



First lecture: Precision measurement in atomic physics

Second lecture: Laser spectroscopy of simple atoms

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- Magnetic moment of electron,
 - $g_e(exp) = 2.00231930436146(56)$
- Rydberg constant = $\frac{2\pi^2 m_e e^4}{h^3 c}$ = 109,737.31568639(91)
- Electric dipole moment of electron
 - $|d_{e}| < 8.7 \times 10^{-29} \, e \cdot cm$
- Time variation of fine structure constant

 $\delta \alpha / \alpha = (-1.6 \pm 2.3) \times 10^{-17} / \text{year} \quad \alpha = \frac{e^2}{\hbar c} \approx \frac{1}{137}$

[1] D. Hanneke et al., *Phys. Rev. Lett.* **100**, 120801 (2008) [2] Th. Udem et al., *Phys. Rev. Lett.* **79**, 2646 (1997) [3] The ACME Collaboration, Science 343, 269 (2014) [4] T. Rosenband et al., Science **319**, 1808 (2008)

Classical measurements



• Time, Length, Mass, Charge

- Definition of Unit
- Good Tools















• Cavendish 1798, G = 6.74×10^{-11} • G = $(6.674 \pm 0.001) \times 10^{-11}$, δ G/G ~ 100 ppm



Outline



Historical Review:

- Precision measurement lead to new physics
- Modern approach: resonance and
 - frequency measurement
- Selected topics

Resonance Method



- First Motivated by Stern-Gerlach experiment, 1922
- First atomic spectroscopy by resonance method NMR, Rabi and Ramsey, 1934-1939





Isidor Isaac Rabi



Norman F. Ramsey

Electric Quadrupole Moment



- Electric Quadrupole moment of Deuteron discovered
- Nuclear force is Non-central! Tensor force



J. M. Kellogg, I. I. Rabi, N. F. Ramsey, and J. R. Zacharias Phys. Rev. 57, 677 (1940)

The Lamb Shift









1947 by Lamb ~1060 MHz

Willis Eugene Lamb Nobel Prize in 1955

"for his discoveries concerning the fine structure of the hydrogen spectrum"







Quantum Electrodynamics

The most precisely tested theory



Sin-Ichiro Tomonaga (朝永振一郎), Julian Schwinger, Richard P. Feynman Nobel Prize in Physics 1965

"for their fundamental work in quantum electrodynamics, with deepploughing consequences for the physics of elementary particles"

Selected topics in precision measurement of Physics

- Hyperfine structure: probing nuclear moment
- Test QED: the g-2 of electron and muon
- New source of CP violation: electric dipole moment of electron and nucleon
- Strong interaction: size of proton
- Time and frequency standard: making a better clock
- Constancy of fundamental constant: can speed of light change?

• Nuclear magnetic moment $\bullet F = 1 + J$ • a and b constant spin anti-parallel F=0 spin parallel F=1 magnetic moment anti-parallel magnetic moment parallel $\Delta E_{HFS} = \frac{1}{2}aK + \frac{1}{4}b\frac{\frac{3}{2}K(K+1) - 2I(I+1)J(J+1)}{I(2I-1)J(2J-1)}$ $3^2 P_{3/2}$ 60.9 MHz F = 2K = F(F+1) - J(J+1) - I(I+1) $3^2 P_{1/2}$ 192 MHz 36.6 MHz F = 1589.6 nm (D₁) 589.0 nm (D₂) 1772 MHz

Hyperfine structure

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 $0.4 - 6s^2 S_{1/2}(F=3) \rightarrow 6p^2 P_{3/2}(F=2,3,4)$ O Data - Fit

Observe magnetic octupole moment of ¹³³Cs

V. Gerginov, A. Derevianko, and C. E. Tanner, PRL 91, 072501 (2003)

$$1^{133}\text{Cs 6p}^{2}\text{P}_{3/2}$$

$$H_{\text{dipole}} = aI \cdot J, \quad H_{\text{quadrupole}} = b\frac{3(I \cdot J)^{2} + \frac{3}{2}(I \cdot J) - I(I + 1)J(J + 1)}{2I(2I - 1)J(2J - 1)}, \quad \int_{0}^{4} \int_{0}^{4}$$



 Observe magnetic octupole moment of ⁸⁷Rb from spectroscopy of hyperfine intervals V Gerginov, C E Tanner, W R Johnson, Can. J. Phys., 87(1): 101-104 (2009)

Large deformation for some heavy nuclei

Comparison to nuclear shell model



Hyperfine anomaly





Blue points: Grossman et al., PRL **83**, 935–938 (1999) Red points: new measurements at TRIUMF (error as of May 30, 2013) Dashed line: magnetization radius = charge radius, normalized to ²¹¹Fr ²¹³Fr ground state: Duong, et al. Europhys. Lett., **3**(2), 175-182 (1987) ²⁰⁶Fr ground state: Voss, et al. To be published.

