

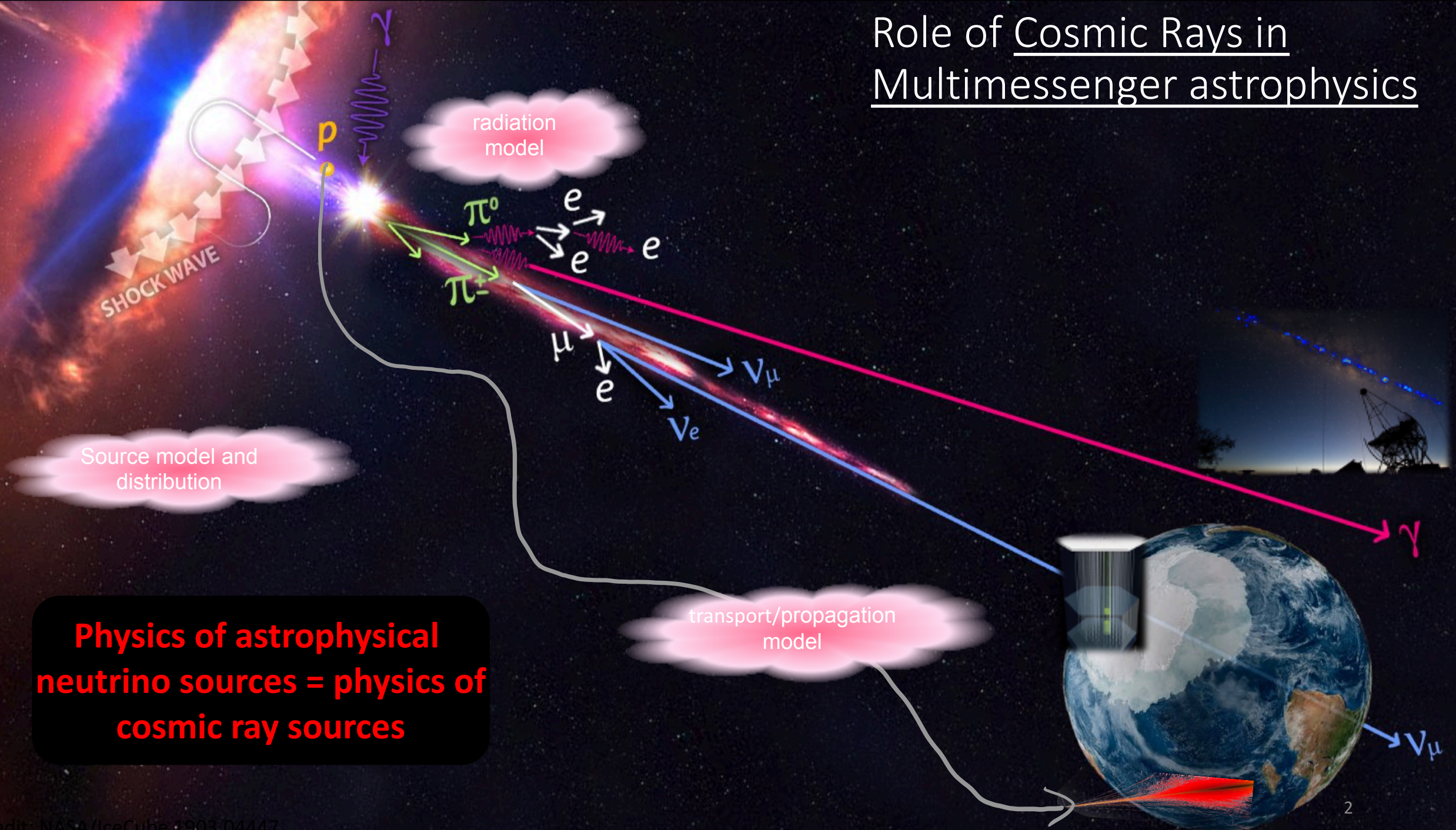
Particle physics challenges in ultra-high energy cosmic rays and atmospheric leptons

Anatoli Fedynitch

... new Assistant Fellow at Institute of Physics, Academia Sinica
Cosmology Frontier in Particle Physics, 2021/10/13

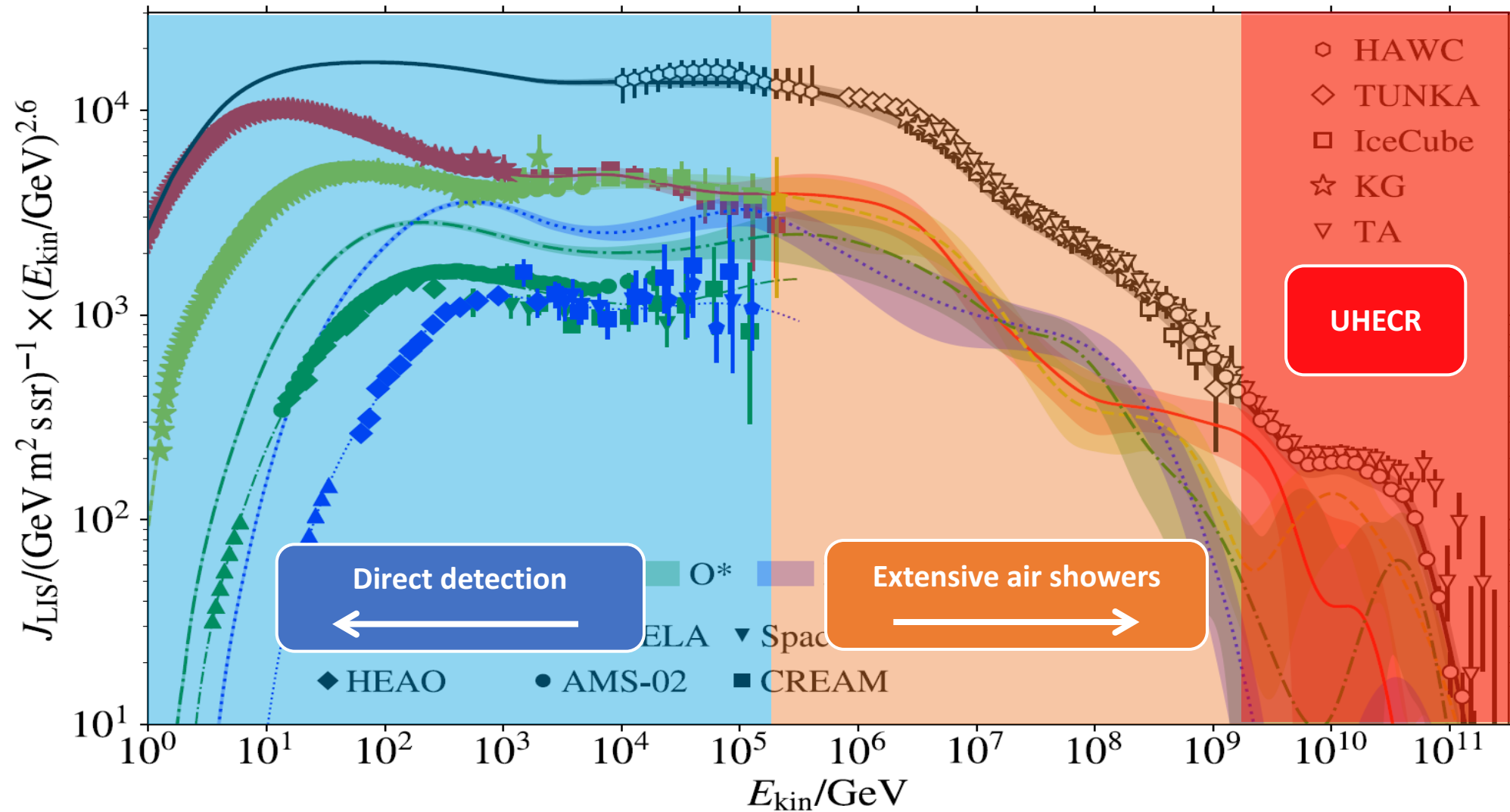


Role of Cosmic Rays in Multimessenger astrophysics



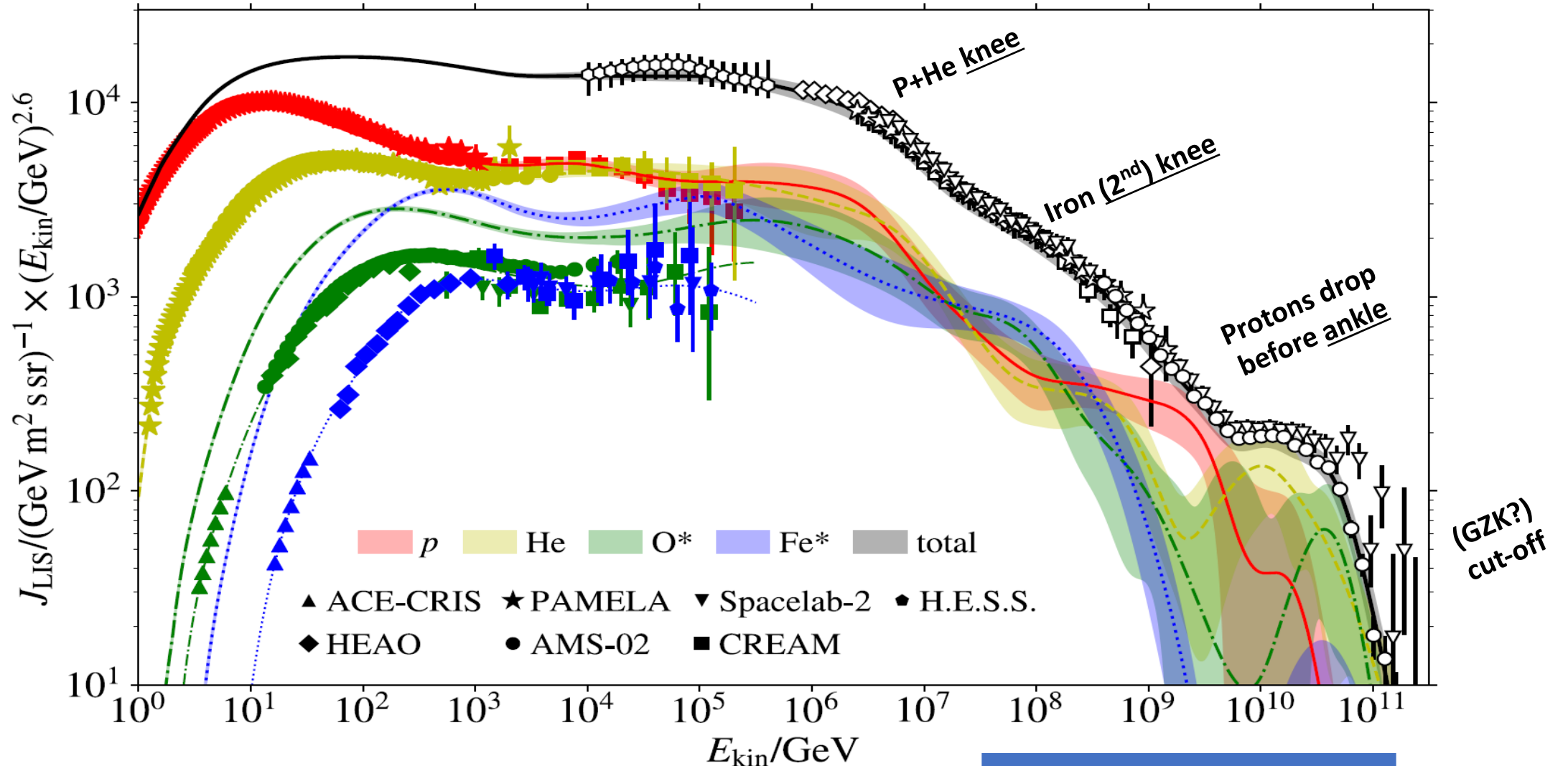
Cosmic Rays observations

Dembinski, AF, Engel, Gaisser, Stanev
PoS(ICRC2017)533



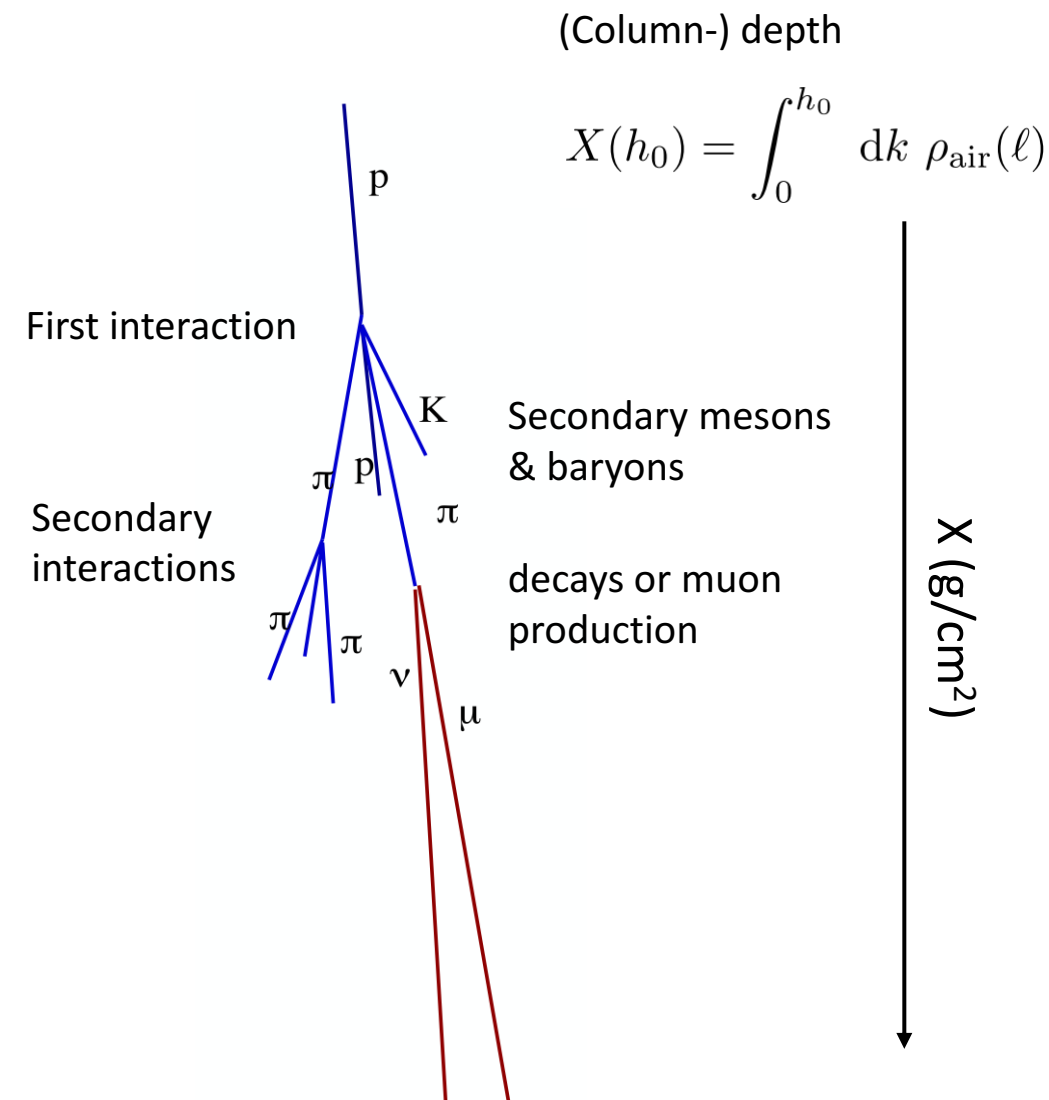
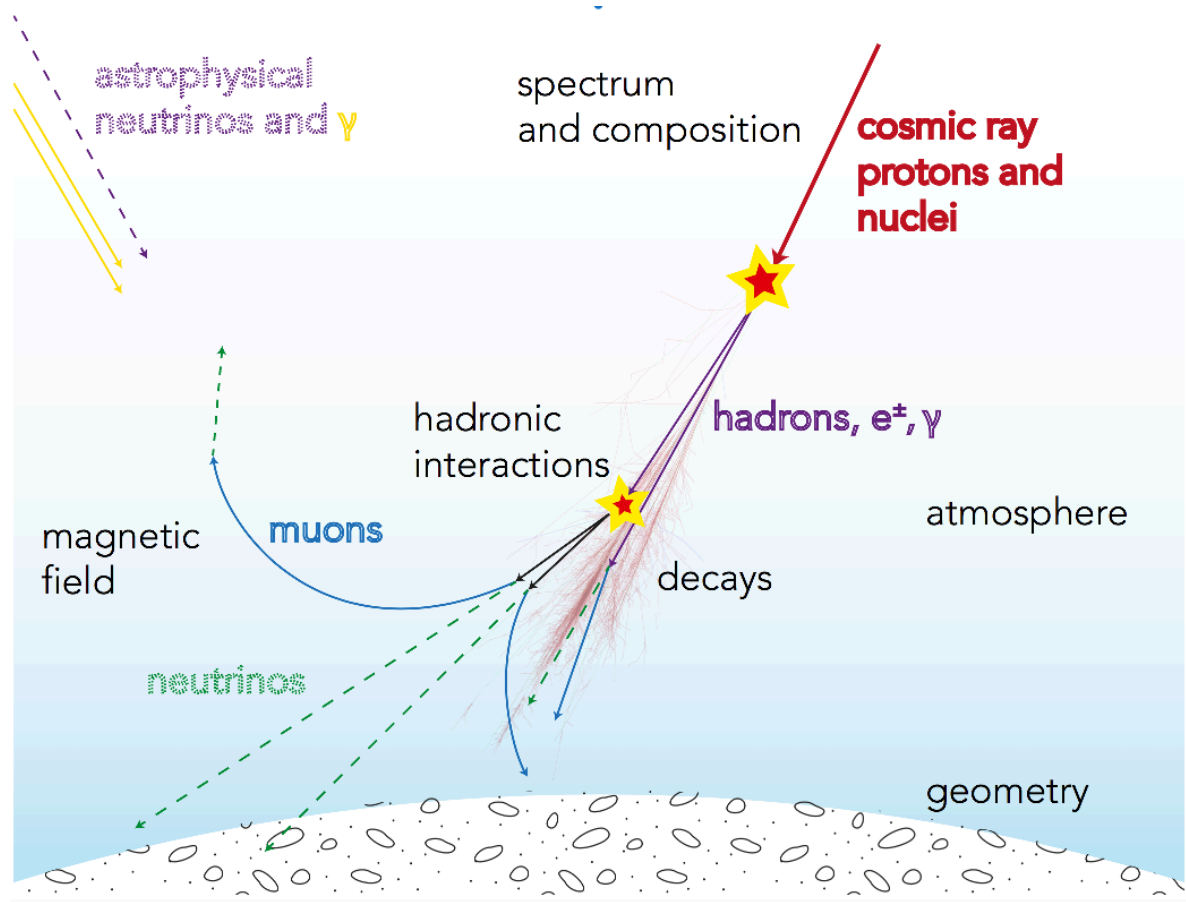
Cosmic Rays observations

Dembinski, AF, Engel, Gaisser, Stanev
PoS(ICRC2017)533



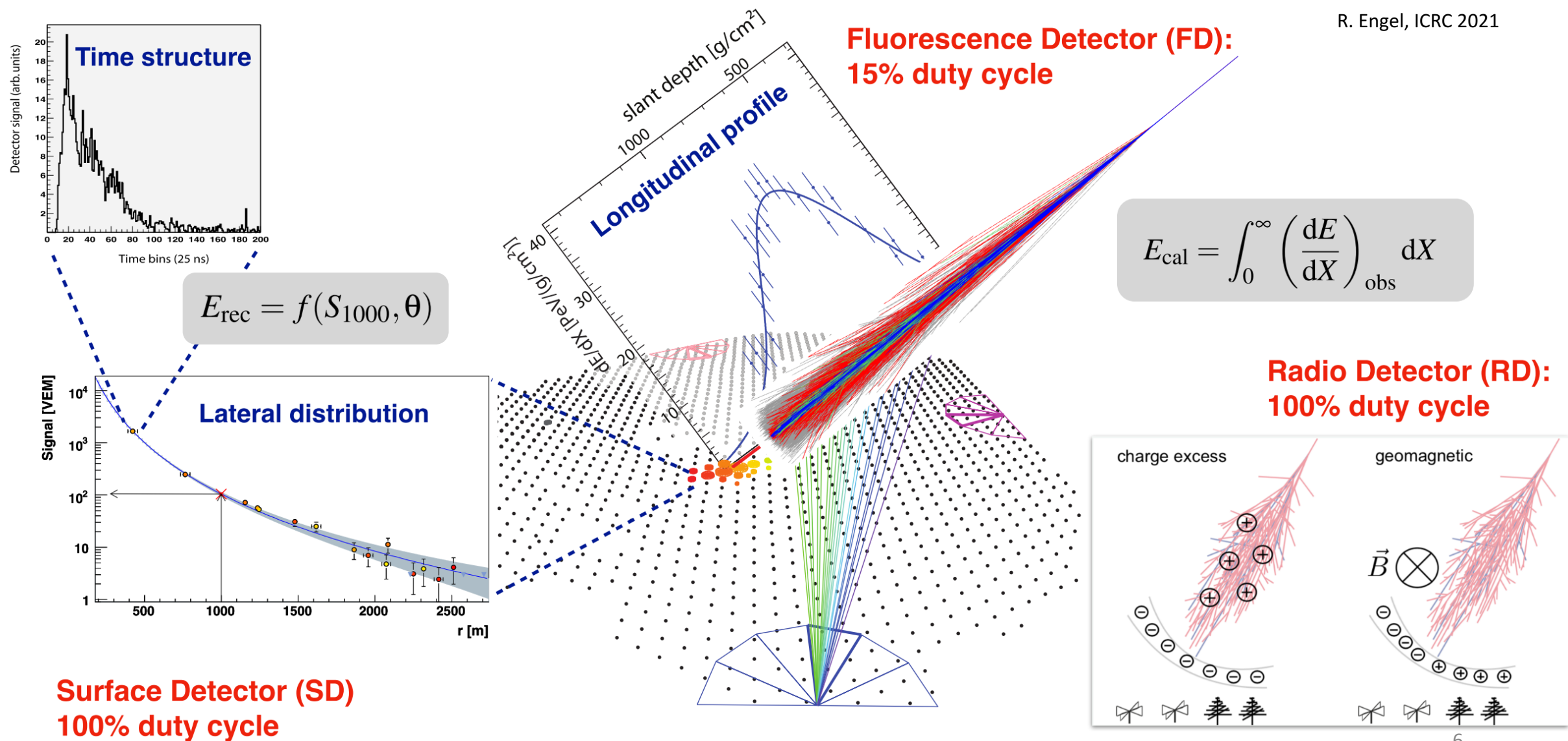
None of the features
unambiguously explained!

