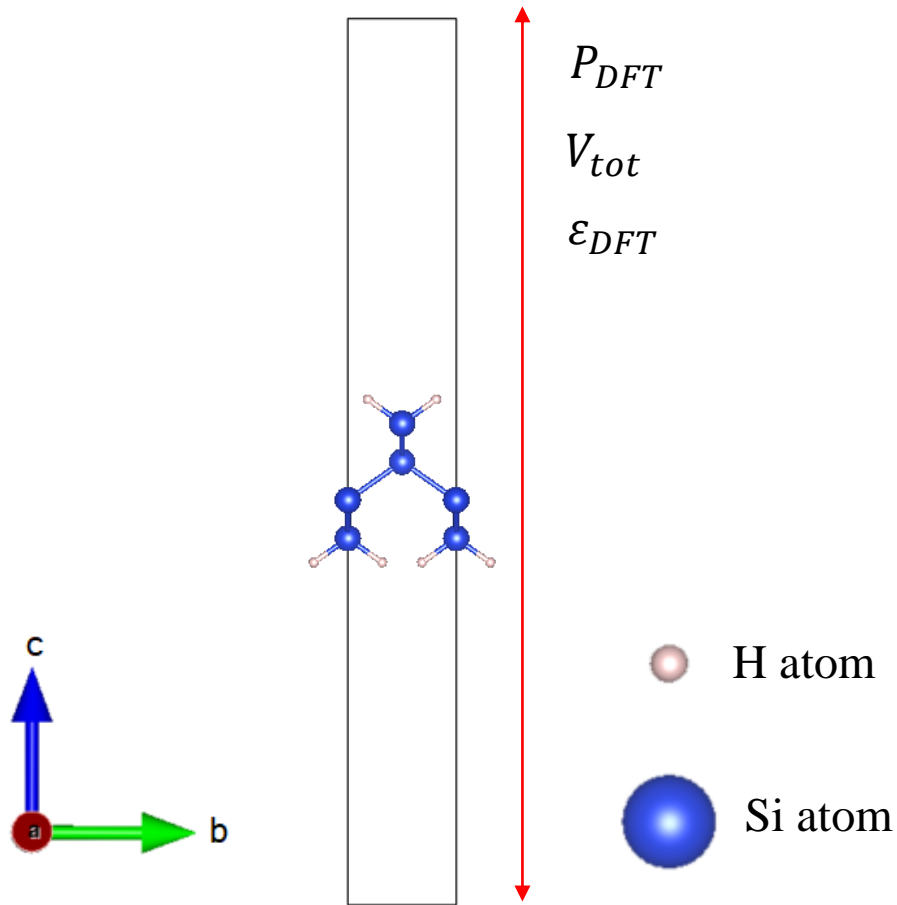
➤ The structure of slab



- Si-H: Eliminate the dangling bond.
- Vacuum: avoid interaction.

Results and discussions

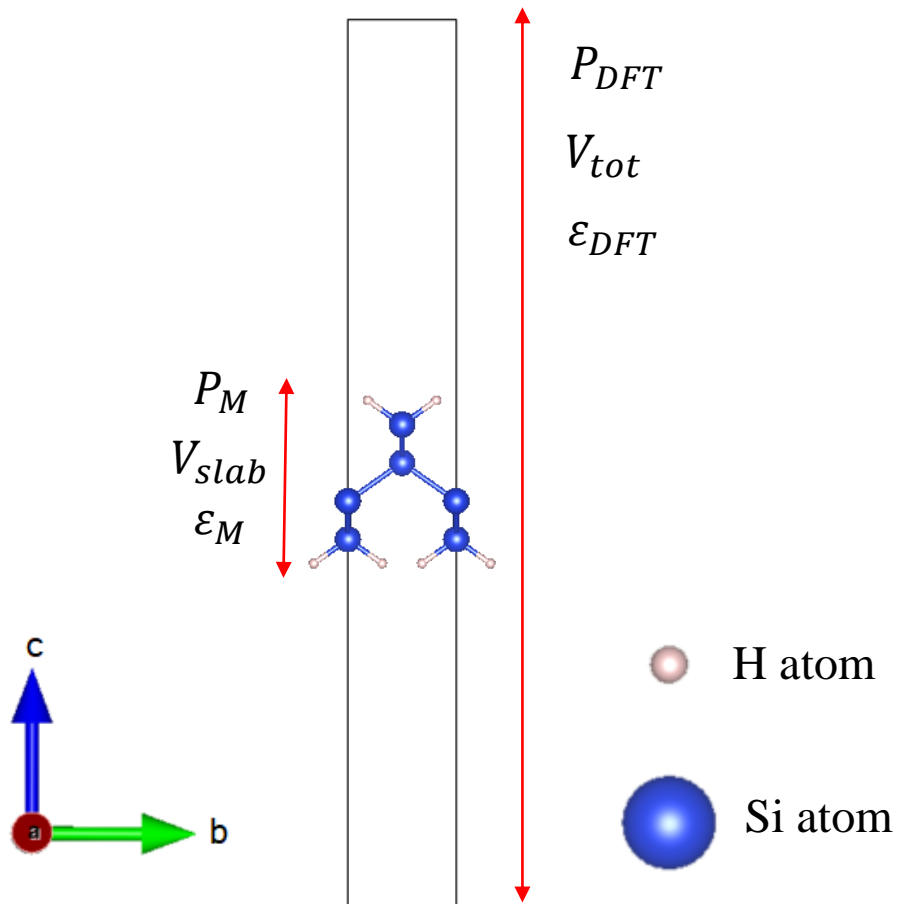
- The result of dielectric constant from DFT by using berry phase method