Measure hyperfine constant of isotopes
Magnetic radius ≠ electric radius

Hydrogen HFS





HFS and Zemach moment





g-2 of electron



What is g-factor? The magnetic moment of the electron is proportional to the electron spin

$$\frac{\left|\overline{\mu}\right|}{\mu_{B}} = g \cdot \frac{\left|\overline{s}\right|}{\hbar}$$

Classical non-relativistic g=1

 $m_{s} = +\frac{1}{2}$

• In QM, Dirac Theory predict g=2In reality, g= 2.002319304

QED and g factor





and a lot more....



Test QED

- Search for structure of electrons
- g can be expanded as a function of $\boldsymbol{\alpha}$

$$\frac{g}{2} = 1 + C_2 \left(\frac{\alpha}{\pi}\right) + C_4 \left(\frac{\alpha}{\pi}\right)^2 + C_6 \left(\frac{\alpha}{\pi}\right)^3 + \dots$$

$$+a_{\mu\tau}+a_{hadronic}+a_{weak}$$

$$\alpha = \frac{e^2}{\hbar c} \approx \frac{1}{137}$$

 $\alpha^{-1} = 137.035\ 999\ 074\ (44)$

D. Hanneke, S. Fogwell, and G. Gabrielse, PRL 100, 120801 (2008)

Measure electron in bound system



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Spin precession (Larmor) frequency

$$\hbar \omega_L = m_s g \cdot \mu_B \cdot B$$
 $\mu_B = \frac{e\hbar}{2m}$

Calibration of magnetic field by cyclotron frequency:

$$\hbar\omega_c = \frac{q}{M}B$$

$$g = 2\frac{\omega_L}{\omega_C} \frac{q}{e} \frac{m}{M} = 2\frac{\omega_L}{\omega_C}$$

Measurement performed on a single electron in Penning trap





g-2 experiment of electron and muon:

 $g_e(exp) = 2.00231930436146(56)$ $g_e(th)$ to determine fundamental constant

 g_{μ} (exp) = 2.0023318416(12)* g_{μ} (th) = 2.0023318367(13)* $\int \sigma deviation$

Size of proton



- Fundamental quantity bothering for decades
- Very important for nuclear calculation
- Lattice QCD not able to calculate precisely

Charge radius of proton by electron scattering

$$\left(\frac{d\sigma}{d\Omega}\right)_{Rosenbluth} = \left(\frac{d\sigma}{d\Omega}\right)_{Mott} \left\{ \left(\frac{G_{E}^{2}(Q^{2}) + \frac{Q^{2}}{4M^{2}}G_{M}^{2}(Q^{2})}{1 + \frac{Q^{2}}{4M^{2}}}\right) + \frac{Q^{2}}{2M^{2}} \cdot G_{M}^{2}(Q^{2}) \cdot \tan^{2}(\theta/2) \right\}$$
$$< r_{c}^{2} > = -6\frac{dG_{E}(Q^{2})}{dQ^{2}}\Big|_{Q^{2}=0}$$

Simon et al, (1980) R_{rms} = 0.862(12) fm
I. Sick, (2003). R_{rms} = 0.895(18) fm

Nuclear size effect





→ decrease transition frequency



- Measure H transition frequency 1s →2s at 121 nm, uncertainty: (th) 16 kHz, (exp) 22 kHz
- \rightarrow charge radius of proton R_{rms} = 0.883(14) fm Lack of precision (only1~2%) very annoying!

Kirill Melnikov and Timo van Ritbergen, Phys. Rev. Lett. 84, 1673(2000)



$$E(nS) \approx \frac{-R_{\infty}}{n^2} + \frac{L_{1S}}{n^3} \qquad L_{1S} = (8172 + 1.56 \cdot r_p^2)MHz$$

• Two unknowns: R_{∞} and r_p

0.883(14) fm, hydrogen spectroscopy, ENS Paris
C. Schwob et al., Phys. Rev. Lett. 82, 4960 (1999).
K. Melnikov and T. van Ritbergen, Phys. Rev. Lett. 84, 1673(2000).
0.890(14) fm, hydrogen spectroscopy, MPI Garching
T. Udem et al. Phys. Rev. Lett. 79, 2646, (1997).