Interactions of cosmic rays in the atmosphere



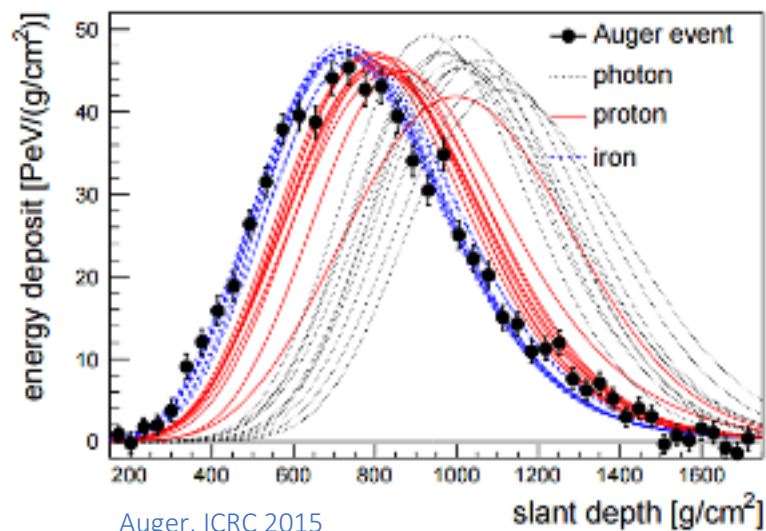
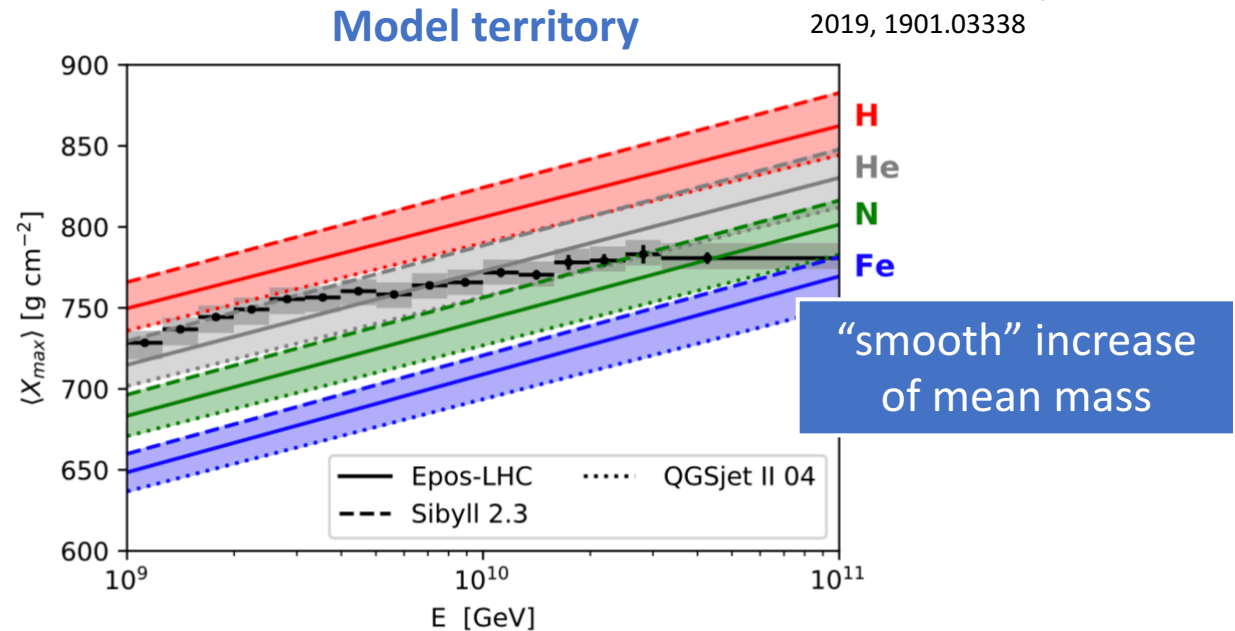
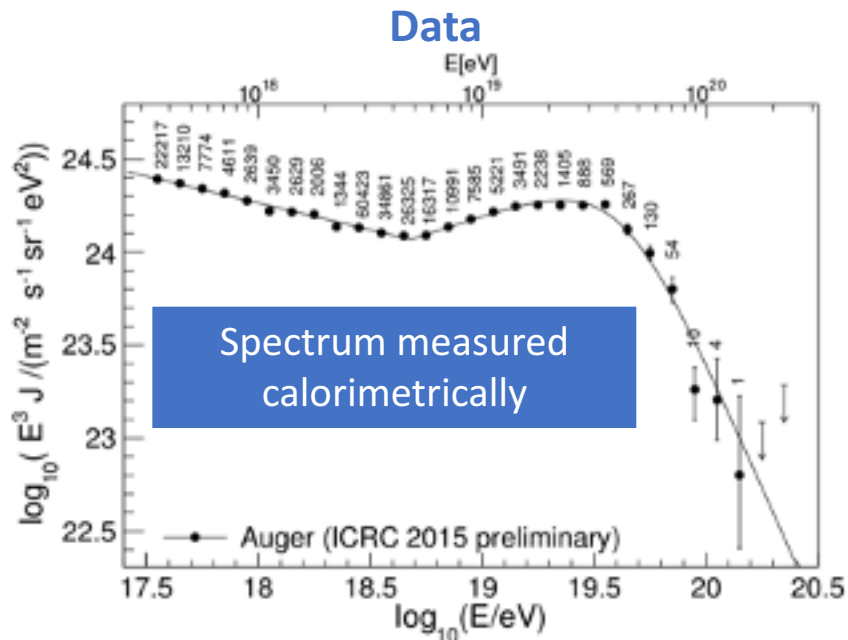
Pierre Auger: hybrid air shower detector

R. Engel, ICRC 2021

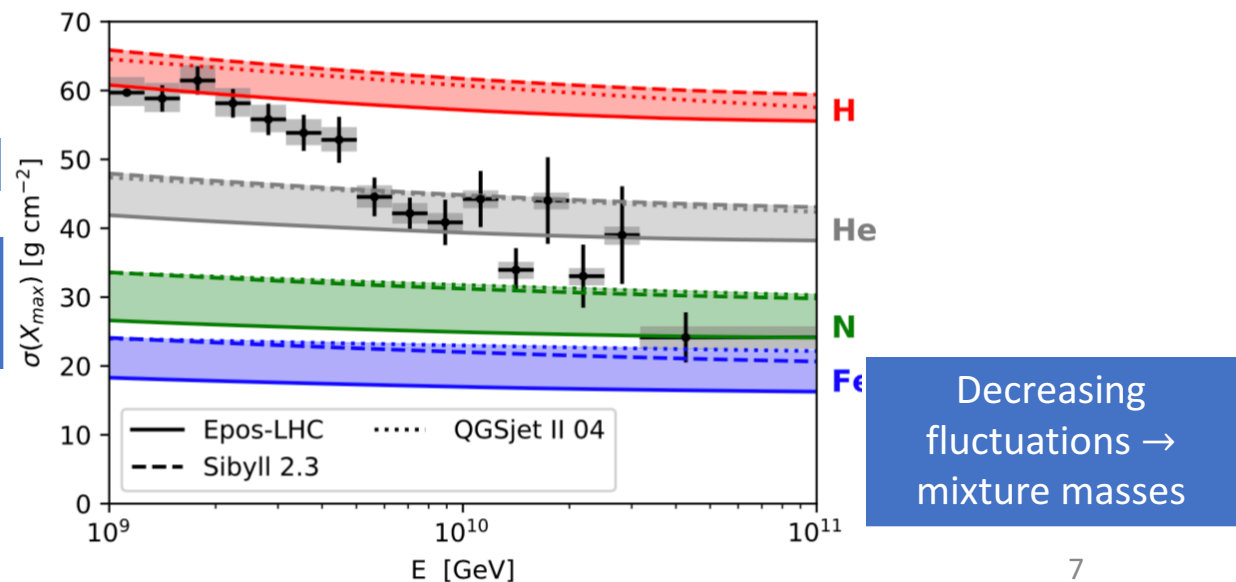


Interpretation of UHECR mass composition

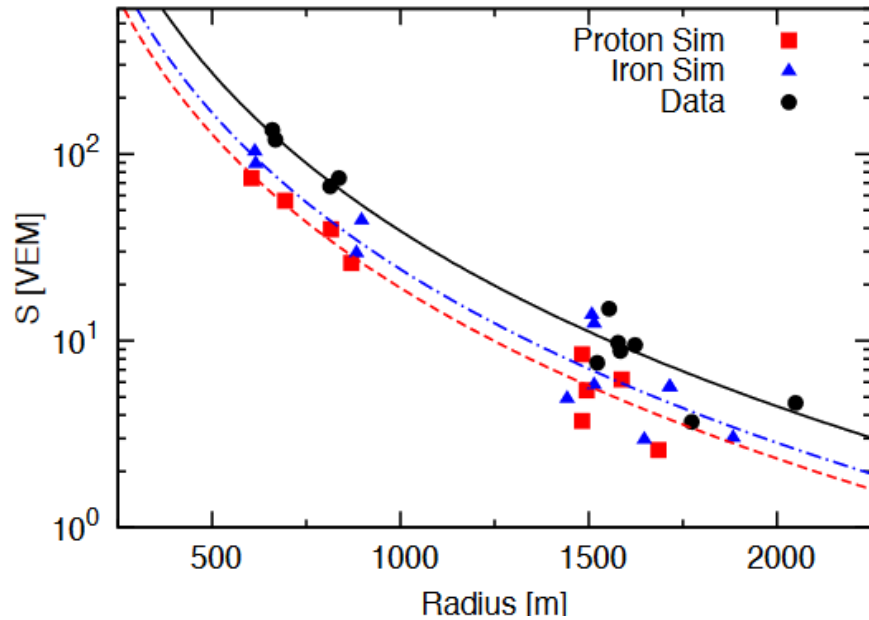
Heinze, AF, et al., ApJ
2019, 1901.03338



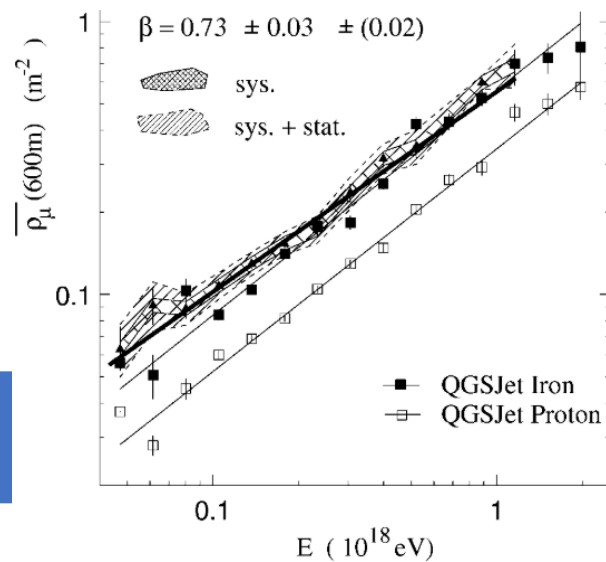
UHECR are nuclei(?)



Muon Puzzle



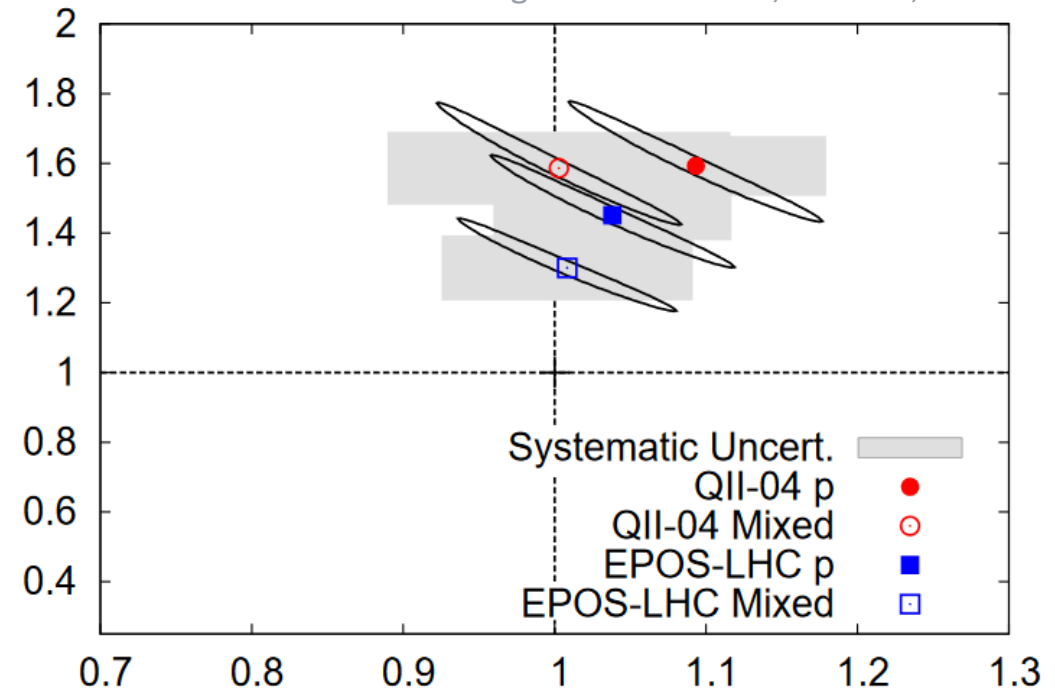
HiRes and MIA collabs. Phys.Rev.Lett. 84 (2000) 4276-4279



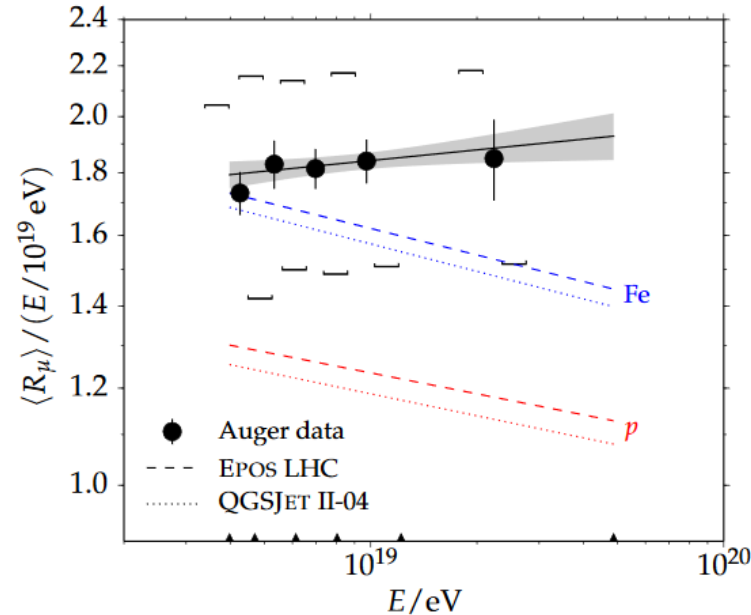
First indication
in late 1990's

$1.2 < R_{\text{had}} < 1.7$
(muon deficit in MC)

R_{had}



Pierre Auger collab. Phys.Rev.D 91 (2015) 3, 032003

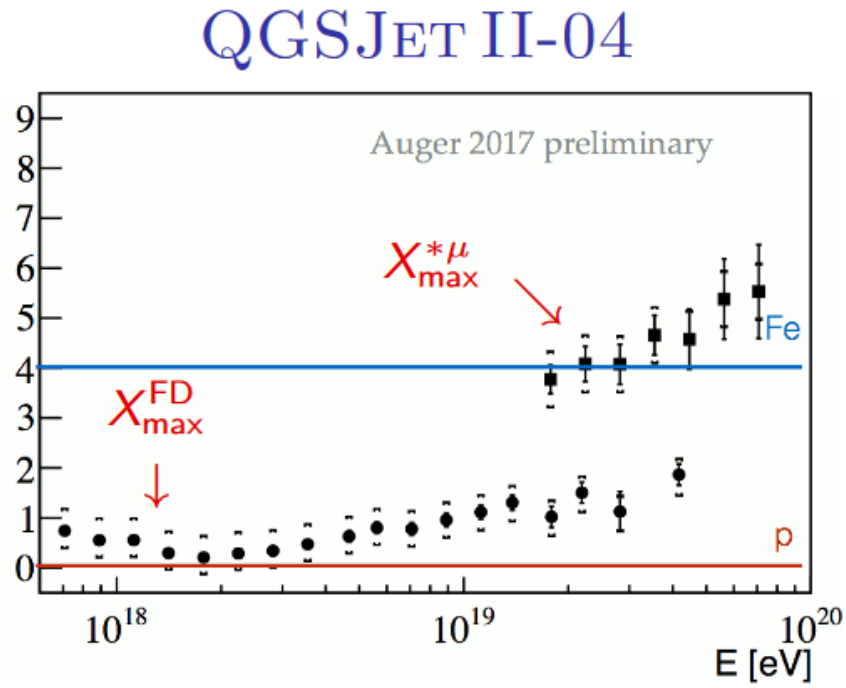
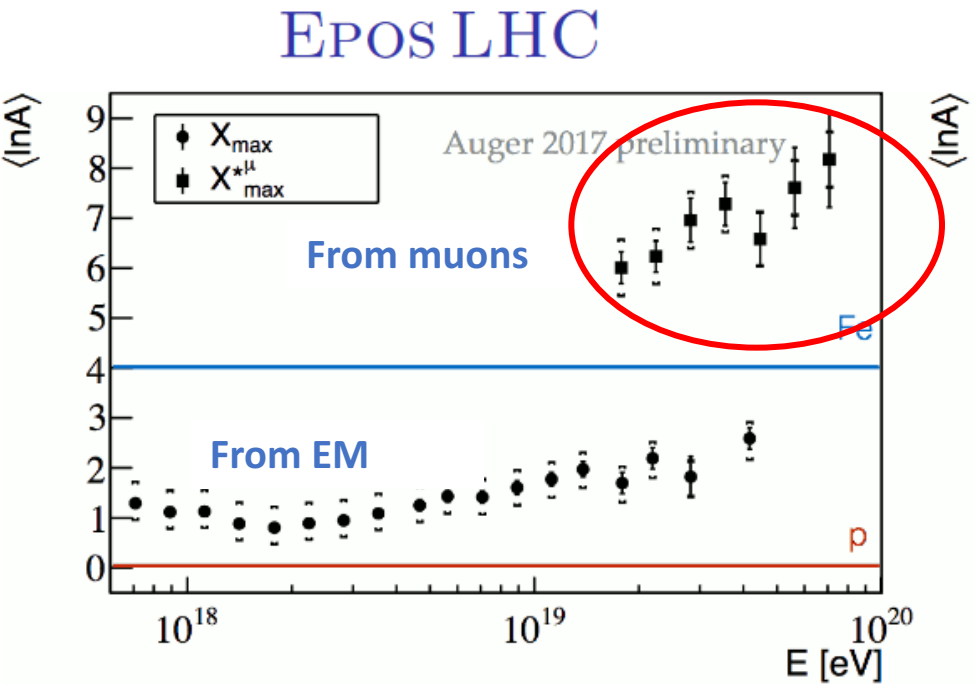
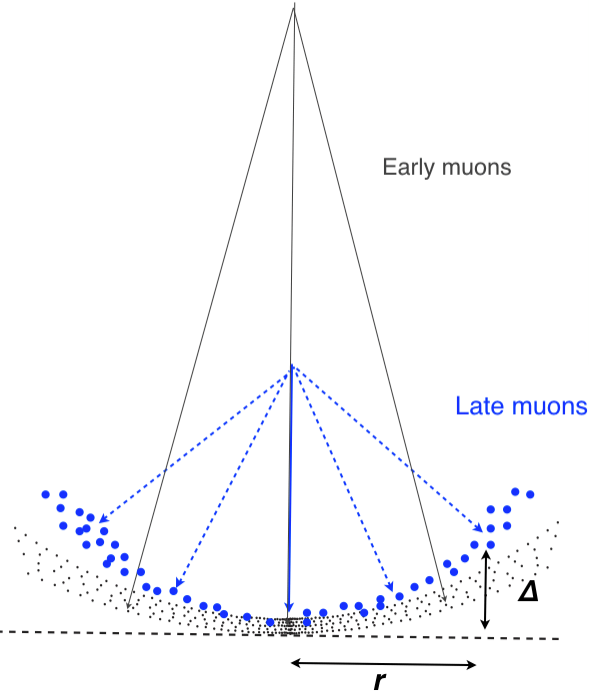