$$\epsilon_{DFT} - 1 = \frac{4\pi}{\epsilon_0} \frac{\partial P}{\partial E}$$

Results and discussions

- The result of dielectric constant from DFT by using berry phase method



$$\epsilon_{DFT} - 1 = \frac{4\pi}{\epsilon_0} \frac{\partial P}{\partial E}$$

$$P_{DFT} = \frac{V_{tot}}{V_{slab}} \times P_M; \text{ (no contribution from vacuum)}$$



Fitting function:

$$\begin{aligned} (\epsilon_{DFT} - 1) &= \frac{P_{DFT}}{P_M} \times (\epsilon_M - 1) \\ &= \frac{\epsilon_M - 1}{1 + \frac{V_{vacuum}}{V_{slab}}}; \end{aligned}$$

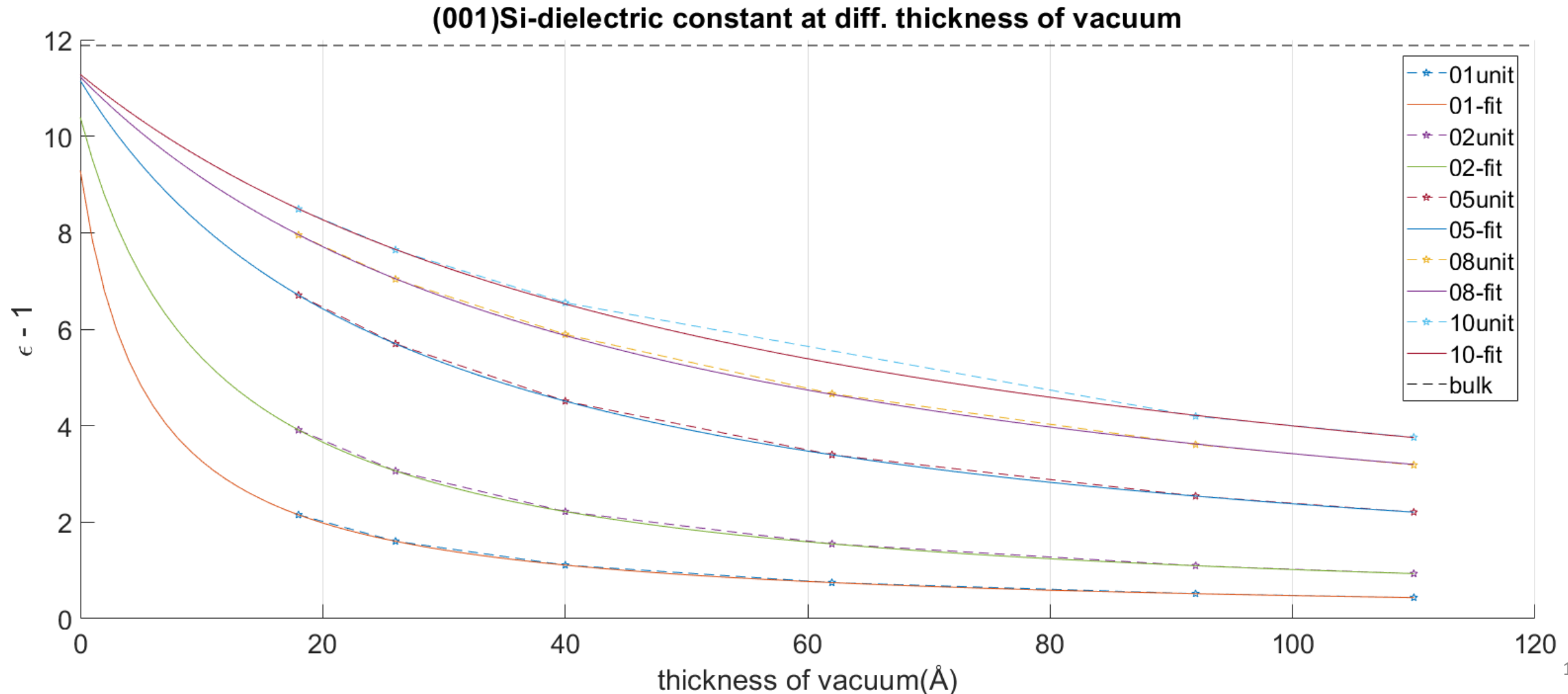
This is what we need.