0.862(12) fm, original electron scattering result
G.G. Simon et.al. Nucl. Phys. A 333, 381 (1980)
0.895(18) fm, re-analysis of world data
I. Sick, Phys. Lett. B 576, 62-67 (2003)
0.879(8) fm, new experiment by GSI
J. C. Bernauer et al., Phys. Rev. Lett. 105, 242001 (2010)

Optical frequency measurement

Precision Spectroscopy of Atomic Hydrogen 23

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Fig. 4. The first 1992 Garching frequency chain for the measurement of the 1S - 2S transition in atomic hydrogen (Φ : phase-locked loop, SHG: second harmonic generation)

Frequency chain

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Figure 5. The PTB harmonic frequency chain was the first to achieve a phase-coherent connection between the caesium primary standard and an optical-frequency reference in the visible range. In this case, the target was the calcium optical frequency standard at 457 THz (657 nm). (Adapted with permission from [96].)

Muonic atom result





$$m_{\mu}/m_{e} \sim 200$$
Bohr radius
$$a_{0} = \frac{4 \pi \varepsilon_{0} \hbar^{2}}{m_{e} e^{2}}$$
Energy level $E_{n} = -\frac{e^{4}}{2(4\pi\varepsilon_{0}\hbar)^{2}} \frac{m_{e}}{n^{2}}$
Wave function
$$\Psi(r) \sim a_{0}^{-3/2} e^{-r/a_{0}}$$
Energy shift due to nuclear size $|\Psi(0)|^{2} \langle r^{2} \rangle$
Sensitivity $\sim (m_{\mu}/m_{e})^{2}$

 $r_{\rm p} = 0.84184(67) \, {\rm fm}$ Pohl et al., Nature 466, 213, 2010 $r_{\rm p} = 0.84087(39) \, {\rm fm}$ Antognini et al., Science 339, 417, 2013

Need more experimental verification of atomic QED calculations



Frequency standard





Figure: S.A. Diddams et al., Science 306, 1318, 2004

Why better clock?



- When you measure something very precisely, new physics will come out by itself!
- Applications:
 - GPS
 - Test special relativity, gravitational red-shift
 - Gravitational wave radiation in binary pulsar
 - Test linearality of quantum mechanics
 - Variation of fundamental constant

Microwave Cs clock





Optical Atomic Clock



• Frequency comb: pioneering work by T.W. Hänsch and J. Hall made frequency measurement possible





Trapped ions: Hg⁺, Ca⁺, Sr⁺, Yb⁺, Ba⁺, In⁺, Al⁺.....
 Long interaction time, can be laser cooled
 Single ion detection, poor S/N

 Trapped neutral atoms: Ca, Sr, Yb, Mg, H..... Large number of atoms, very high S/N Complicated systematics

• Precision ~ $10^{-17} - 10^{-18}$ (Hz^{1/2})

Permanent electric dipole moment

 1957 Landau first pointed out the electric dipole moment (EDM) of a fundamental particle would suggest P and T violation



d: electric dipole moment

- = vector
- u: spin or magnetic moment

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= pseudo-vector, (like r x p)

Neutron EDM: history




CP violation without strangeness



 Matter–antimatter asymmetry suggest another source of CP violation • Electron: intrinsic ? •Quark: intrinsic ? Neutron/proton: from quark EDM ? New interaction? Atoms, molecules: large enhancement factors

> Atoms: TI, Cs, Hg, Xe, Rn, Ra, Fr Molecule: PbO, YbF, ThO Ions, solid state systems, etc...



Problem: reverse E field cause leakage current, huge noise from B field

Current status

-10 5

0.0

0.2







Typical value E ~ 10 kV/cm ω~ 10Hz, $\delta ω$ ~ nHz

Sensitivity approaching some Standard Model extension

What if someone observes EDM? Theories ready with many parameters

figure from M. Romalis, Princeton

Time (sec)

0.4

0.6

1.0

0.8



Second lecture:

Laser spectroscopy of simple atoms

work performed at NTHU Physics



Atomic spectroscopy



Precision spectroscopy of simple atoms
Hydrogen: exact solution exist
Helium: numerical method
Lithium: numerical method

Remain as input for atomic calculation
Magnetic moment of nucleus
Charge radius of nucleus



- Calculable atomic structure: precision measurement test fundamental physics
- <u>Advances in atomic theories</u>, e.g. in H, He, Li, He⁺, Li⁺, Be⁺ etc...
- New experimental techniques, e.g.: cold atoms by atom and ion trap, frequency comb, exotic atoms, etc...
- What fundamental physics to study?