R_E → energy scale is OK

Recent review by: J. Albrecht,
L. Cazon, H. Dembinski, AF,
KH. Kampert, T. Pierog, W.
Rhode, D. Soldin, B. Spaan,
R. Ulrich, M. Unger,
arXiv:2105.06148

Production depth inconsistent with expectations

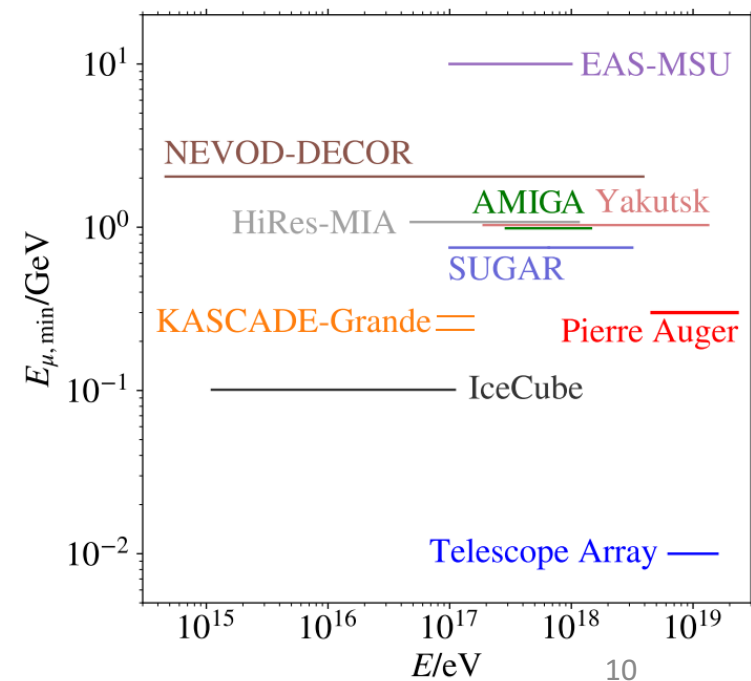
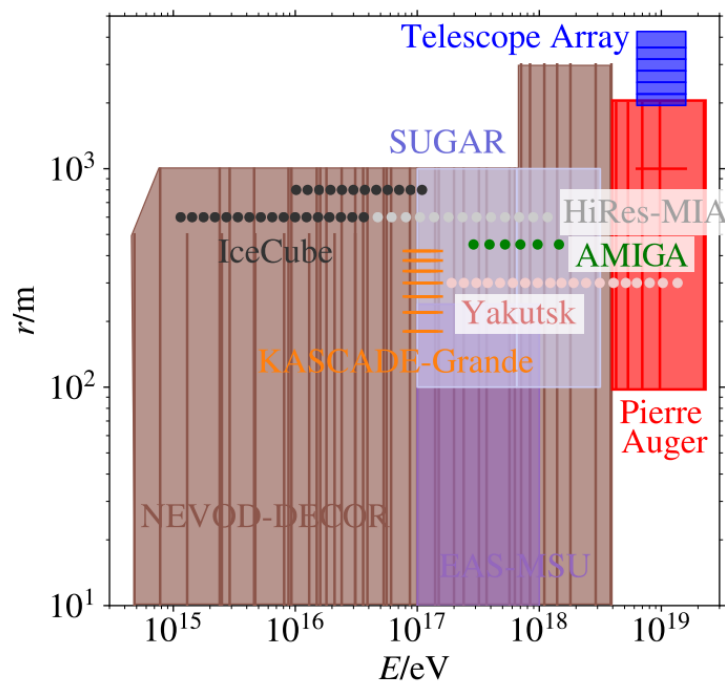
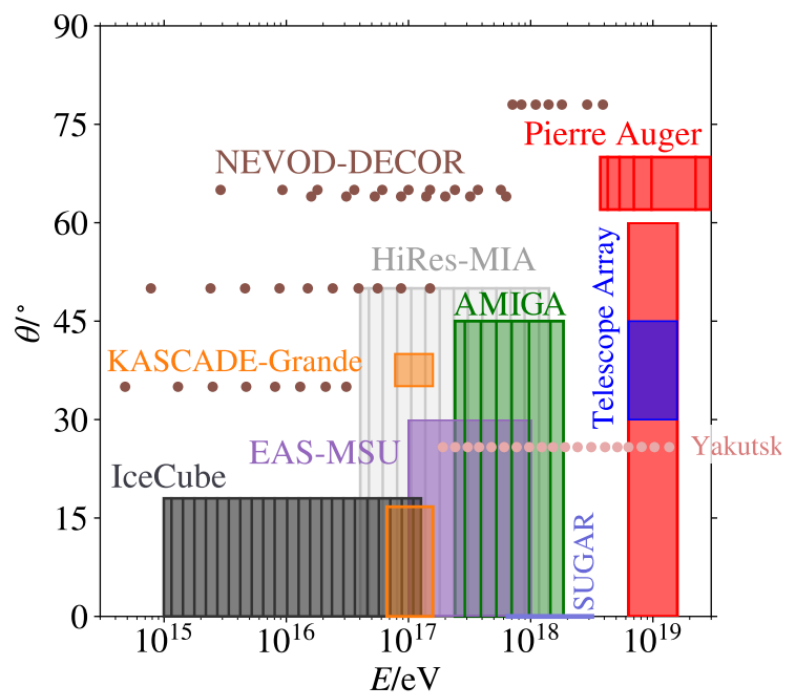
R. Prado, ISVHECRI 2018



Special working group formed (WHISP)

- 2018: Apparently conflicting evidence from different experiments
- Working group on Hadronic Interactions and Shower Physics (WHISP) formed by members of 8 experimental collaborations for UHECR 2018 conference
- Goal: Combine diverse set of muon measurements

PoS(ICRC2021)349

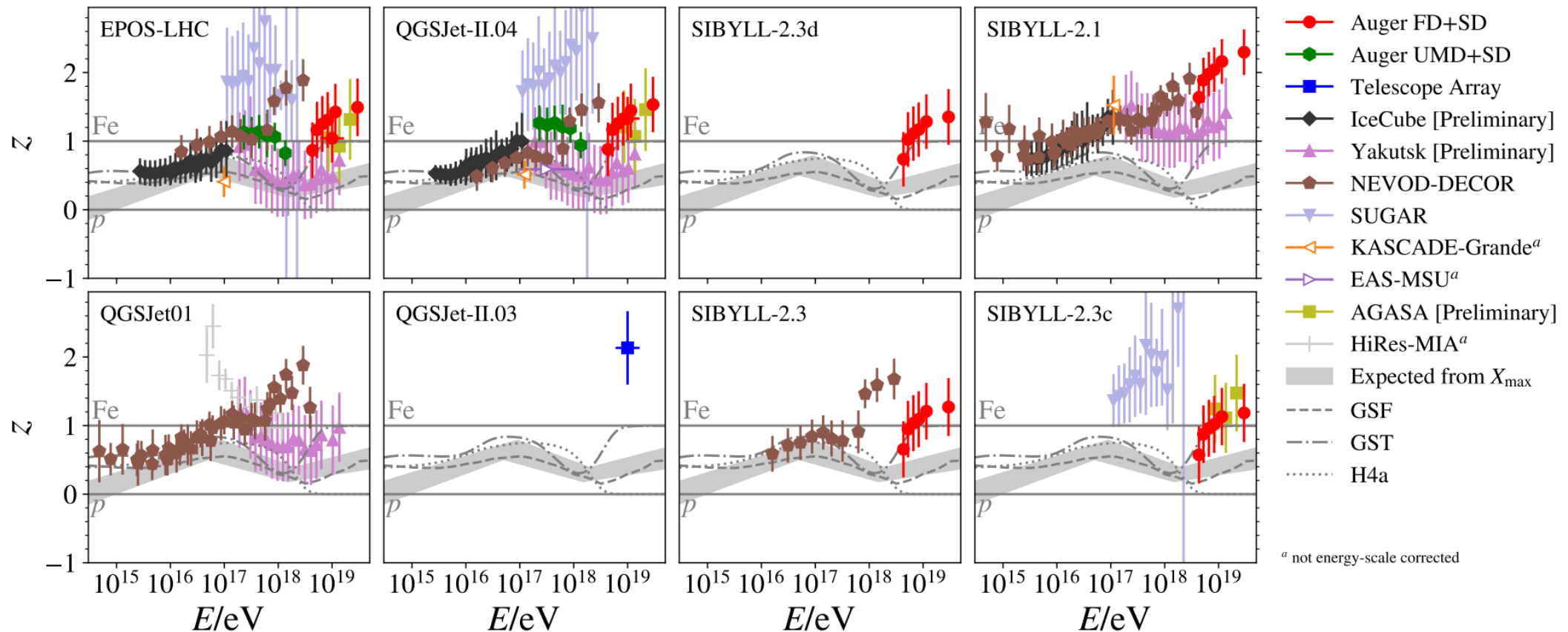


Cross-calibration of data + abstract reference scale

Abstract muon scale
independent of experiment,
dependent on air shower model

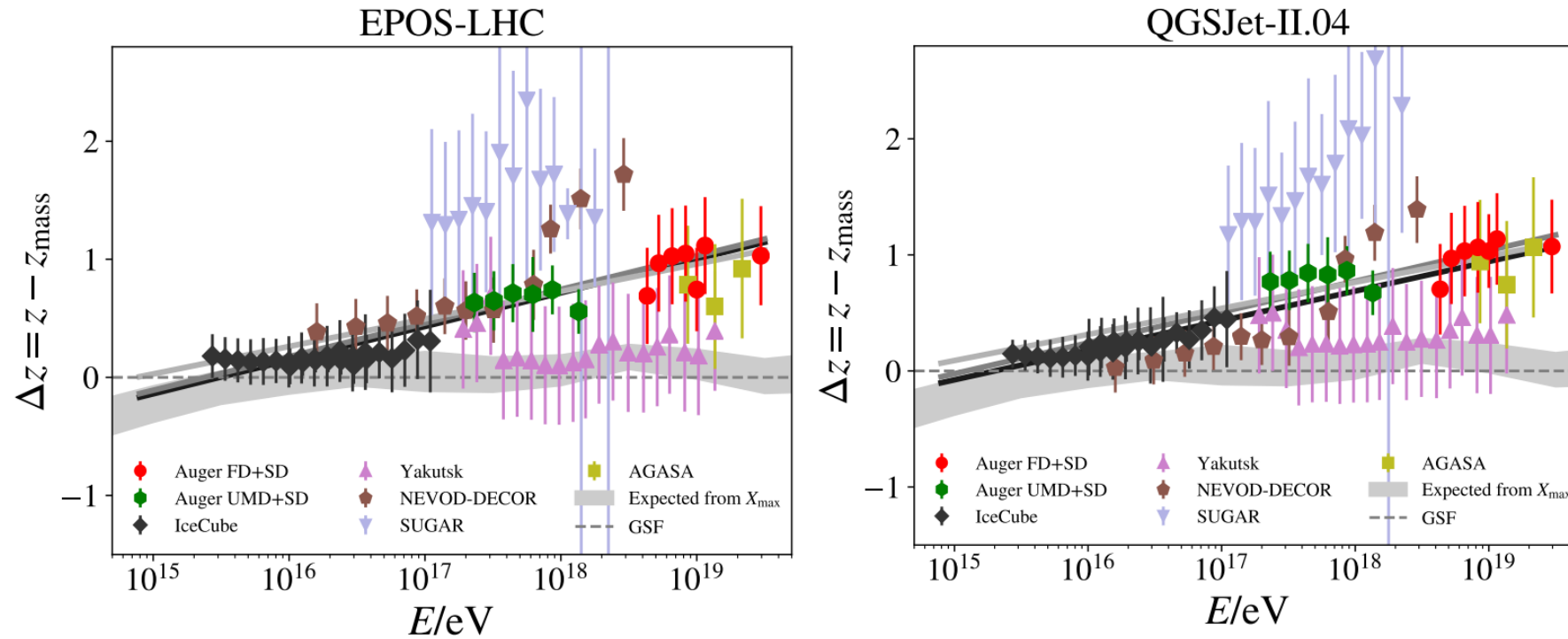
$$Z = \frac{\overset{\text{data}}{\ln(N_{\mu}^{\text{det}})} - \overset{\text{sim}}{\ln(N_{\mu_p}^{\text{det}})}}{\overset{\text{sim}}{\ln(N_{\mu_{\text{Fe}}}^{\text{det}})} - \overset{\text{sim}}{\ln(N_{\mu_p}^{\text{det}})}}$$

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Clear evidence muon deficit in simulations

PoS(ICRC2021)349



$$z = \frac{\ln(N_{\mu}^{\text{det}}) - \ln(N_{\mu p}^{\text{det}})}{\ln(N_{\mu}^{\text{det}}) - \ln(N_{\mu p}^{\text{det}})}$$

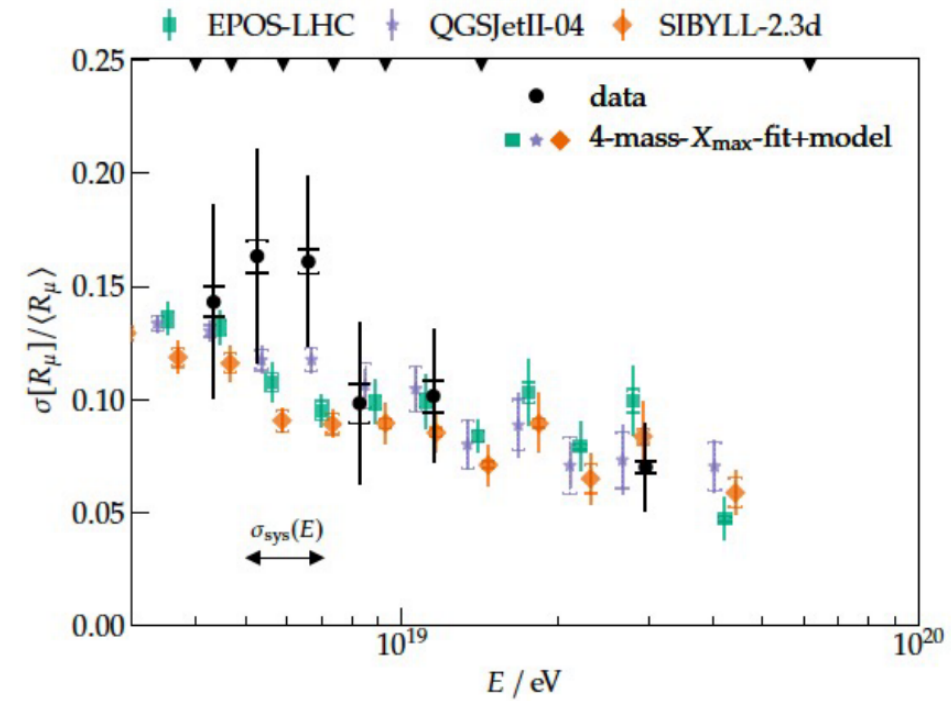
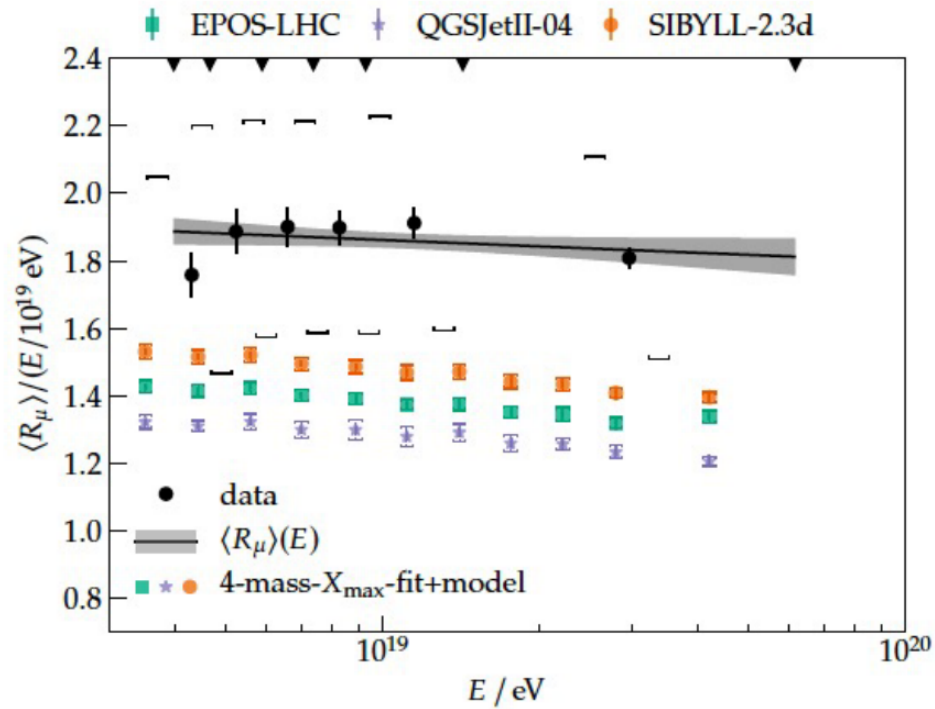
- Slope is 8σ (10σ) away from zero for EPOS-LHC (QGSJet-II.04)
- Onset of deviation around 40 PeV corresponds to $\sqrt{s} \sim 8$ TeV; in reach of LHC

$$z_{\text{mass}} \approx \frac{\langle \ln A \rangle}{\ln 56}$$

From GSF model

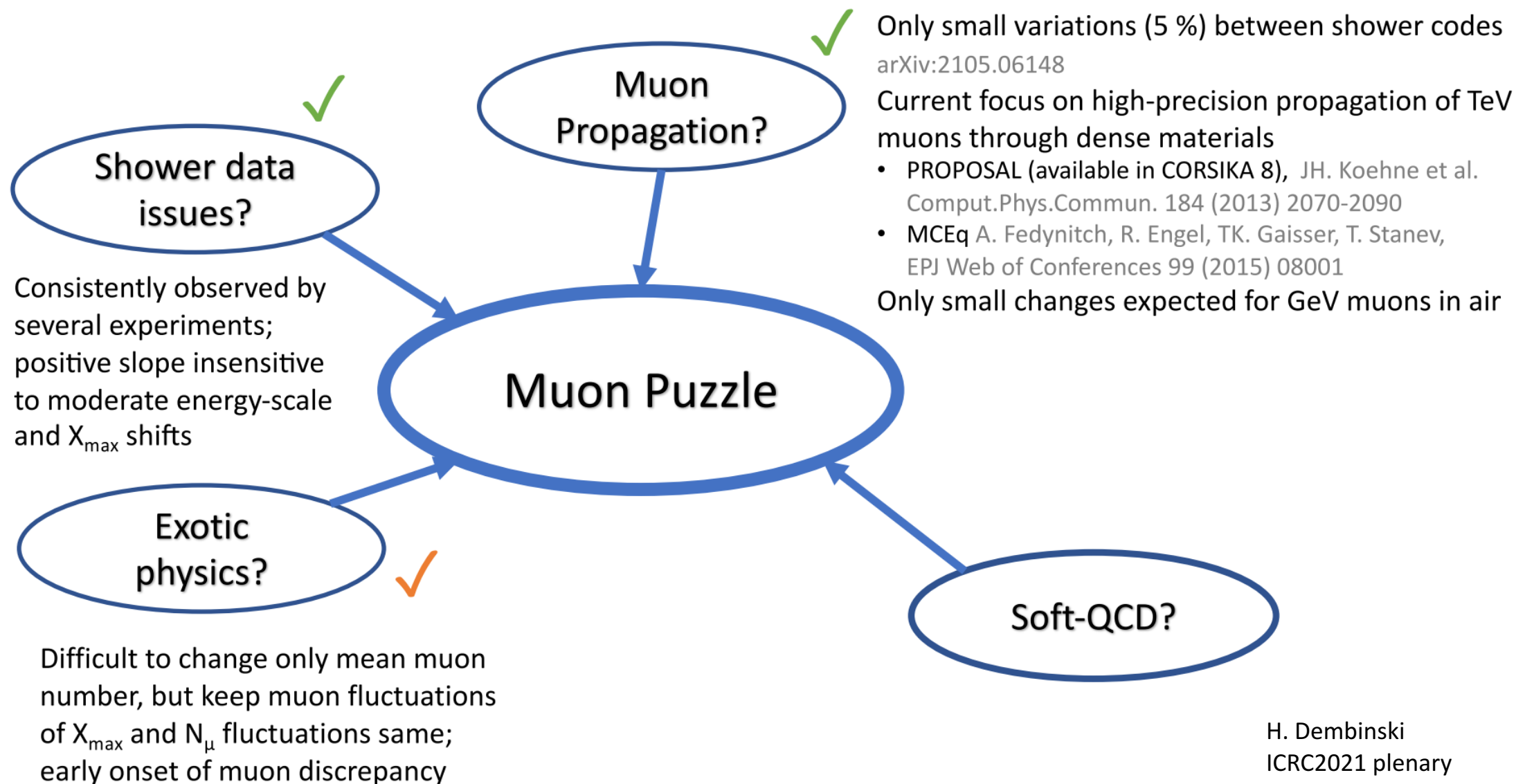
Muon number fluctuations found to be consistent