Results and discussions

➤ The result of dielectric constant $\epsilon_{xx,yy}$

Fitting function:

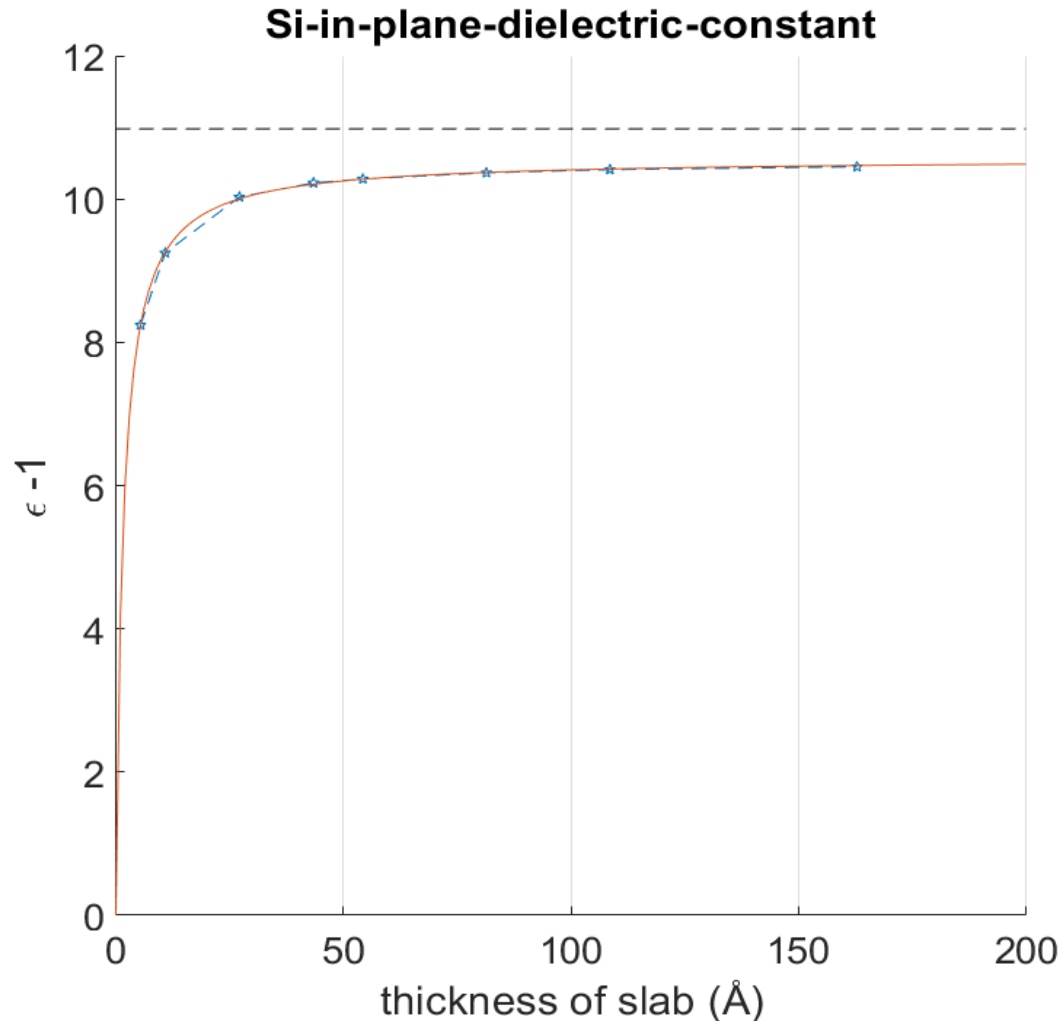
$$(\epsilon_{DFT} - 1) = \frac{\epsilon_M - 1}{1 + \frac{V_{vacuum}}{V_{slab}}}$$



Results and discussions



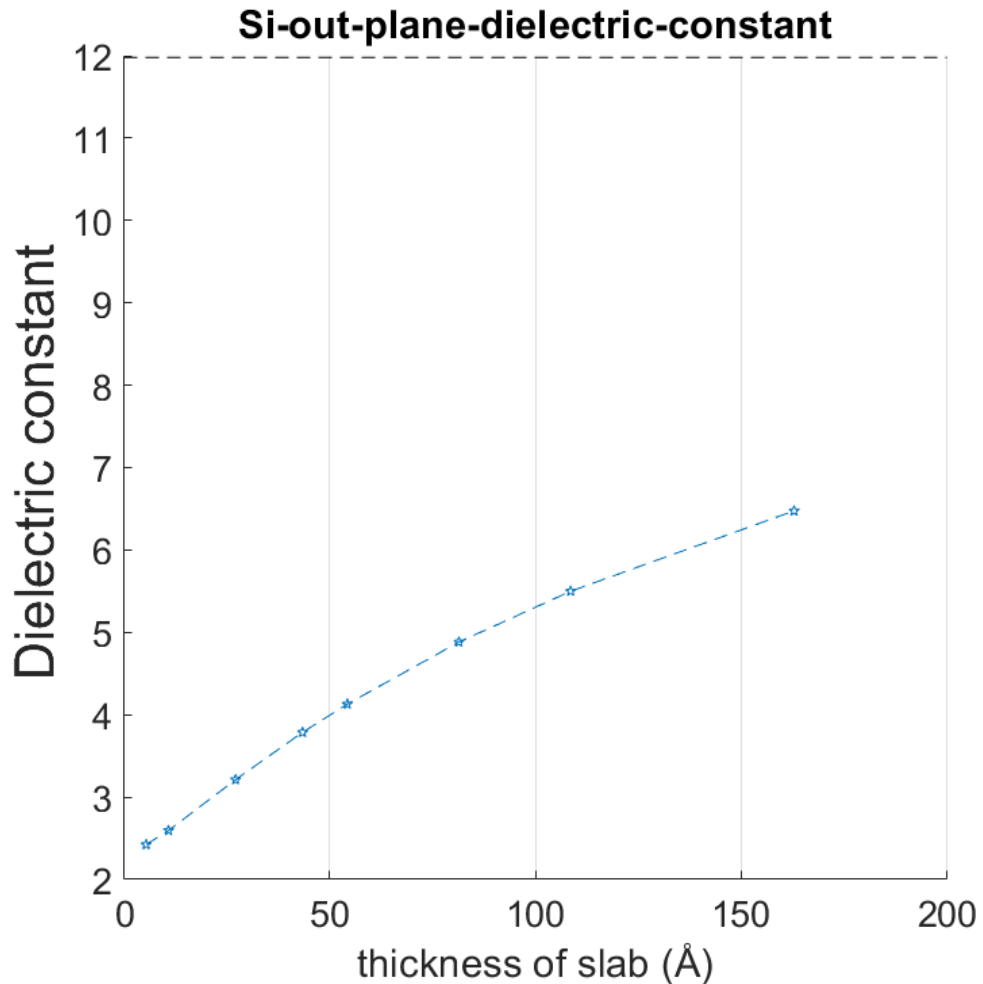
➤ The result of dielectric constant $\epsilon_{xx,yy}$