Atomic structure (Hydrogen)



 $En = -\alpha^2 mc^2 \left(\frac{1}{2n^2}\right) = \frac{-13.6eV}{n^2}$ • non-relativistic $-\alpha^4 mc^2 \frac{1}{4n^2} \left| \frac{2n}{(l+1/2)} - \frac{3}{2} \right|$ • relativistic correction spin-orbit interaction $-\alpha^4 mc^2 \frac{1}{4n^2} \left| \frac{2n}{(i+1/2)} - \frac{3}{2} \right|$ (L·S, fine structure) • nuclear moment (HFS) $\left(\frac{m}{m_{\pi}}\right)\alpha^4 mc^2 \frac{4\gamma_p}{3n^2} \left[f(f+1) - 3/2\right]$ $\alpha^{5}mc^{2}\frac{1}{4n^{3}}\left\{k(n,l)\pm\frac{1}{\pi(i+1/2)(l+1/2)}\right\}$ QED effect (Lamb shift) $\frac{2\pi}{2} Ze^2 |\psi(0)|^2 \langle r^2 \rangle_{proton}$ • nuclear size effect

Muonic atom result







 $r_{\rm p} = 0.84184(67) \, {\rm fm}$ Pohl et al., Nature 466, 213, 2010 $r_{\rm p} = 0.84087(39) \, {\rm fm}$ Antognini et al., Science 339, 417, 2013

Need more experimental verification of atomic QED calculations









Reference:

[1] Kirill Melnikov and Timo van Ritbergen, Phys. Rev. Lett. 84, 1673(2000)
[2] A. Huber, Th. Udem, B. Gross, J. Reichert, M. Kourogi, K. Pachucki, M. Weitz, and T.W. Hänsch. Phys. Rev. Lett. 80, 468 (1998)

Precision of Theory



Total transition frequency (optical):

- QED effects
- H: ~10 kHz, He: ~1 MHz, Li: > 10 MHz
- Isotope shift:
- Nuclear charge radius
- H: ~1 kHz, He: ~1 kHz, Li: ~10 kHz
- Fine and hyperfine structure :
- State mixing, find hyperfine constant
- H: <1 kHz, He: <1 kHz, Li: several kHz







This method widely used in H-D, ⁴He-³He, and ⁶Li-⁷Li and determine the difference in the nuclear size



- Isotope shift: different velocity may cause systematic effect
- FS and HFS in one isotope: almost immune to beam alignment



Spectroscopy of lithium D lines at NTHU







lodine spectrometer



• Frequency modulation transfer saturation spectroscopy





Absolute frequency measurement



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	$Measured^a$	Calculated	Measured – Calculated
a_1	446,806,191,890(25)	446,806,194,569	-2,679
a_{10}	$446,\!806,\!778,\!950(35)$	446,806,781,526	-2,576
a_{15}	$446,\!807,\!072,\!638(24)$	446,807,075,266	-2,628
$a_{15} - a_1$	880,748(35)	880,697	51(35)
$a_{15} - a_{10}$	$293,\!688(42)$	293,740	-52(42)
$a_{10} - a_1$	587,060(43)	586,957	103(43)

Y.-C. Huang et al., Appl. Opt. 52, 1448-1452 (2013)

Experimental setup





Typical signal for lithium-7





Laser power dependence





- AC Stark effect from other levels
- Photon momentum \rightarrow cooling or heating
- Optical pumping

DEPARTMENT OF PHYSICS **Results** National Tsing Hua University Yerokhin [6] Yerokhin [6] Puchalski [7] Puchalski [7] Orth [8] Orth [8] Walls [1] Walls [1] Noble [2] Noble [2] Das [4] Das [4] Singh [9] Sansonetti [5] Sansonetti [5] This work Huang [10] This work 25.9 26.0 26.1 26.3 26.4 26.2 91.7 91.8 92.2 91.9 92.0 92.1 ⁶Li 2P_{1/2} Hyperfine splitting (MHz) ⁷Li 2P_{1/2} Hyperfine splitting (MHz) Sansonetti [11] Scherf [12] H-V-I Walls [1] Noble [2] Das [4] Sansonetti [5] This work 10,533 10,535 10,534 10,536 10,532 D₁ isotope shift (MHz)

Results for charge radius



• IS, HFS in D1 of Li-6,7 measured

D ₁ IS (MHz)	Reference	Year
10 533.800(8)	This work	2013
10 533.763(9)	Sansonetti	2011
10 534.215(39)	Das	2007
10 534.039(70)	Noble	2006
10 533.160(68)	Bushaw	2003
10 534.26(13)	Walls	2003
10 533.13(15)	Scherf	1996

Y.-C. Huang et al., J. Phys. B: At. Mol. Opt. Phys. 46, 075004 (2013)