Pierre Auger collab., Phys.Rev.Lett. 126 (2021) 15, 152002



- First measurement of mean and **variance** of muon number distribution
- Variance of muon number consistent with current model predictions; mean deviates
- Constrains scenarios in which only first (or second) interaction is modified, e.g. in model with violation of Lorentz-invariance [PoS\(ICRC2021\)340](#)

Attempts to explain the Muon Puzzle



Matthews-Heitler model

J. Matthews, Astroparticle Physics 22 (2005) 387–397

N_{ch} : Particle multiplicity per interactions

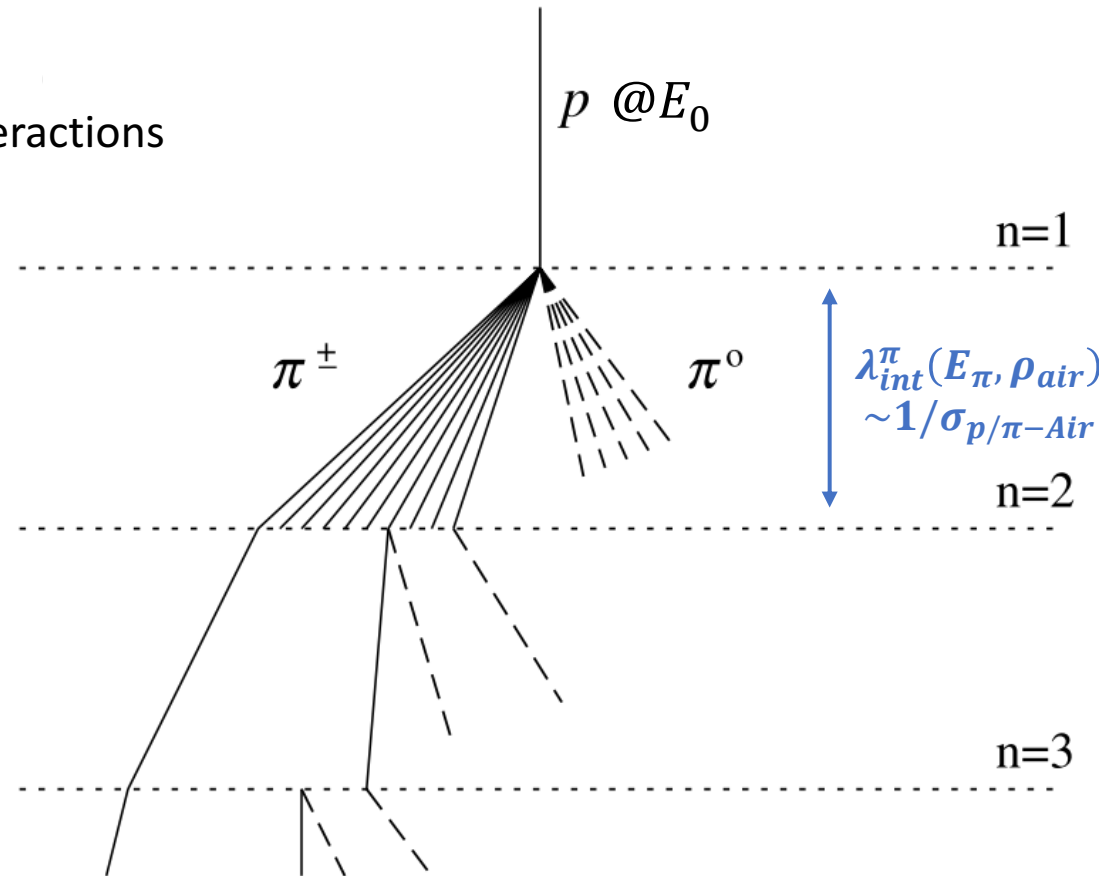
$$N_{\pi} = N_{ch}$$

$$E_{\pi} = E_0 / \left(\frac{3}{2} N_{ch} \right)$$

⋮

$$N_{\pi} = (N_{ch})^n$$

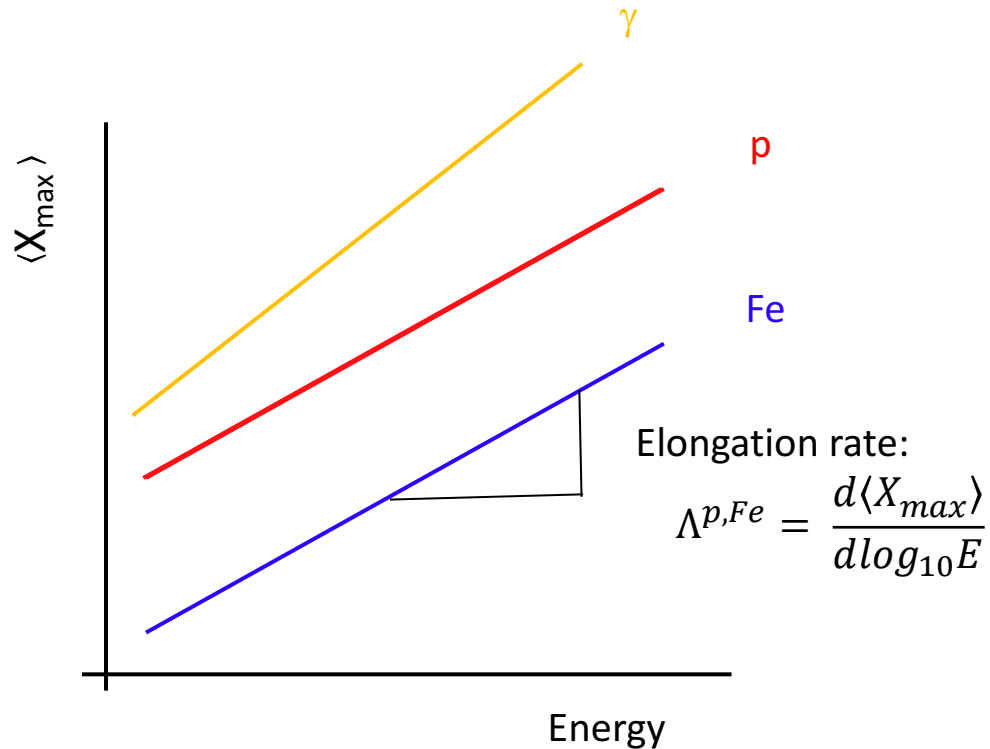
$$E_{\pi} = E_0 / \left(\frac{3}{2} N_{ch} \right)^n$$



Typical numbers of generations:
 $n_c = 3, 4, 5, 6$ for
 $E_0 = 10^{14}, 10^{15}, 10^{16}, 10^{17}$ eV

- Critical energy $\xi_c^{\pi^{\pm}}$ (= pions stop interacting) depends on:
 - Proton, pion cross section
 - Atmosphere
- Critical energy depends on primary energy (10-30 GeV)
- Central conclusions from Heitler model
 - **Cross sections** important
 - **Multiplicity** important

Understanding X_{\max}



A **third** important parameter is the **(in-)elasticity**, the energy transfer to the **leading** particle
 ...yields slightly modified formulae.

J. Matthews, Astroparticle Physics 22 (2005) 387–397
 + *K.-H. Kampert, M. Unger, Astroparticle Physics 35 (2005) 660–678*

Assuming **only** energy transfer from
 had. to EM **in first interaction**:

$$X_{\max}^p = X_o + \lambda_r \ln [E_o / (3N_{\text{ch}} \xi_c^e)]$$

$$= X_{\max}^\gamma + X_o - \lambda_r \ln[3N_{\text{ch}}]$$

$$X_o = \lambda_I \ln 2$$

EM radiation length in
 air

The elongation rate is then simply:

$$\Lambda^p = \Lambda^\gamma + \frac{d}{d\log_{10} E_o} \{X_o - \lambda_r \ln[3N_{\text{ch}}]\}$$

$$= 58 \text{ g cm}^{-2} \text{ per decade}$$

Reduction due to **growth of cross section** with energy

.. to growth of **multiplicity** ...

Seeking the connection to QCD

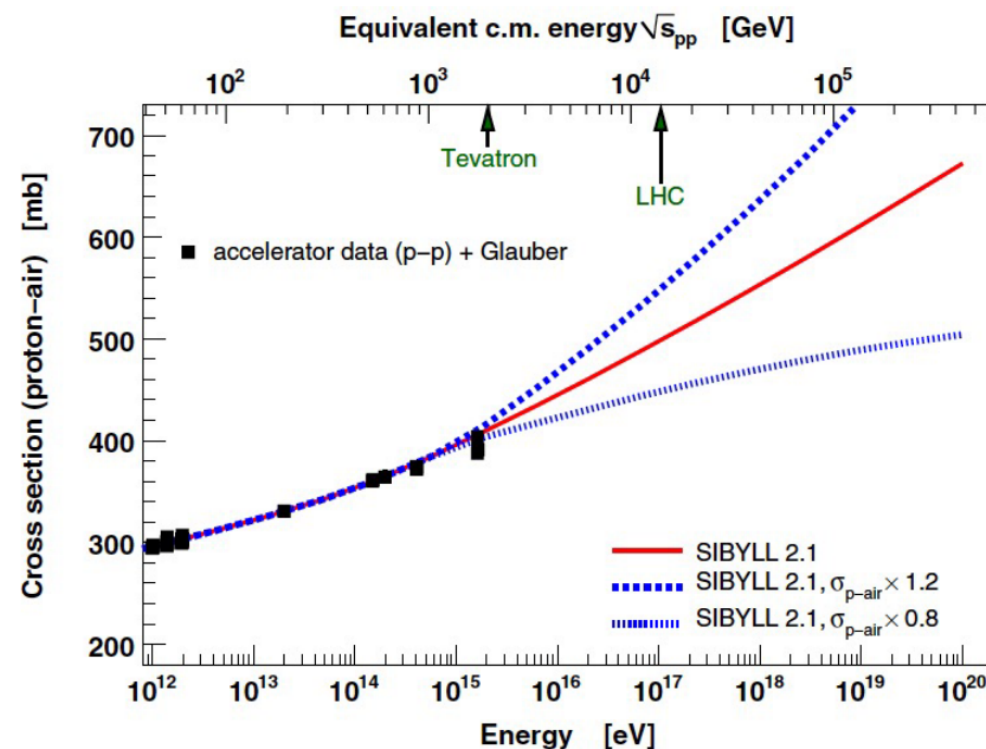
Introduce empirical variation of hadronic interactions

$$f(E) = 1 + (f_{19} - 1) \cdot \begin{cases} 0 & E < 1 \text{ PeV} \\ \frac{\log_{10}\left(\frac{E}{1 \text{ PeV}}\right)}{\log_{10}\left(\frac{10 \text{ EeV}}{1 \text{ PeV}}\right)} & E \geq 1 \text{ PeV} \end{cases}$$

Modified features

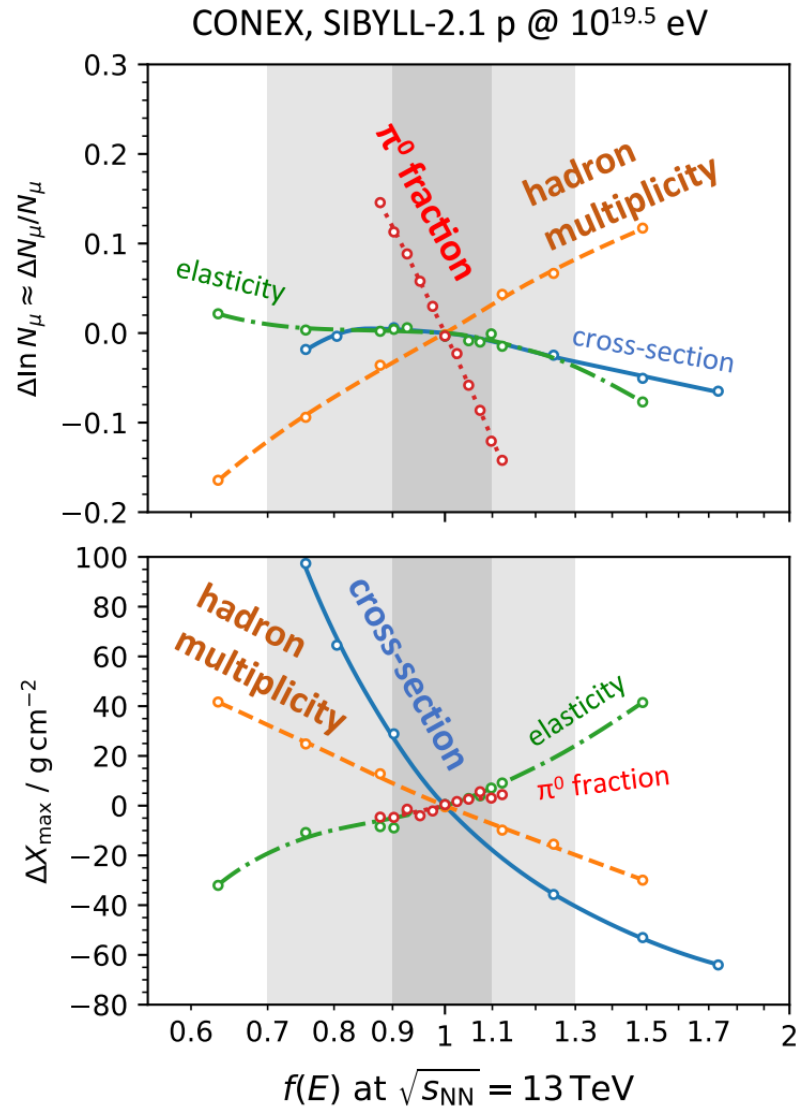
- **cross-sections**
inelastic cross-section of all interactions
- **hadron multiplicity**
total number of secondary hadrons
- **elasticity** = $E_{\text{leading}}/E_{\text{all}}$
- **π^0 fraction** = $1 - \alpha$

R. Ulrich, R. Engel, M. Unger, PRD 83 (2011) 054026



Identify most sensitive hadronic parameters

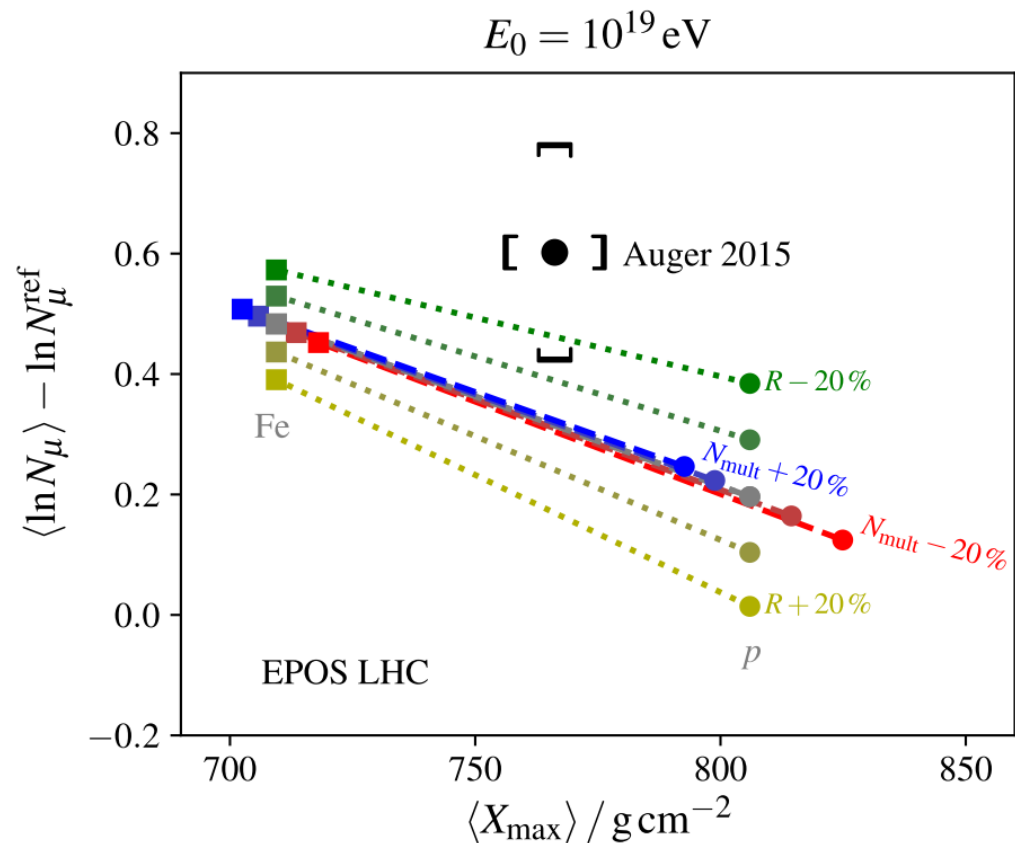
R. Ulrich, R. Engel, M. Unger, PRD 83 (2011) 054026



- Number of muons produced, N_μ
 - Very sensitive to π^0 fraction
 - Sensitive to hadron multiplicity
- Depth of shower maximum, X_{\max}
 - Very sensitive to cross-section
 - Sensitive to hadron multiplicity
 - Insensitive to π^0 fraction