- Saturation around 50Å of thickness.
- Decrease with thinner thickness.

Results and discussions

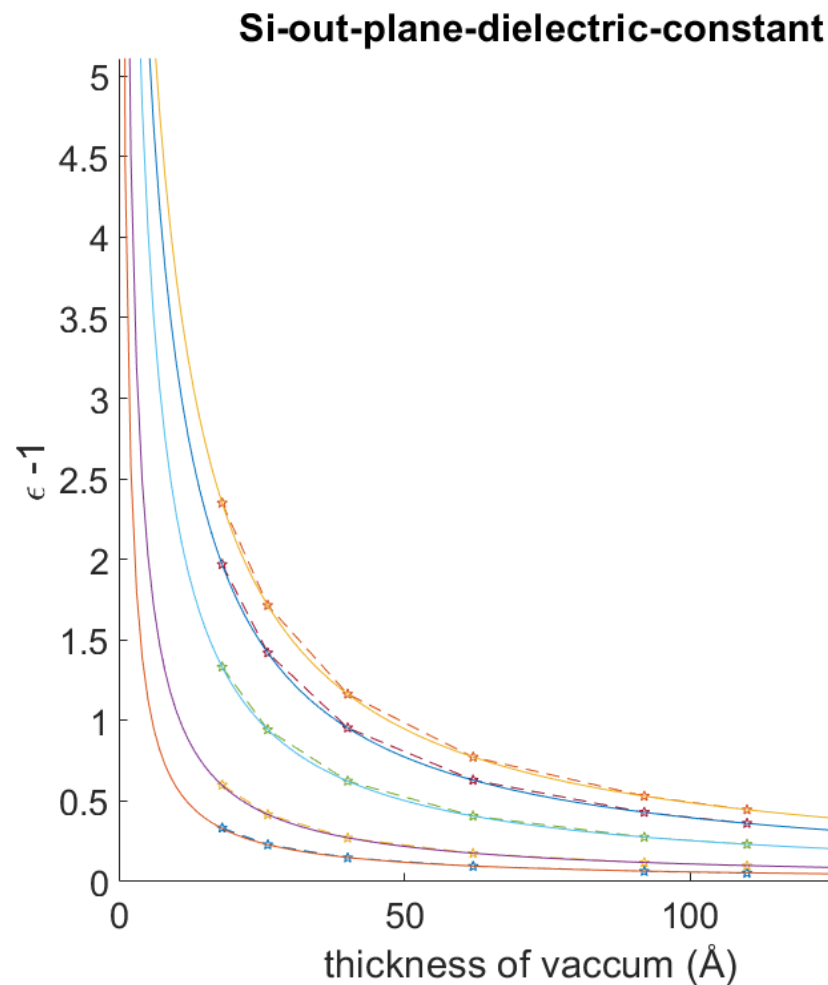
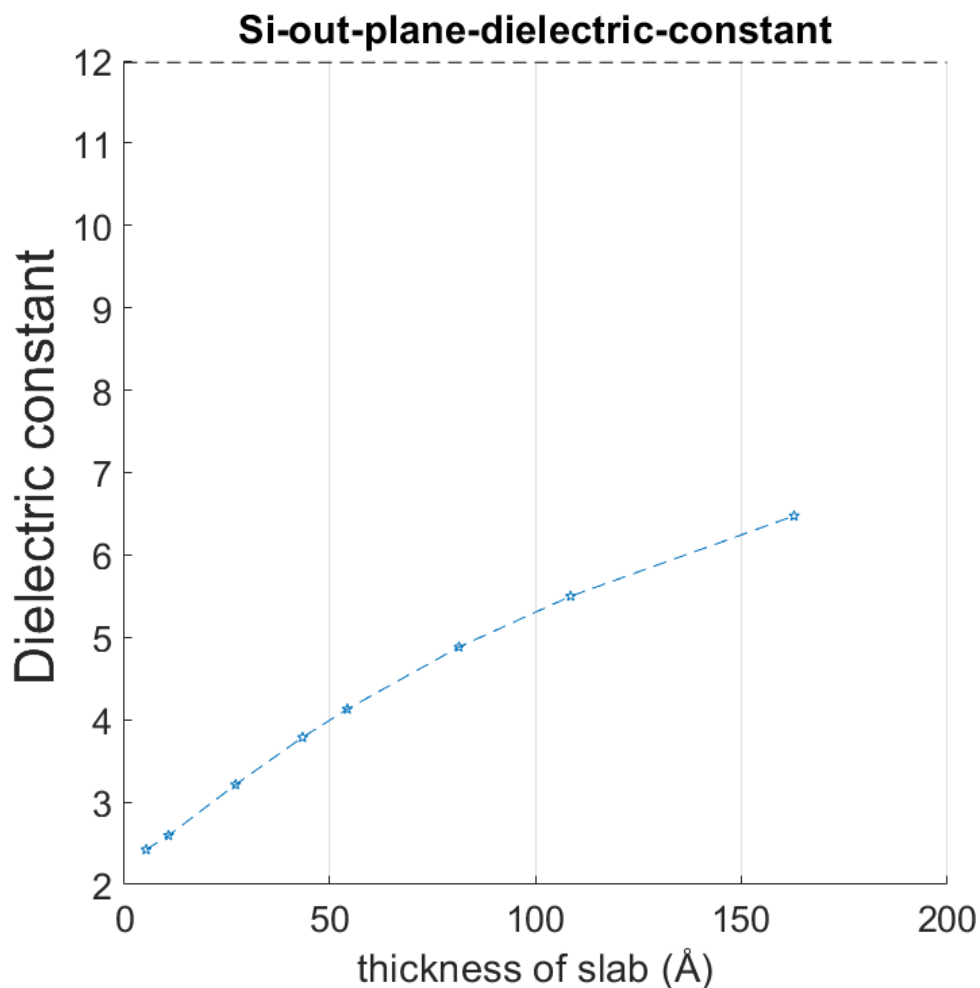
- The result of dielectric constant ϵ_{zz}