Error Budgets



Course	⁷ Li		⁶ Li		Instana shift
Source	$2S_{1/2}$	$2P_{1/2}$	$2S_{1/2}$	$2P_{1/2}$	isotope smit
statistical	12	8	13	8	10
Reference laser instability	16	-	13	-	21
Laser power variation	1	0.5	1	0.5	1.5
First-order Doppler effect	2	<1	<1	<1	20
Zeeman shift	<1	<1	<1	<1	<1
Total	20	8	18	8	31



Helium spectroscopy





Motivation



Better theory

- Experiments mostly performed in triplet state
- Singlet-triplet forbidden transition probed

R. van Rooij et al., Science 333, 196 (2011)





Direct Absorption Spectrum







Direct Absorption Spectrum Department of Physics National Tsing Hua University



Saturated Absorption Spectrum



3000



Simulation of Saturated Absorption Spectrativersity

Without Pump
$$I(v) = I_0 \times Exp[-\kappa \times z]$$

$$\kappa = n_0 h v \alpha_0 \times \sqrt{\frac{m}{2\pi kT}} \times Exp\left[-\frac{mc^2(v-v_0)^2}{2kTv_0^2}\right] \times \frac{c}{v_0} \times \frac{\pi\Gamma_0}{2}$$
With Pump
$$I(v)' = I_0 \times Exp[-\kappa' \times z]$$

$$\kappa' = n_0 h v \alpha_0 \times \sqrt{\frac{m}{2\pi kT}} \times Exp\left[-\frac{mc^2(v-v_0)^2}{2kTv_0^2}\right] \times \frac{c}{v_0} \times F(v-v_0)$$

Amplitude Modulation Transfer Signal

$$S_{AMT} = A_0 (Exp[-\kappa' \times z] - Exp[-\kappa \times z])$$

Simulation





Simulation of Saturated Absorption Spectrativersity

$$S'_{AMT} = A_0 \left(Exp[-\kappa' \times z] - Exp[-\kappa \times z] \right) + B_0 \left(Exp[4\ln 2\frac{(\nu - \nu_0)^2}{\delta_G^2}] \right)$$

Velocity-Changing Collision



Spectroscopic results





P.-L. Luo et al., Phys. Rev. Lett. 111, 013002 (2013)

• First absolute frequency measurement on this transition

• 10 time more precise in isotope shift

Helium spectroscopy





668 nm transition



ECDL at 668 nm locked to frequency comb

• Comb \rightarrow PPLN, change rep rate



Results





10 time more precise than previous measurement
lonization energy





f - 960332041.019 (MHz)

P.-L. Luo et al., Phys. Rev. A 88, 054501 (2013)





Reported in Physics Focus

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PHYSICS FOCUS

Precision Laser Spectroscopy of Helium Testing QED Atomic Calculations

Helium is the simplest multi-electron atom and has been the best testing ground for many-body QED atomic calculations. Unlike the hydrogen atom, for which analytical solutions exists, similar studies of helium requires extensive numerical calculations in order to determine its electronic structures. Precision laser spectroscopy of He can improve the theoretical value of Lamb shift and be used to determine the nuclear charge radii of helium.

Recently, researchers from a multi-

had to control precisely many experimental parameters, e.g., laser power stability, magnetic field shielding, discharge condition, and helium gas pressure. Otherwise, any systematic error will limit the final precision of the measurement. A typical spectrum is shown in Fig. 2. This represents the first Doppler-free measurement of the $2^{1}S_{0} \rightarrow 2^{1}P_{1}$ transition.

For the ionization energy of the $2^{1}P_{1}$ state, a discrepancy of 3.5σ with the most precise theoretical value is found. This is shown in Fig. 3. This



Fig. 1: Schematic of the experimental setup. OFC: optical frequency comb; PD: photodetector; HSPD: high-speed photodetector; AOM: acousto-optical modulator.



EIT



EIT in the He 2^1S_0 - 2^1P_1 - 3^1D_2 Transition



Experimental Setup





Observation of EIT Signal in ⁴He





Ladder-Type EIT in an RF Discharge







Work completed

- Lithium HFS, IS in D1 line
- Helium singlet 2S-2P, 2P-3D states
- Either resolve discrepancy or test theories

Work in progress and future work

- Lithium 2S-3P measurement at 323 nm
- EIT study of helium 2S-2P and 2P-3D transition
- Helium 2S-3D two photon transition at 1009 nm
- Lithium ion spectroscopy

People involved



清華大學物理系:施宙聰老師,羅佩凌,黃耀欽,官鈺禪, 郭彦廷,王淳汝,蕭伃真 工研院量測中心:彭錦龍博士 成功大學光電所:崔祥辰老師

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