Changing pi0 fraction seems most promising

S. Baur et al., arXiv:1902.09265

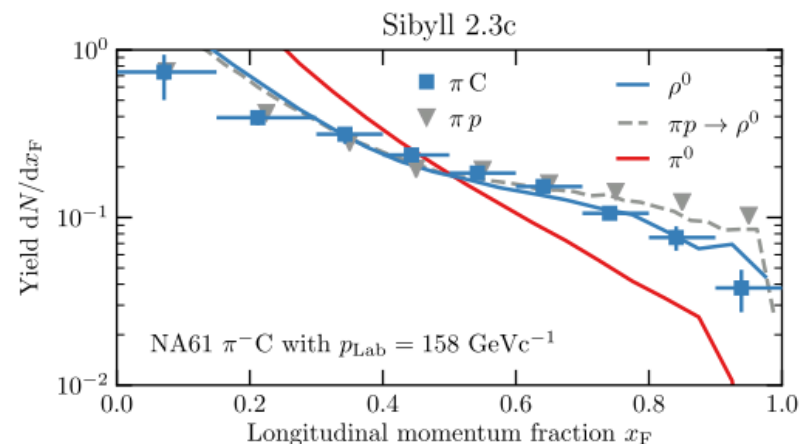
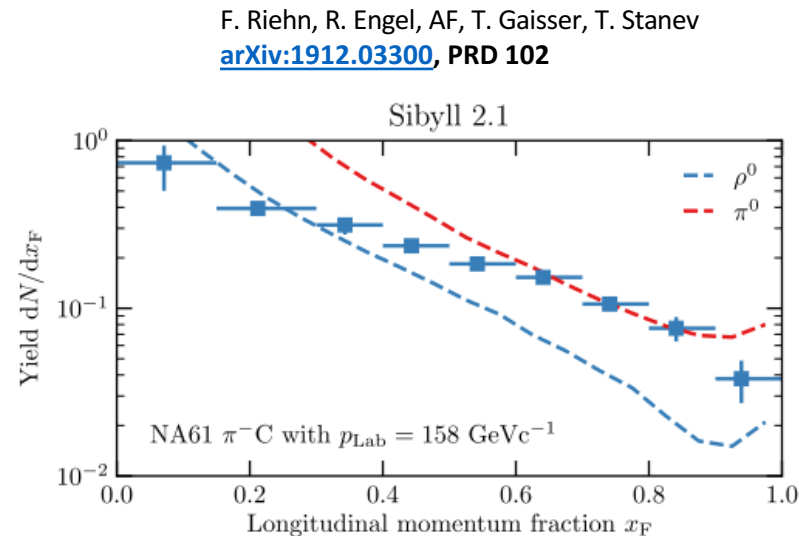
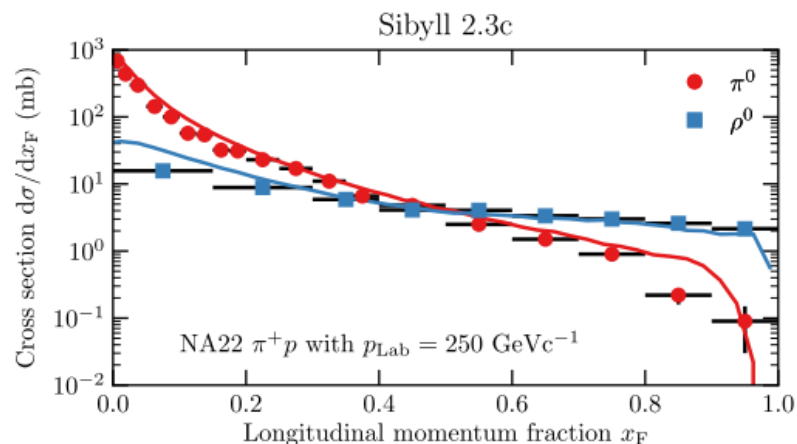
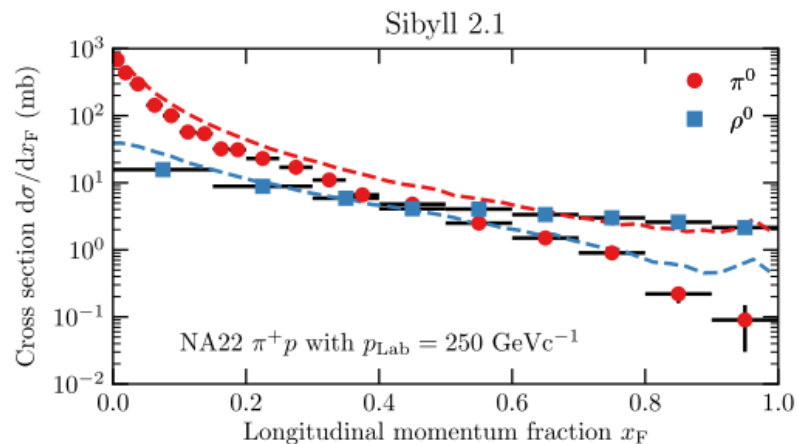
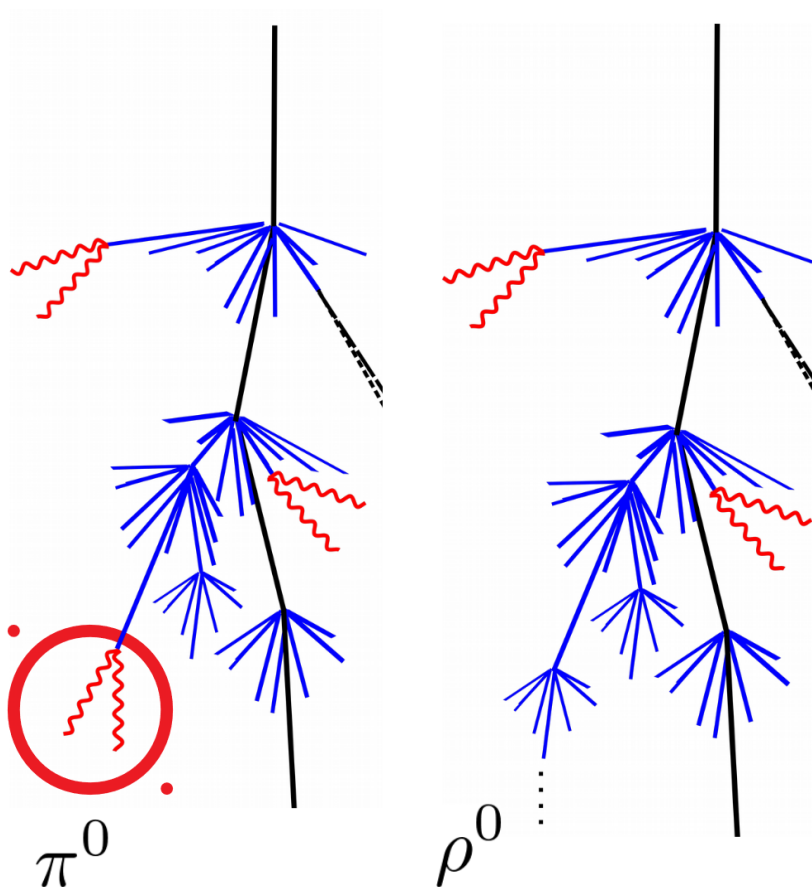


accessible experimental variable

$$R = \frac{E_{\pi^0}}{E_{\text{other hadrons}}}$$

- Changing hadron multiplicity is not a solution to the muon puzzle
- R has large effect on muon number and needs to be well known

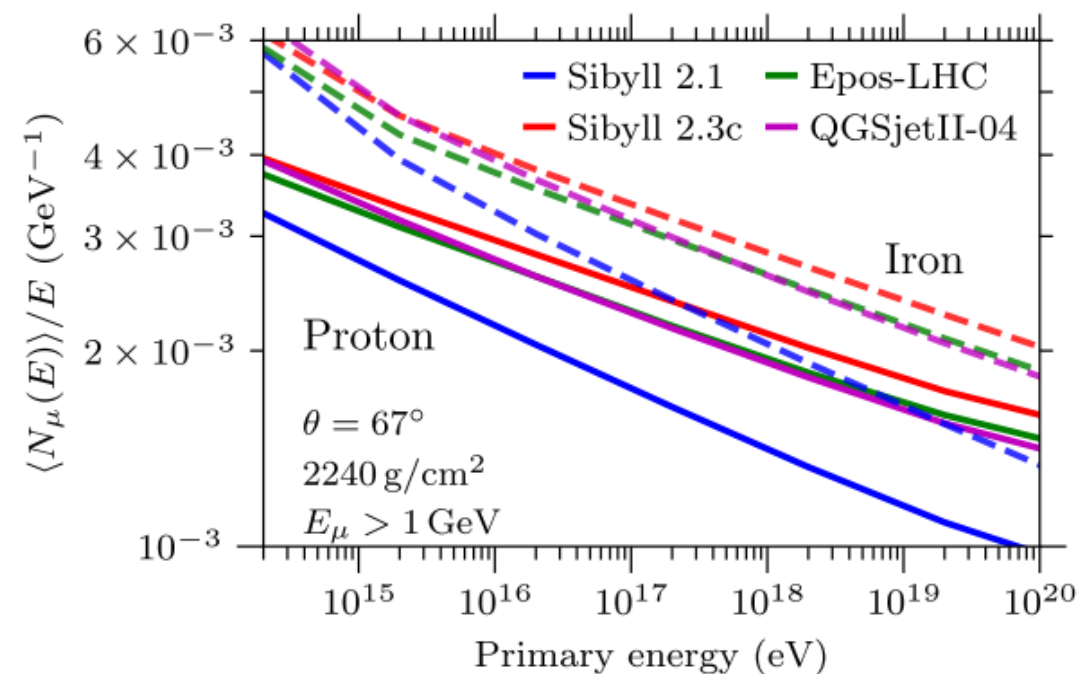
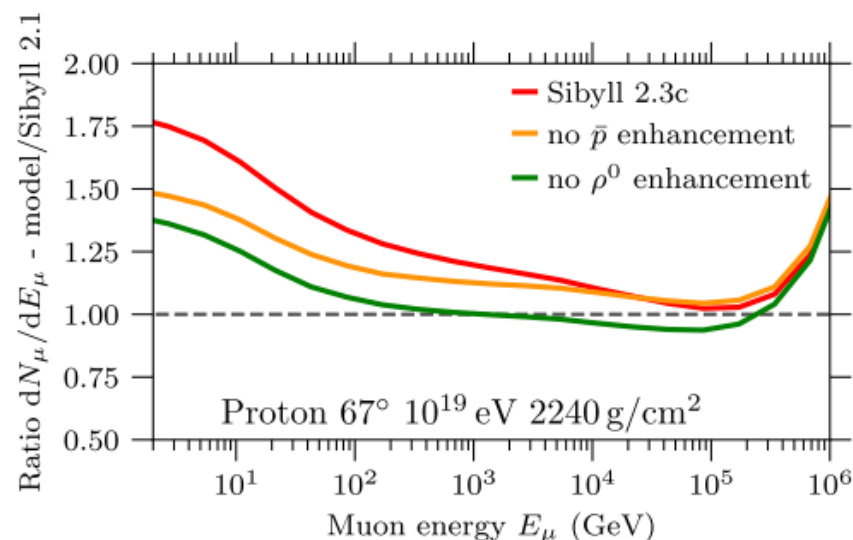
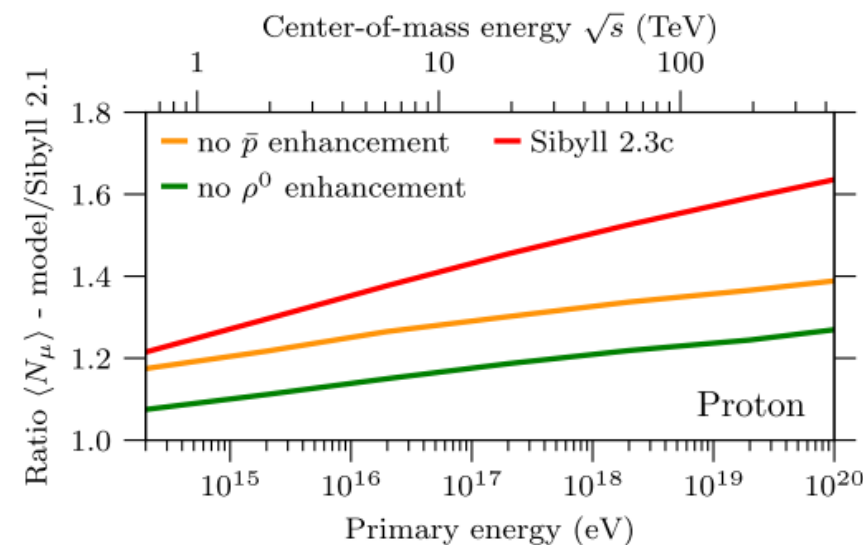
More charged hadrons through leading rho0 production



No fixed-target measurement of π^0 production off nuclei

Impact of corrections on expected muon number

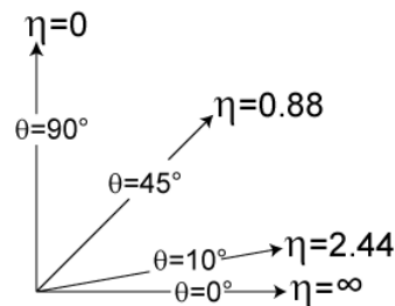
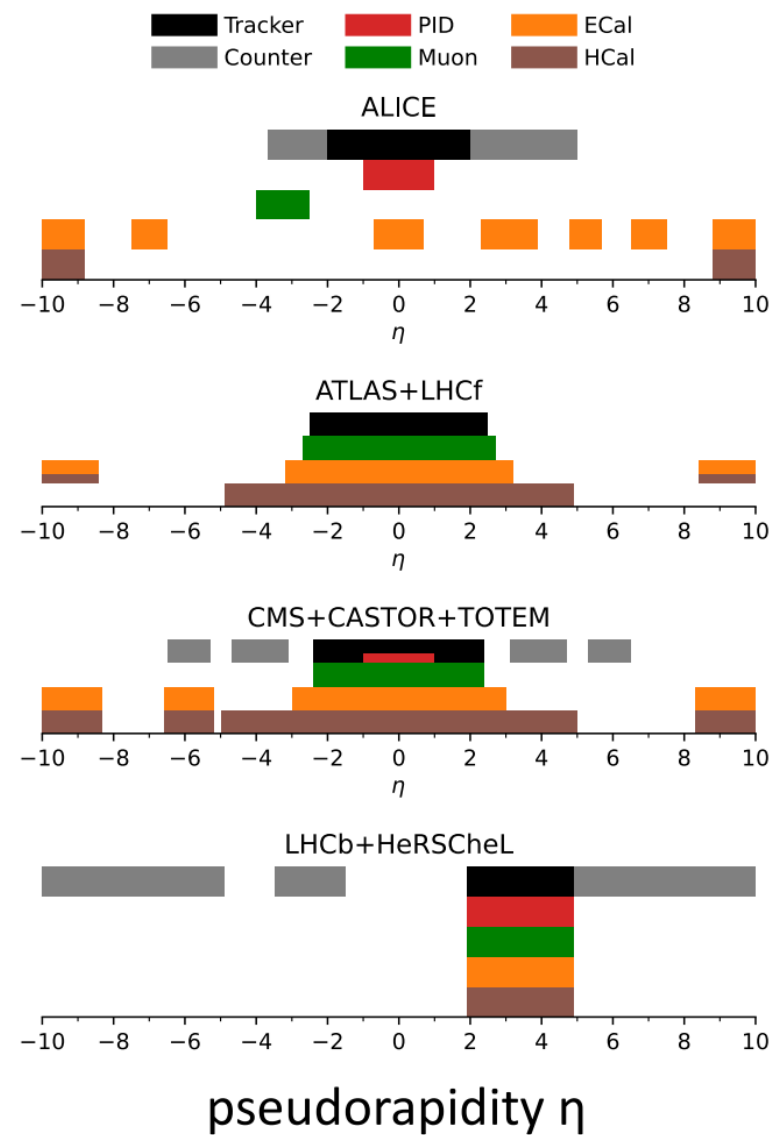
F. Riehn, R. Engel, AF, T. Gaisser, T. Stanev
[arXiv:1912.03300](https://arxiv.org/abs/1912.03300), PRD 102



!75%! more muons in newer models at certain energies

Possibilities to learn from LHC data?

arXiv:2105.06148



η related to emission angle

Image credit: JabberWok - Wikipedia CC BY-SA 3.0

- Most LHC experiments focus on $|\eta| < 2$ region
 - Detectors well instrumented here
- Forward capabilities $|\eta| > 2$
 - ALICE, TOTEM: counters
 - CMS-CASTOR: Calorimeters for $e\gamma$ and hadrons
 - LHCb: full tracking and PID at $2 < \eta < 5$
 - LHCf: neutral particles $\eta > 8$

Relevant phase space – a challenge for instrumentation

arXiv:2105.06148

EPOS-LHC: pO 10 TeV

„Muon production weight“
how many muon would be produced in shower
by secondaries in this collision

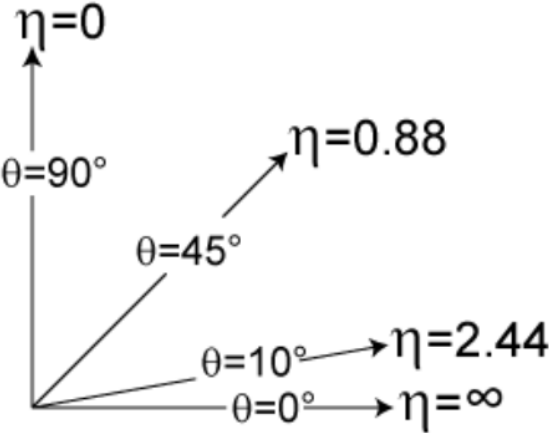
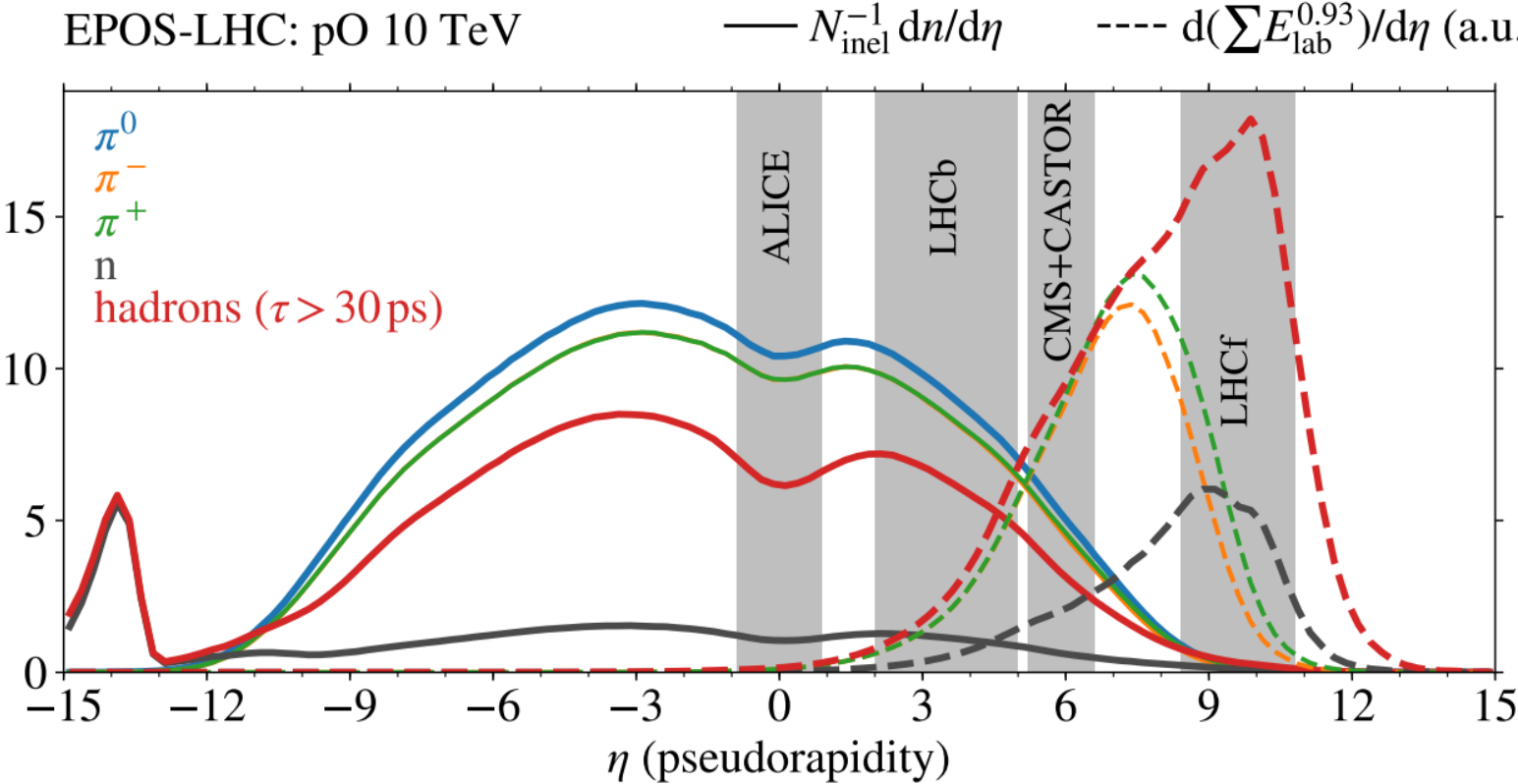
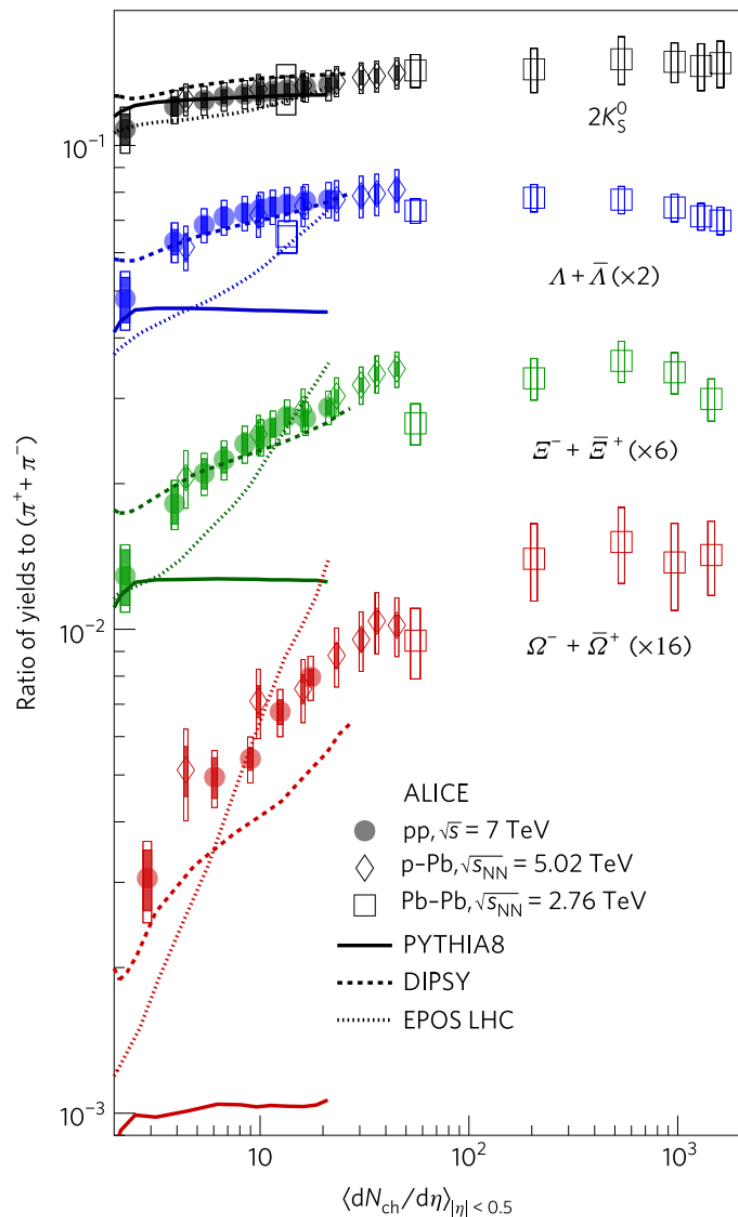


Image credit:
JabberWok - Wikipedia CC BY-SA 3.0

Other ways to modify R?