Results and discussions



➤ The result of dielectric constant ϵ_{zz}

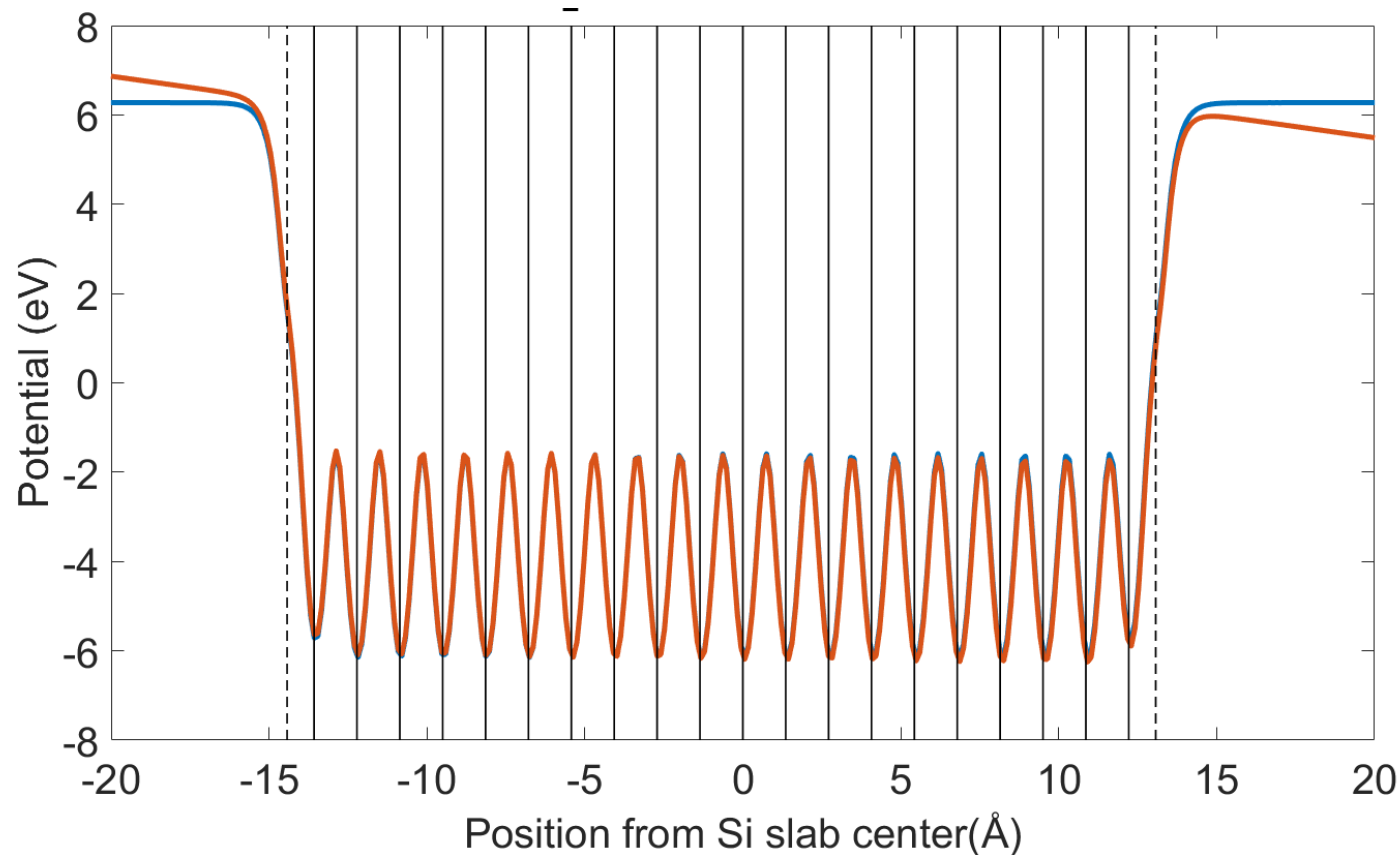
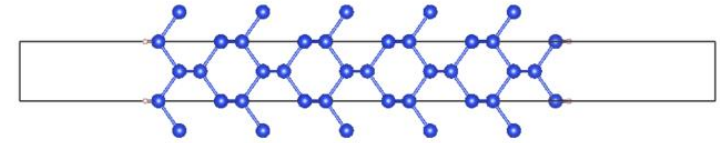
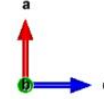