- Difficult to change R within standard QCD
- Fragmentation of strings and excited nuclear remnant believed to be universal
- Iso-spin symmetry: $\pi^+ : \pi^- : \pi^0 \sim 1 : 1 : 1$
- ALICE discovered universal enhancement of strangeness production in $pp, pPb, PbPb$
ALICE, Nature Phys. 13 (2017) 535
- More strangeness \rightarrow less $\pi^0 \rightarrow$ more muons in air showers
 $R \approx 0.41 - 0.45$ (low density) $R \approx 0.34$ (high density)
- Enhancement seems to depend **only** on density of charged particles produced in the event \rightarrow predictive power!
- Open question: Does it extend forward to $\eta \gg 1$?

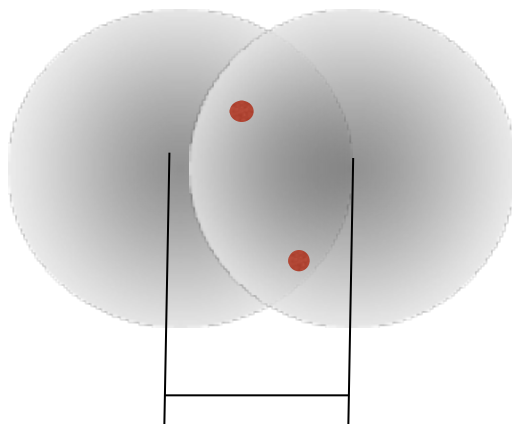
Hadronic models for air-shower simulation

	DPMJET-III.19-1	EPOS-LHC	QGSJETII-04	SIBYLL2.3d	PYTHIA 8
Domain	EAS, HEP	EAS, HIC	EAS	EAS	HEP
Theoretical basis	GRFT + minijet	GRFT + energy sharing	GRFT + resummation	GRFT + minijet	parton model
Nuclear collisions	Glauber	extended GRFT	extended GRFT	extended superposition	Glauber via Argantyr
Pomeron	soft+hard	semi-hard	semi-hard	soft+hard	soft+hard
Energy evolution of parton densities	via $Q_0(s)$ cut	parameterised	Higher-order Pomeron graphs	via $Q_0(s)$ cut	via $Q_0(s)$ cut
Energy evolution of elasticity	constant	falling	falling	constant	—
Parton distributions	CT14	custom	custom	GRV	various
Non-diffractive remnant	—	multi-quark exchange (low to high mass)	one-quark exchange (low mass)	one-quark exchange (low mass)	low mass
Diffraction (low mass)	2-channel eikonal	diffractive Pomeron	3-channel eikonal	2-channel eikonal	Pomeron emission
Diffraction (high mass)	cut enhanced graphs	Pomeron exchange	cut enhanced graphs	Pomeron exchange	Pomeron exchange
String fragmentation (fitted data)	Lund (e^+e^-)	area law (e^+e^-)	custom (pp)	Lund (pp)	Lund (e^+e^-)
Forward-central correlation	weak	strong	strong	weak	strong
Charm production	pQCD (incomplete)	—	—	parameterised + intrinsic	pQCD
Collective effects	string fusion	core-corona (parameterised)	—	—	colour reconnection, rope hadronization, string shoving

GRFT: Glauber-Regge-Field-Theory

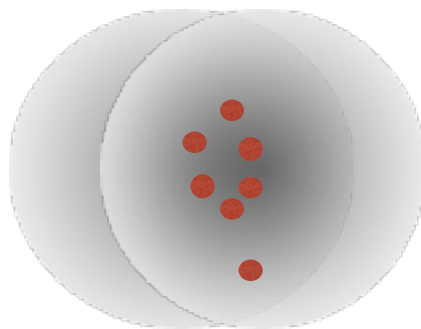
Multiplicity scales with MPI and depends on transverse parton density

Low energy

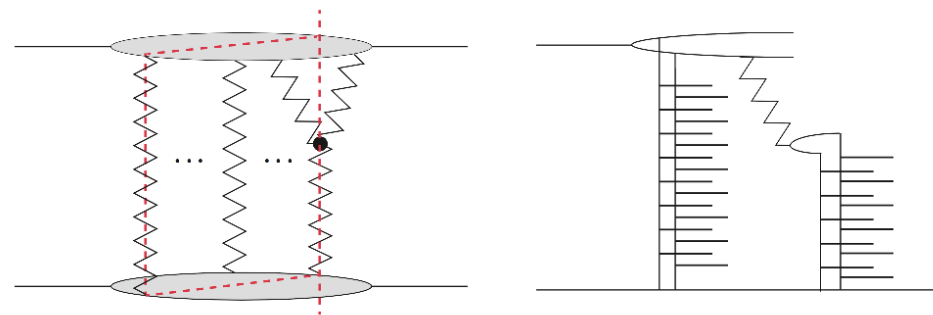


Impact parameter b

High energy



Example for cut topologies



Simple MPI model:

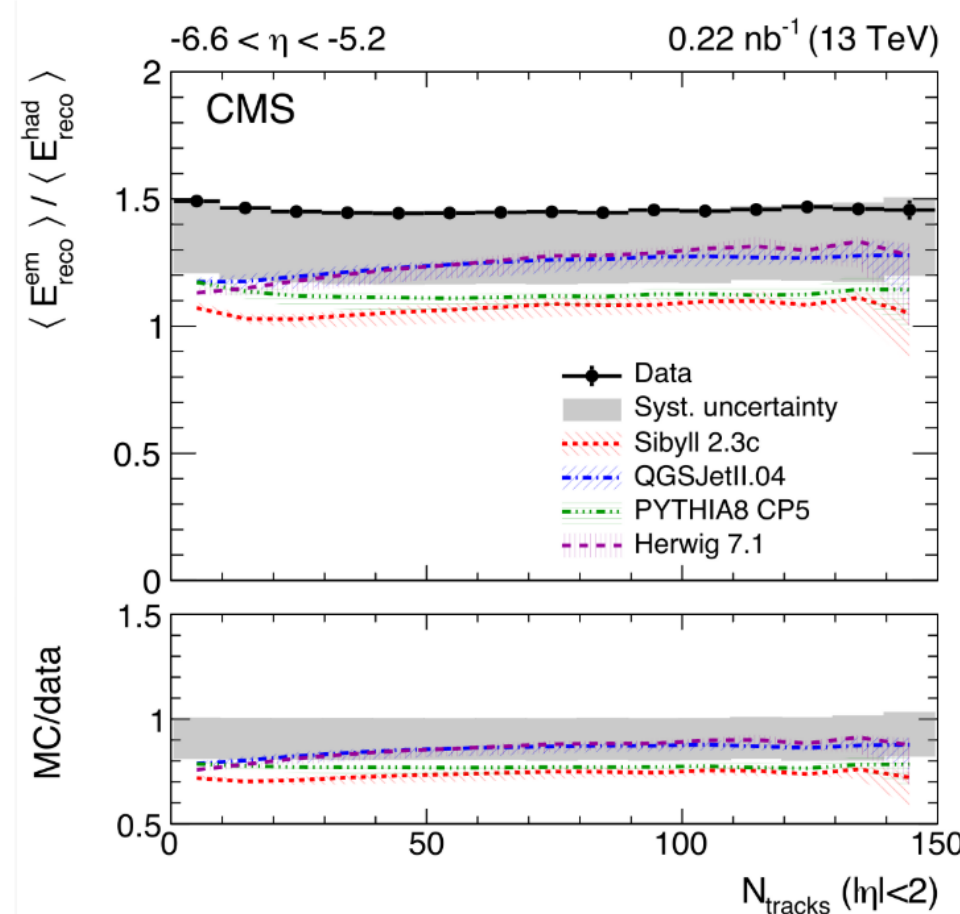
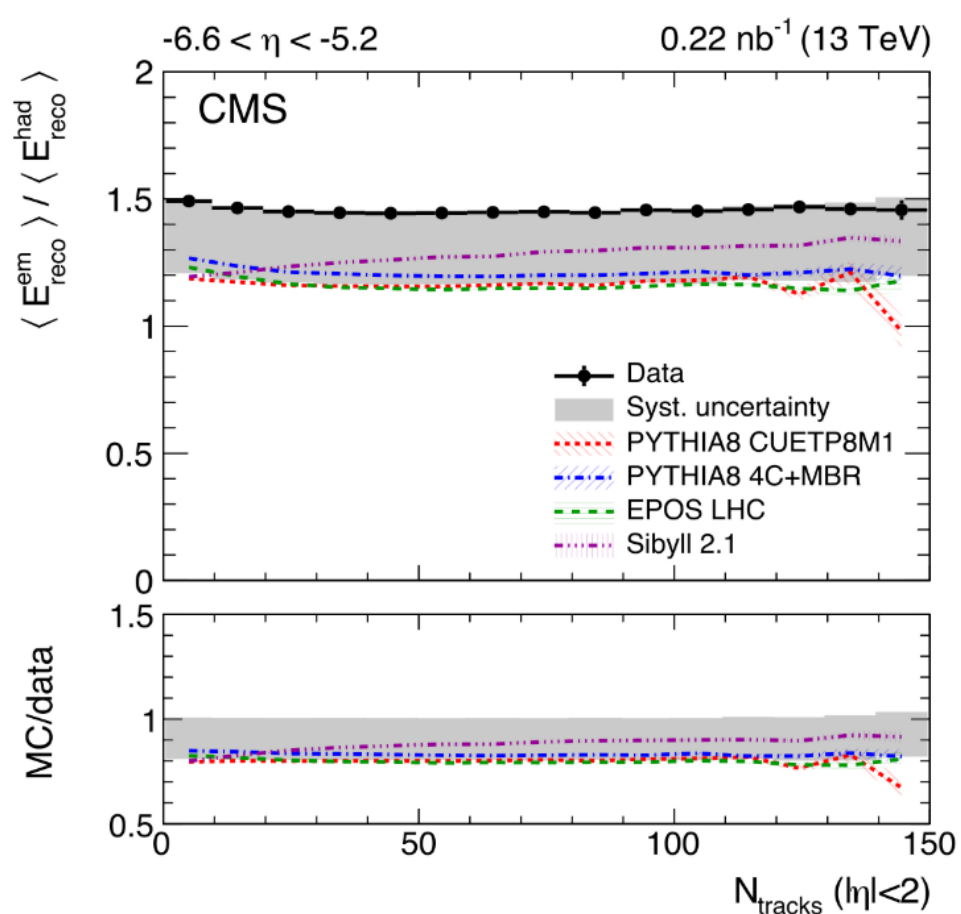
$$\sigma(n_S, n_H, \dots) = \int d^2 \vec{B} \frac{(-2\chi_S)^{n_S}}{n_S!} \frac{(-2\chi_H)^{n_H}}{n_H!} \dots e^{-2\chi}$$

- Unitarity and multiple-cut structure from Eikonal expansion
- uncorrelated multiple interactions
- Collinear factorization not applicable due to missing transverse dependence
- Problems: Saturation? Hydro? Core-corona? Energy evolution? FSI? → ...cooking...cooking...

Direct measurements of R in pp suggest that R already too low → less muons

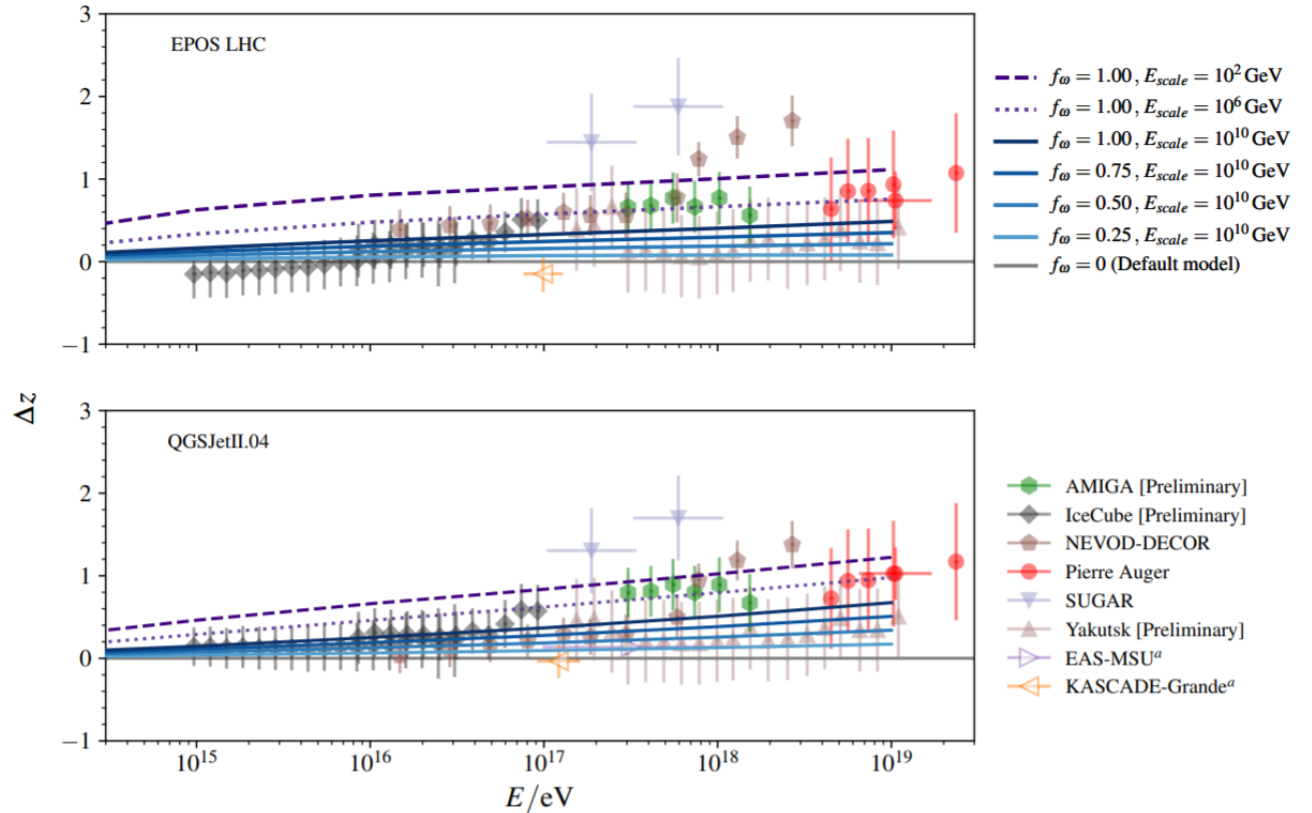
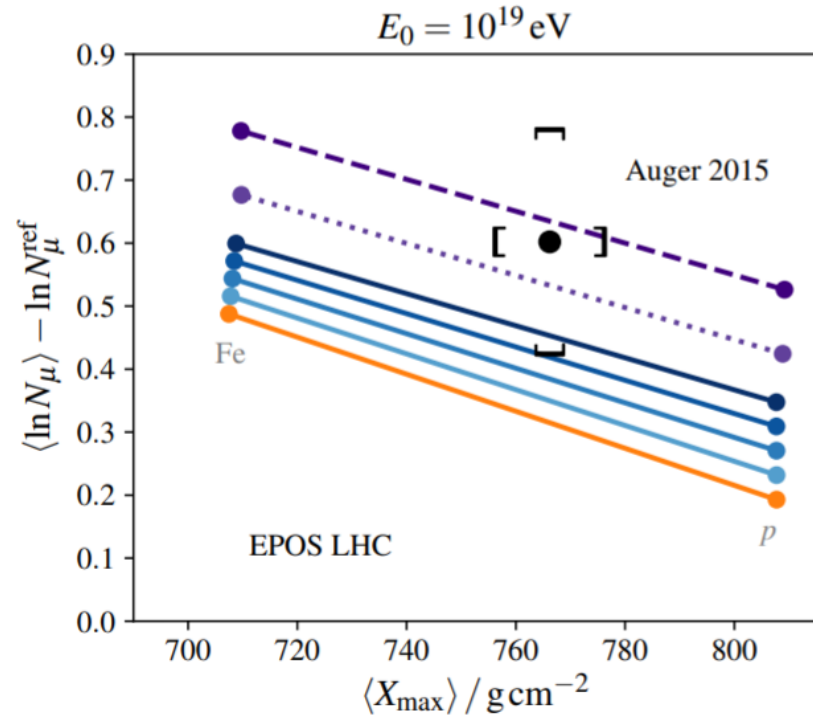
CMS, Eur.Phys.J. C79 (2019) no.11, 893;

p-p @ 13 TeV



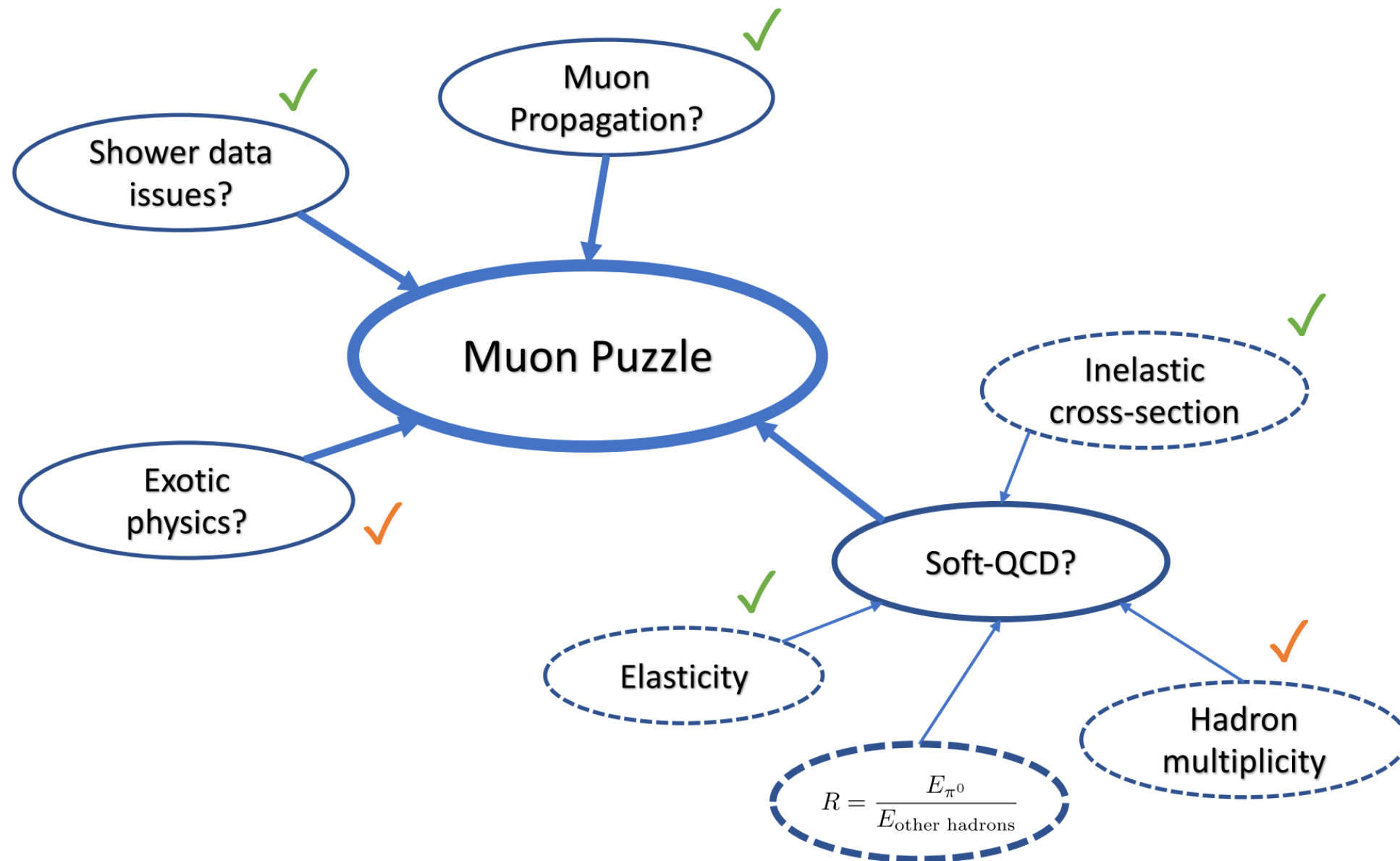
Another possibility is the (mis-)understanding of strangeness at high energy

S. Baur et al., arXiv:1902.09265



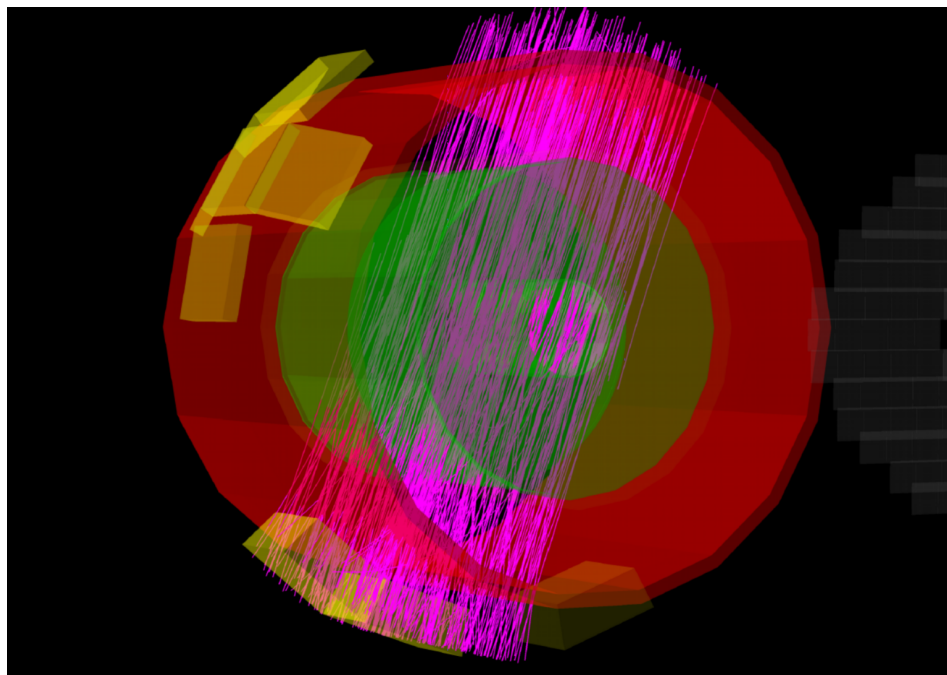
- Toy model with statistical hadronization (core) in addition to string/remnant fragmentation (corona)
 - Statistical hadronization needed to describe strangeness enhancement seen by ALICE
 - Can close muon number gap number in air showers and matches faster increase with energy
- Constrained by CMS-CASTOR measurements of R
- Can be tested further with data on forward strangeness production from LHCb and LHCf

The Muon Puzzle

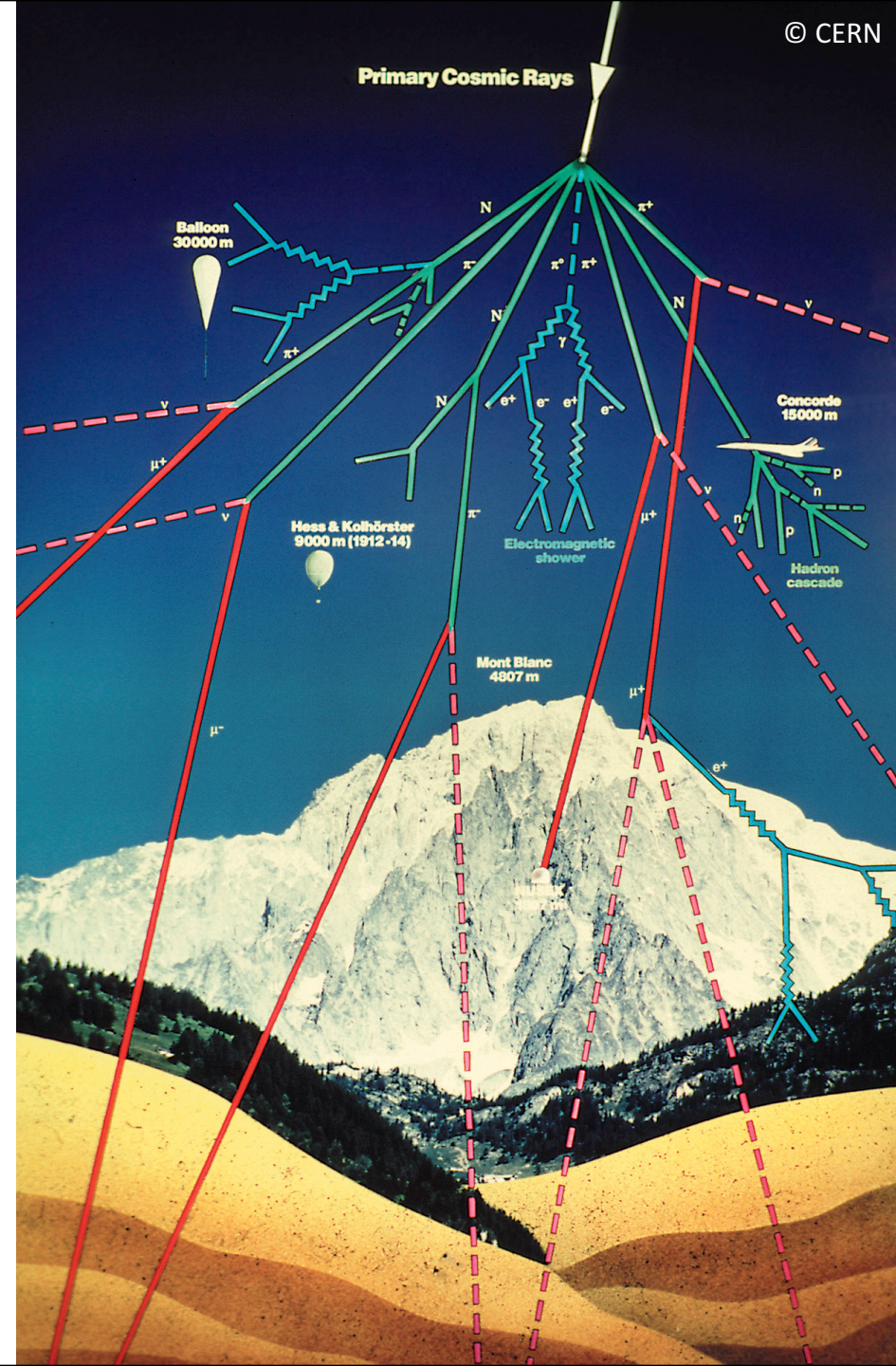


Inclusive atmospheric muons

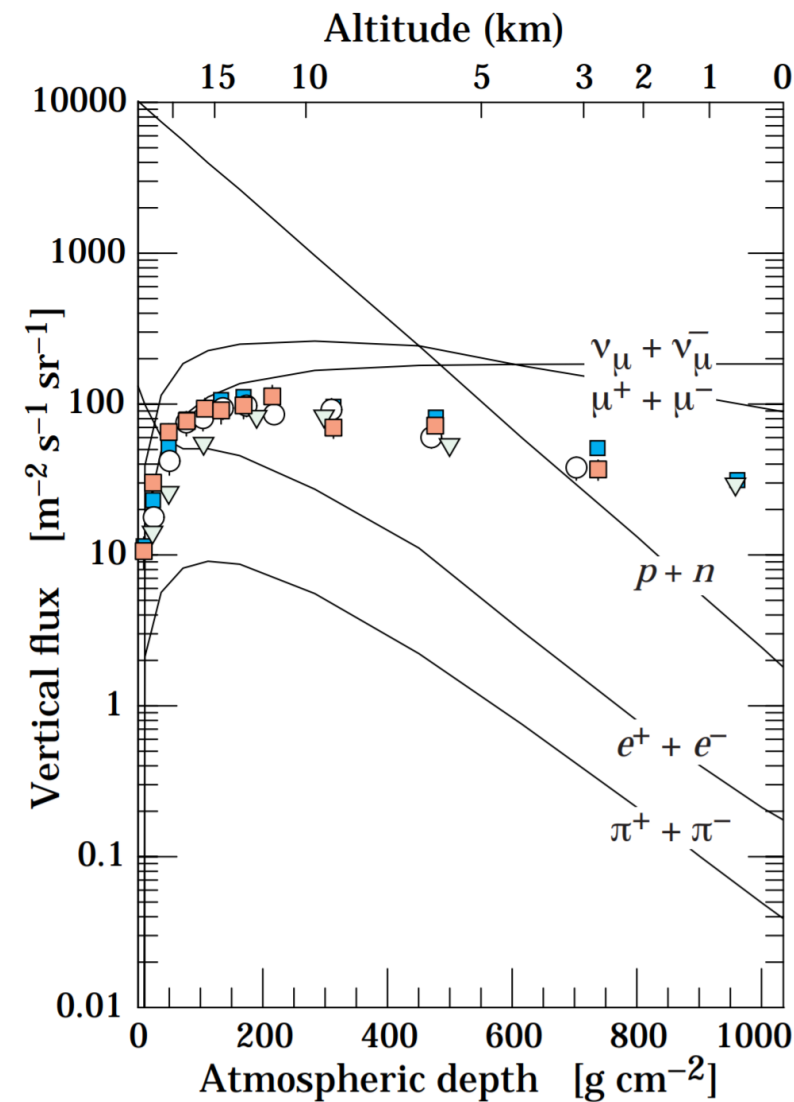
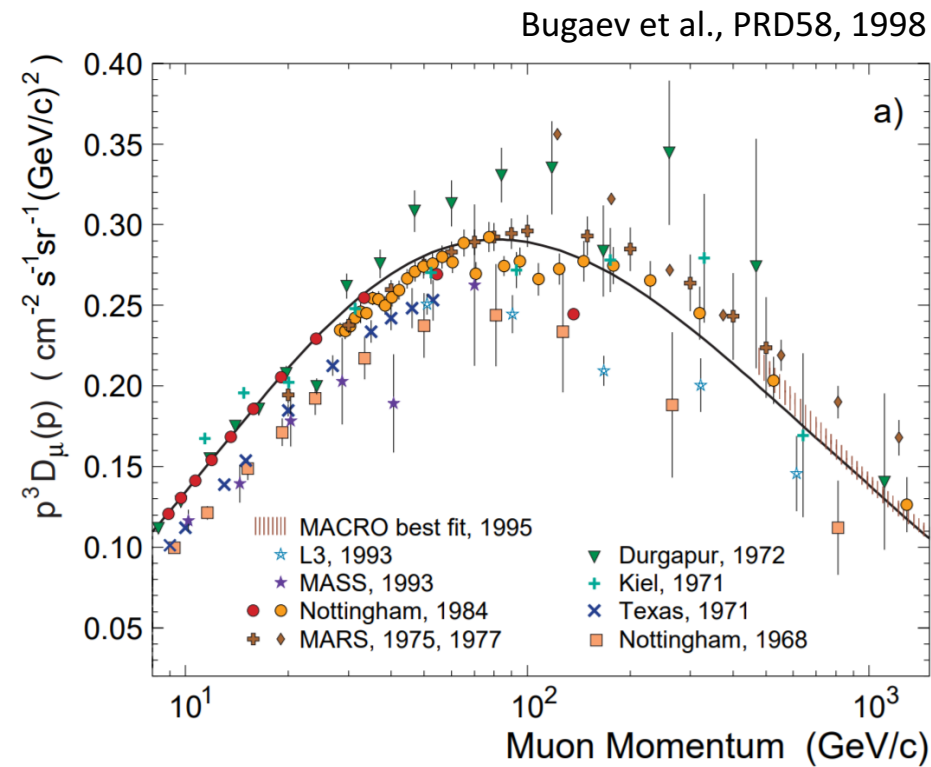
ALICE Collaboration



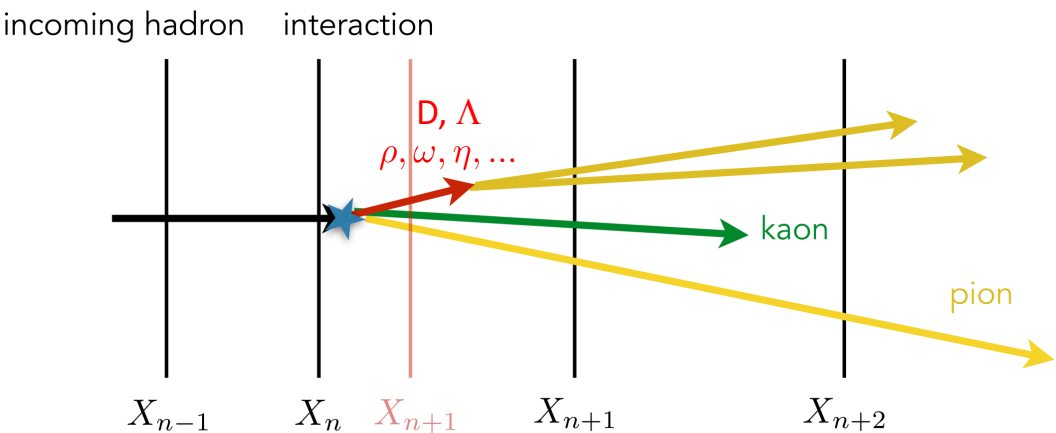
- **Muon bundle:** muons within a single air showers
- **Inclusive muons:** Each atmospheric muon counted individually (integral over many showers)



Muon fluxes in the atmosphere



Hadronic components

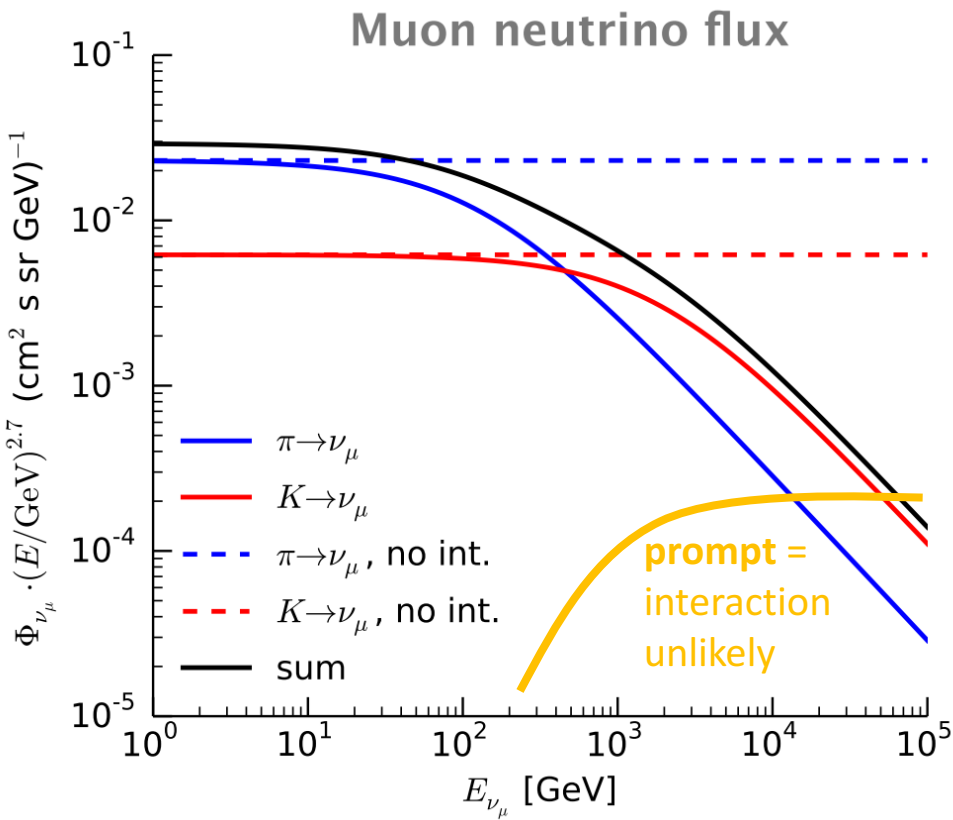


conventional
 $p, A + \text{air} \rightarrow \pi^\pm, \pi^0, K^\pm, K_{S,L}^0$

muons and muon neutrinos
 $\pi^\pm, K^\pm \rightarrow \mu^\pm \nu_\mu (\bar{\nu}_\mu)$

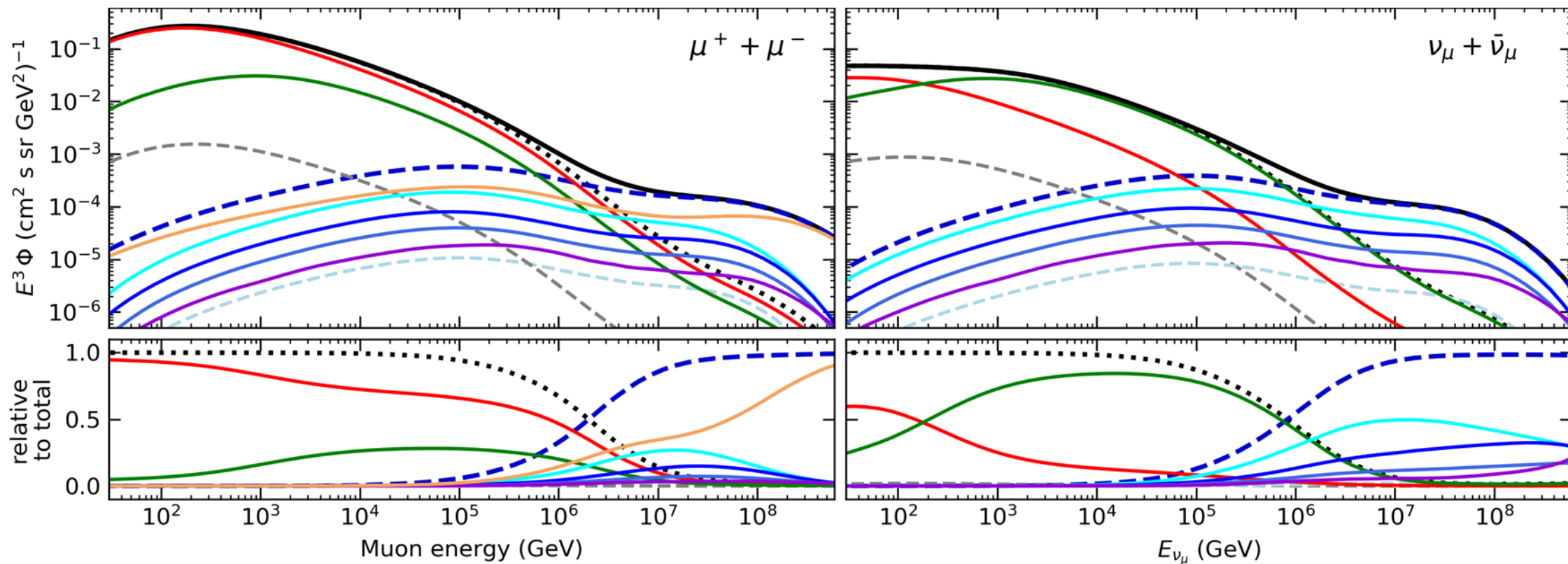
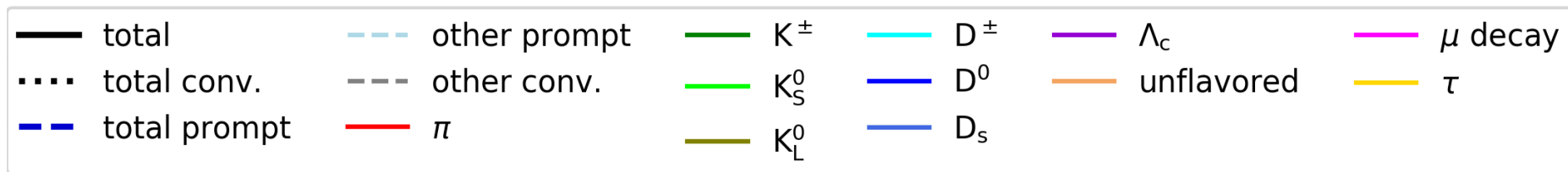
electron neutrinos
 $K^\pm, K_L^0 \rightarrow [\pi^\pm, \pi^0] e^\pm \nu_e (\bar{\nu}_e)$

prompt
 $p, A + \text{air} \rightarrow D, \Lambda_C \rightarrow \nu_\mu, \nu_e, \mu$