➤ $P_{DFT} \neq \frac{V_{tot}}{V_{slab}} \times P_M ?$

Results and discussions



- The result of dielectric constant ϵ_{zz}



— zero E-field
— external E-field

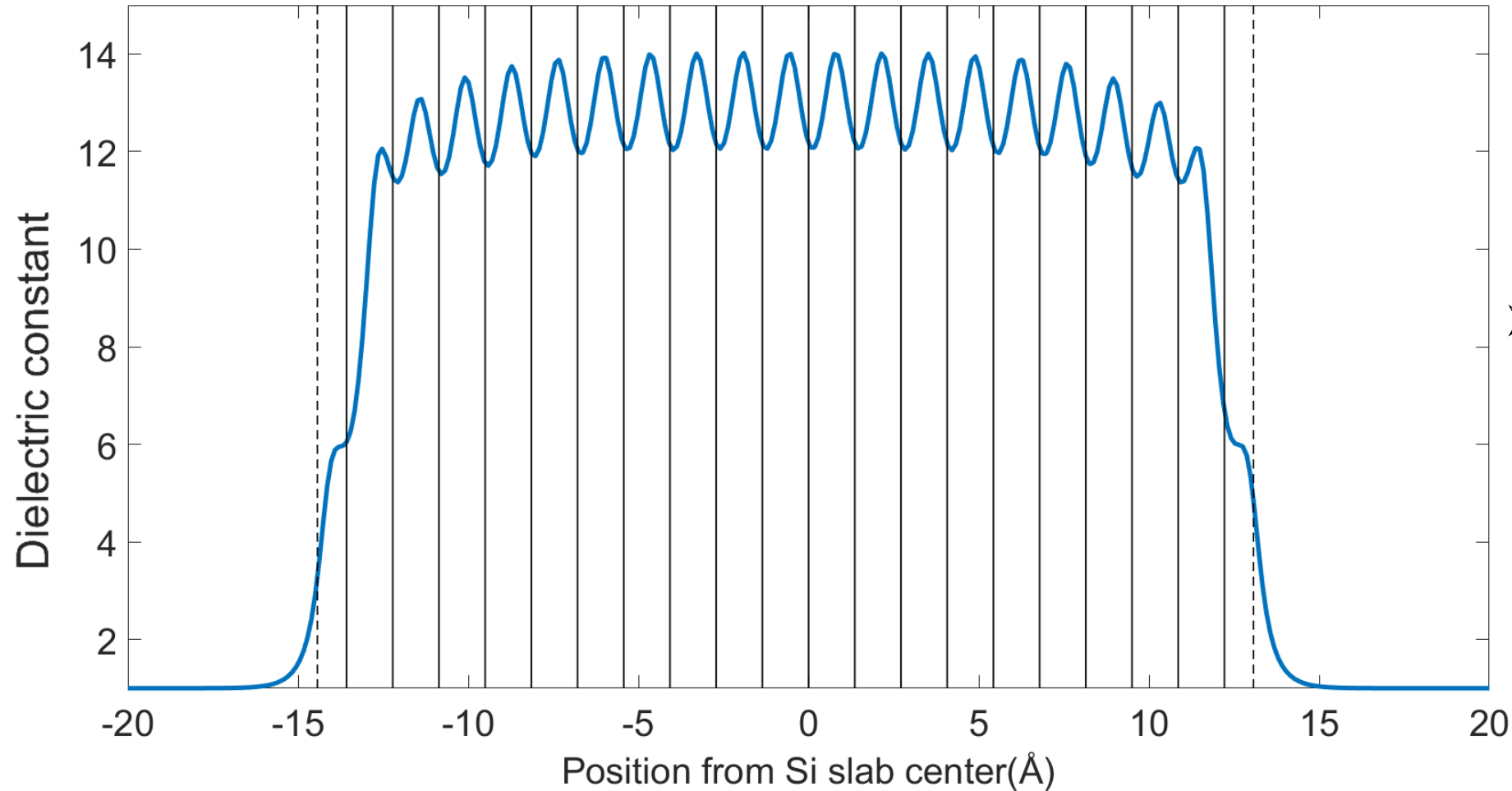
- $$\epsilon(z) = \frac{E_{in}}{E_{ext}} = \frac{\frac{\partial \Delta V_{in}(z)}{\partial z}}{E_{ext}}$$

- This method doesn't be used along in-plane direction.

Results and discussions



➤ The result of dielectric constant ϵ_{zz}

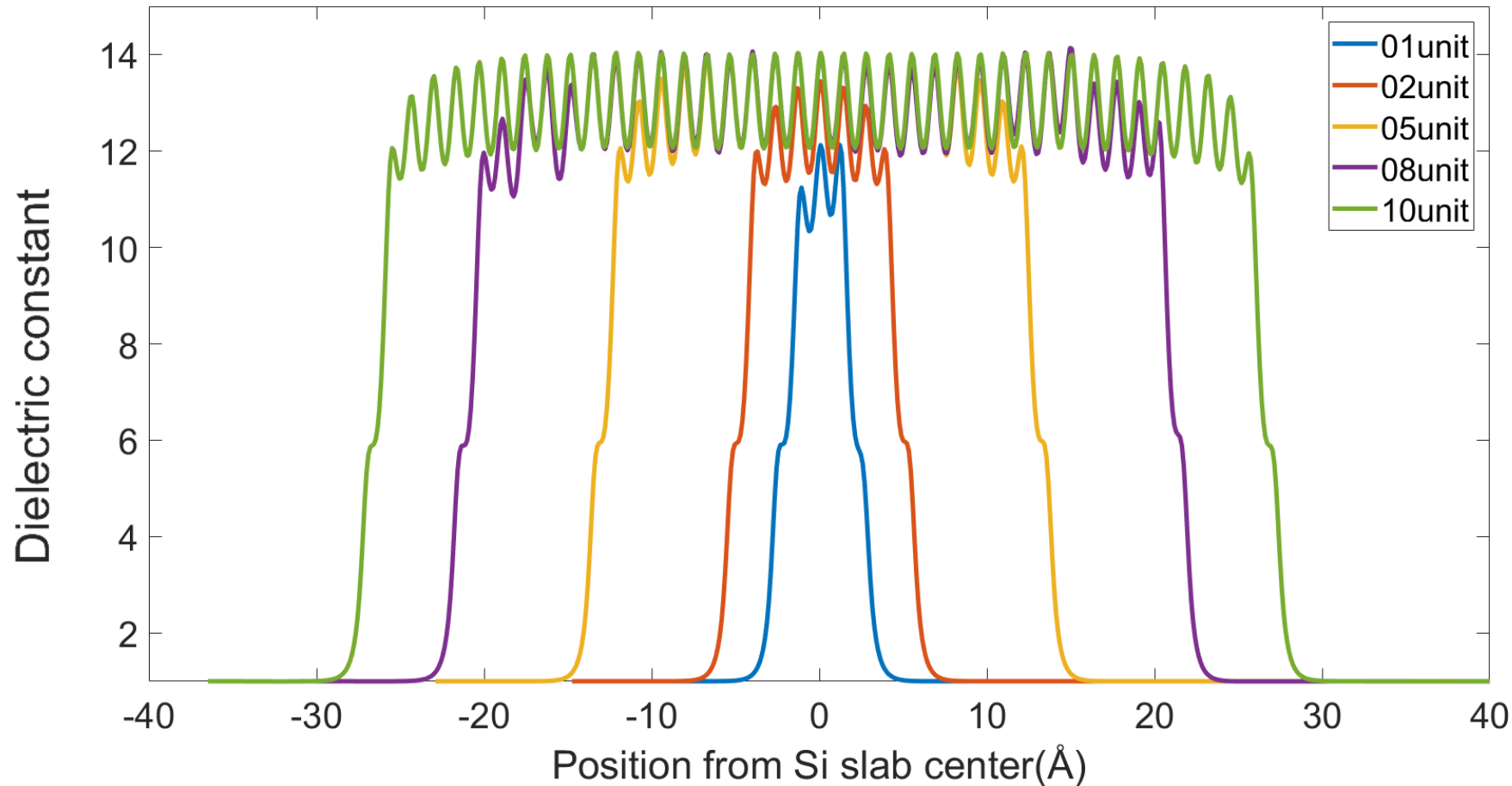


➤ The dielectric constant function of z.

Results and discussions



➤ The result of dielectric constant ϵ_{zz}



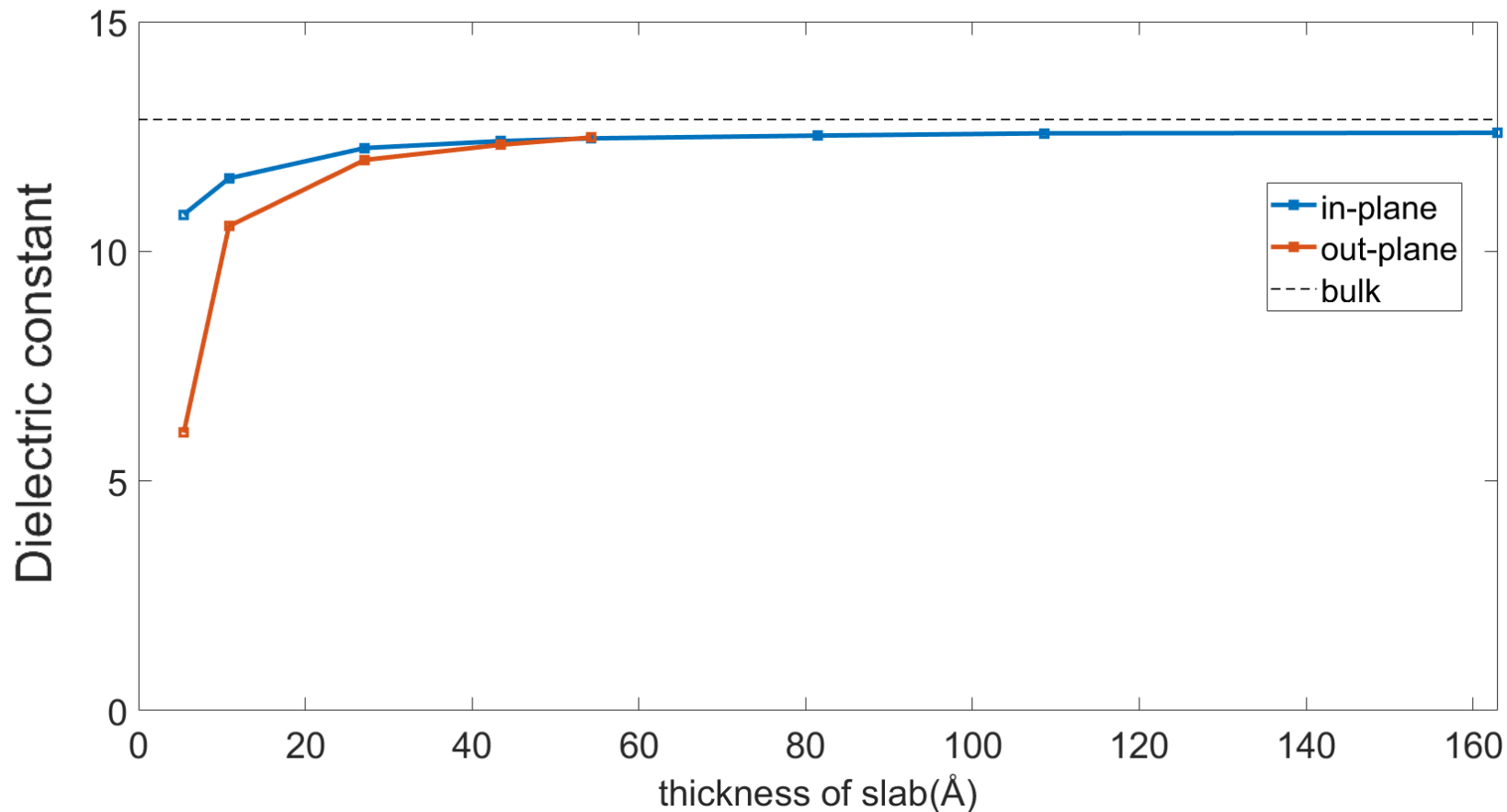
➤ $\epsilon_{zz}(z)$ is non-uniform.

➤ $\langle \epsilon_{zz} \rangle$ decays as thickness of slab decreases.

Results and discussions



- The result of dielectric constant ϵ_{xx} , ϵ_{yy} , ϵ_{zz}



- Anisotropy in ultrathin Si(001).
 - $\epsilon_{xx} = \epsilon_{yy} \neq \epsilon_{zz}$
- Isotropy in Si if the thickness is larger than 50Å .

Summary



- The property of dielectric constant $\epsilon_{zz}(z)$ in edge is smaller than center.
- The average dielectric constant $\epsilon_{xx}(\epsilon_{yy})$, $\langle \epsilon_{zz} \rangle$ decays as thickness of slab decreases.
- The dielectric constant $\epsilon_{xx}(\epsilon_{yy})$, ϵ_{zz} is anisotropy in ultrathin Si(001).
- When the thickness of Si is larger than 50 \AA , the dielectric constant is isotropy and close to bulk.

Summary



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2509

Impact of Semiconductor Permittivity Reduction on Electrical Characteristics of Nanoscale MOSFETs

Si-Hua Chen, Shang-Wei Lian, Tzung Rang Wu, Tay-Rong Chang, Jia-Ming Liou, Darsen D. Lu^{ID},
Kuo-Hsing Kao^{ID}, *Member, IEEE*, Nan-Yow Chen, Wen-Jay Lee^{ID}, and Jyun-Hwei Tsai

Thanks for listening