High-energy mesons live long enough to interact → **Spectral steepening**

Spectral and angular distribution related to



Building a bridge to particle physics at accelerators

For atmospheric leptons

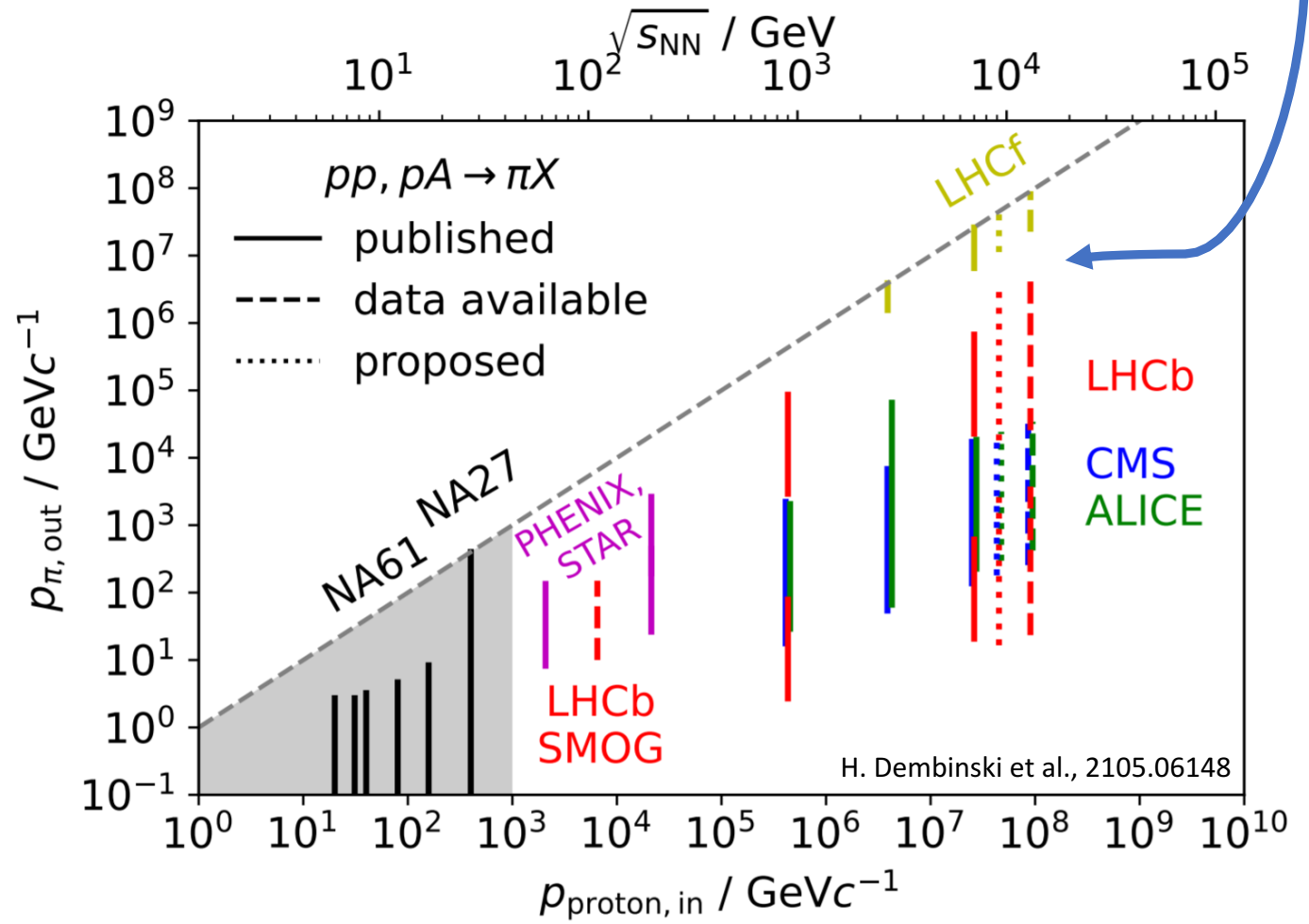
$$p_z \sim \text{TeV} - \text{PeV}$$

$$p_T \sim \text{few GeV}$$

$$\theta \sim \mu\text{rad}$$

$$x_{\text{lab}} = \frac{E_{\text{secondary}}}{E_{\text{primary}}} \approx \frac{p_{z,\text{secondary}}}{E_{\text{primary}}}$$

$$x_{\text{lab}} > 0.1, \quad \eta \rightarrow \infty$$



Building a bridge to particle physics at accelerators

For atmospheric leptons

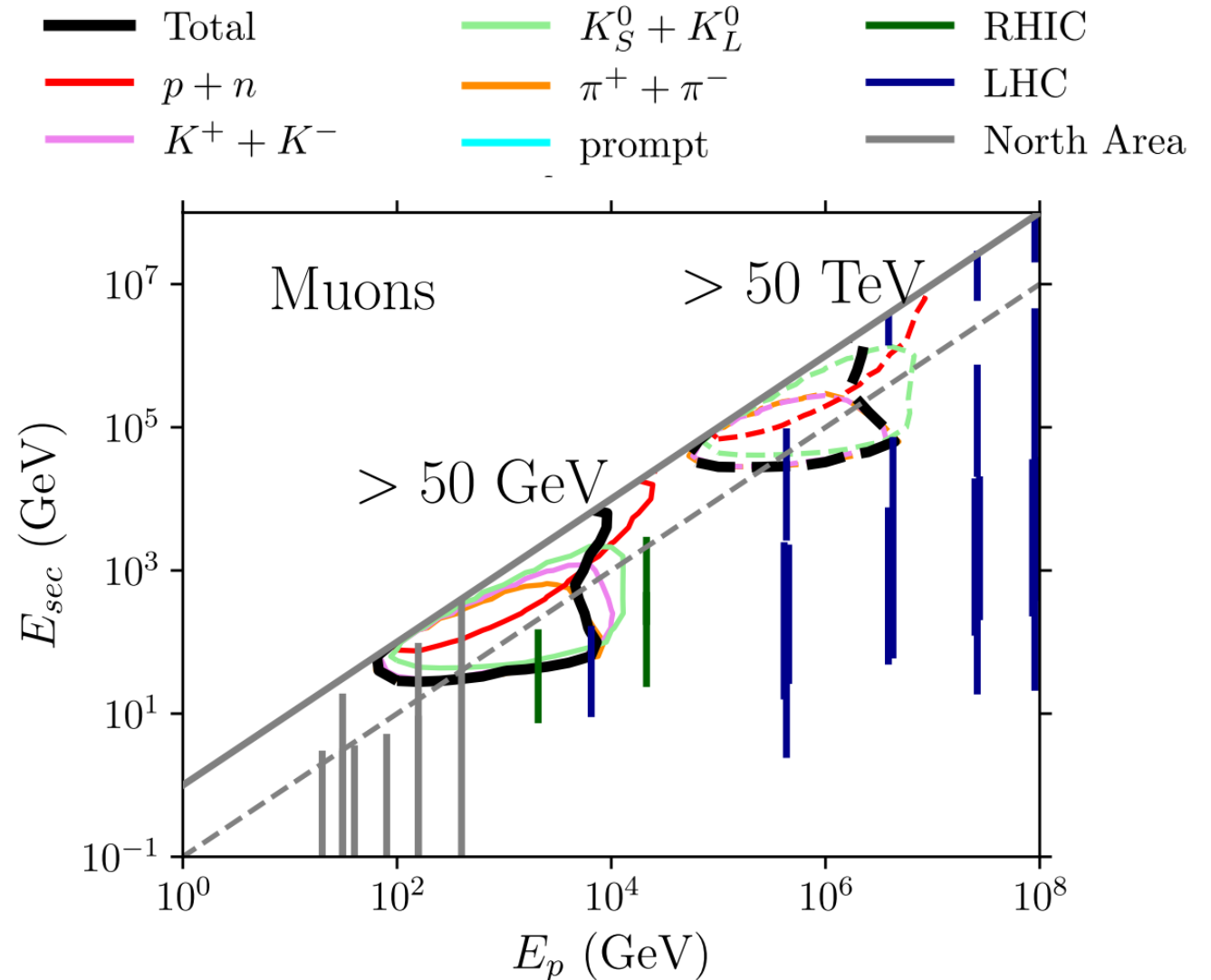
$$p_z \sim \text{TeV} - \text{PeV}$$

$$p_T \sim \text{few GeV}$$

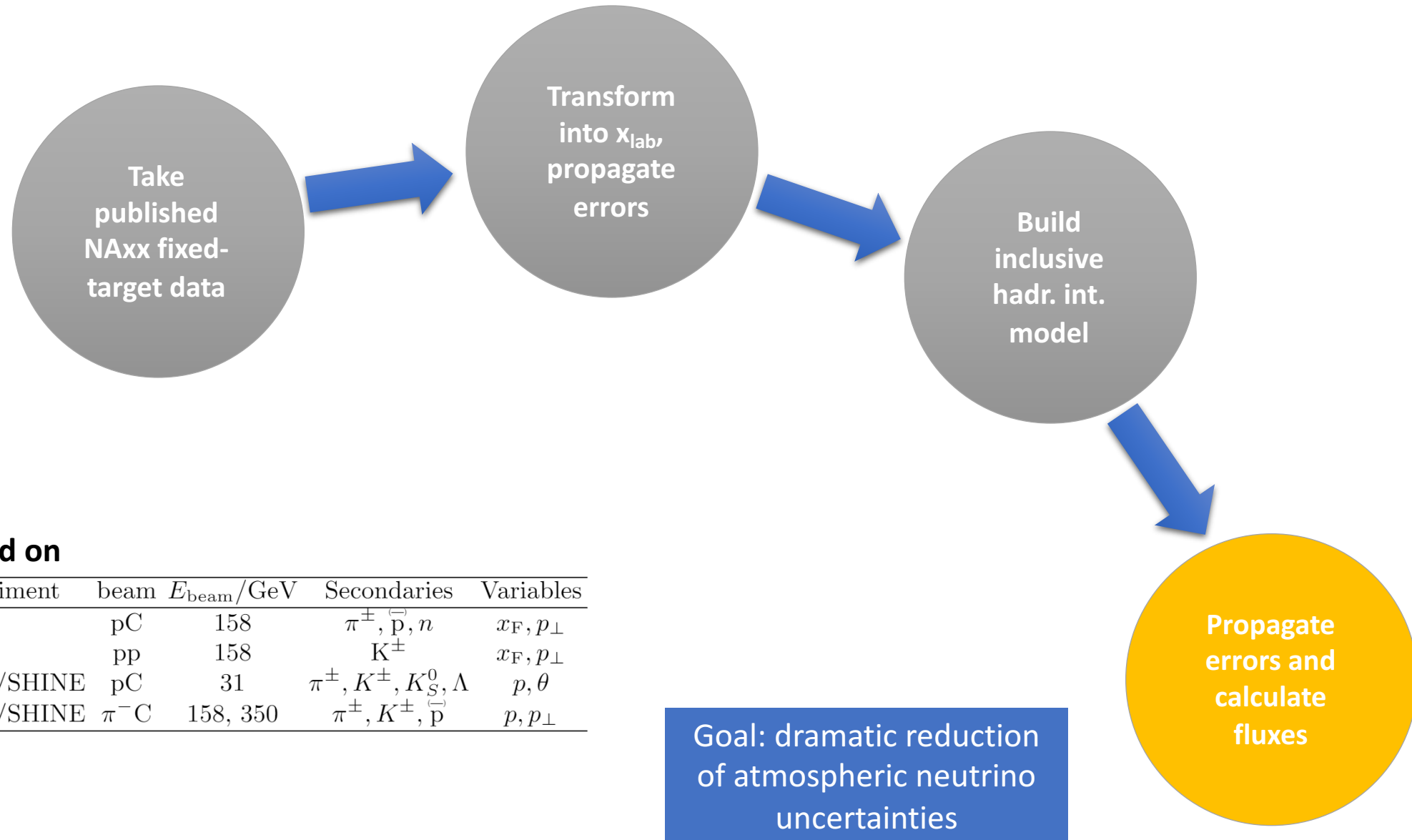
$$\theta \sim \mu\text{rad}$$

$$x_{\text{lab}} = \frac{E_{\text{secondary}}}{E_{\text{primary}}} \approx \frac{p_{z,\text{secondary}}}{E_{\text{primary}}}$$

$$x_{\text{lab}} > 0.1, \quad \eta \rightarrow \infty$$

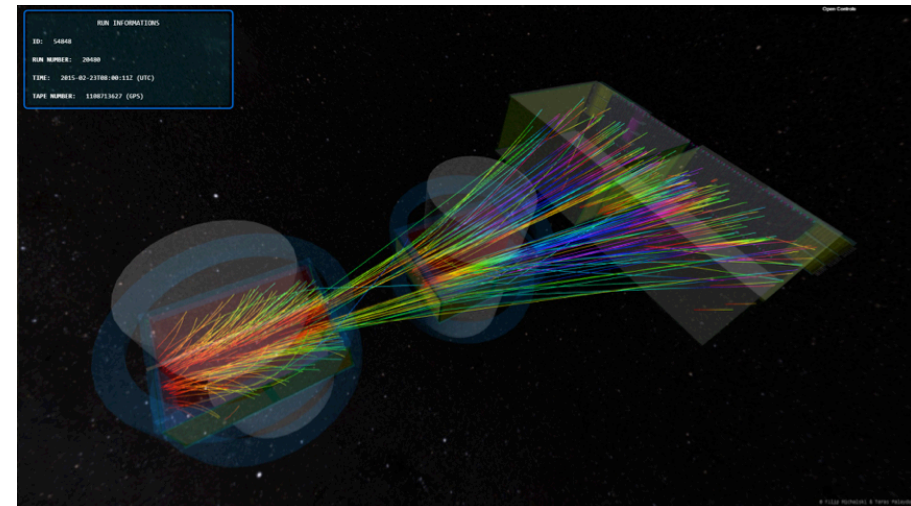
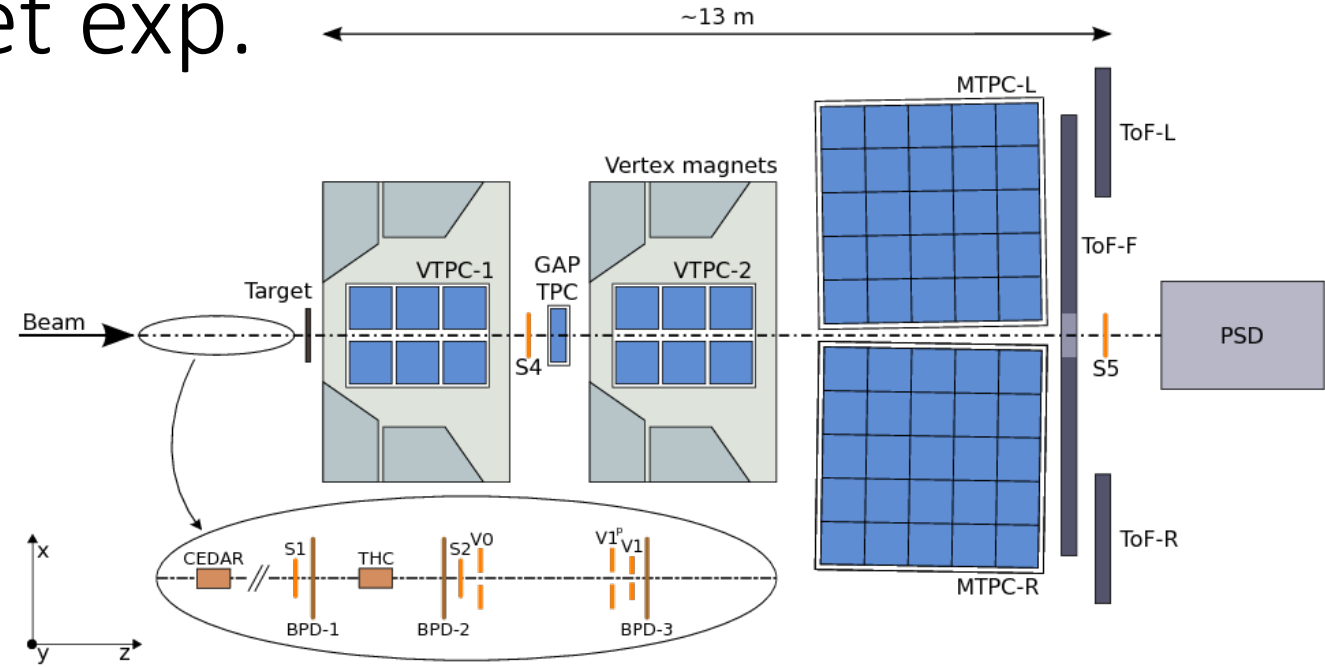
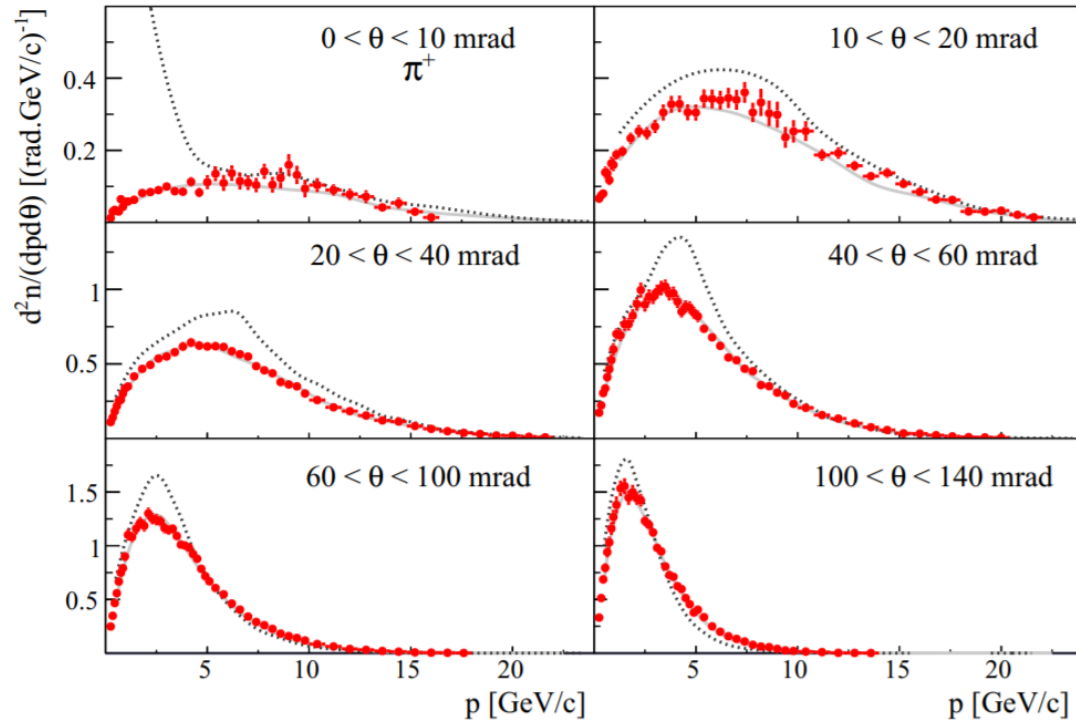


DDM: Data-Driven hadronic interaction Model



NA61/SHINE fixed-target exp.

Proton on carbon, 31 GeV, NA61, EPJ 76, 2016

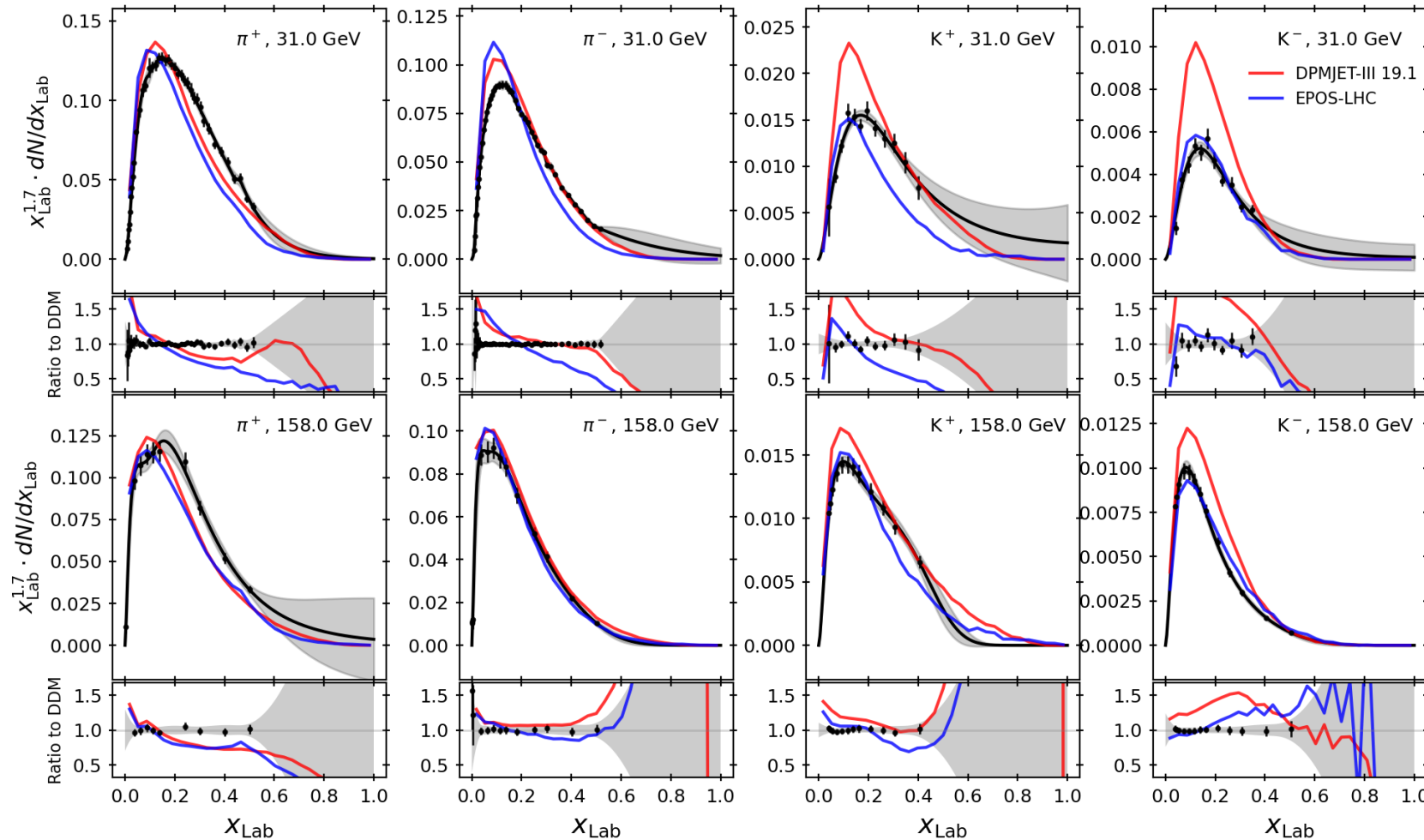


Courtesy of CERN (home.cern)

Fits to proton-carbon data

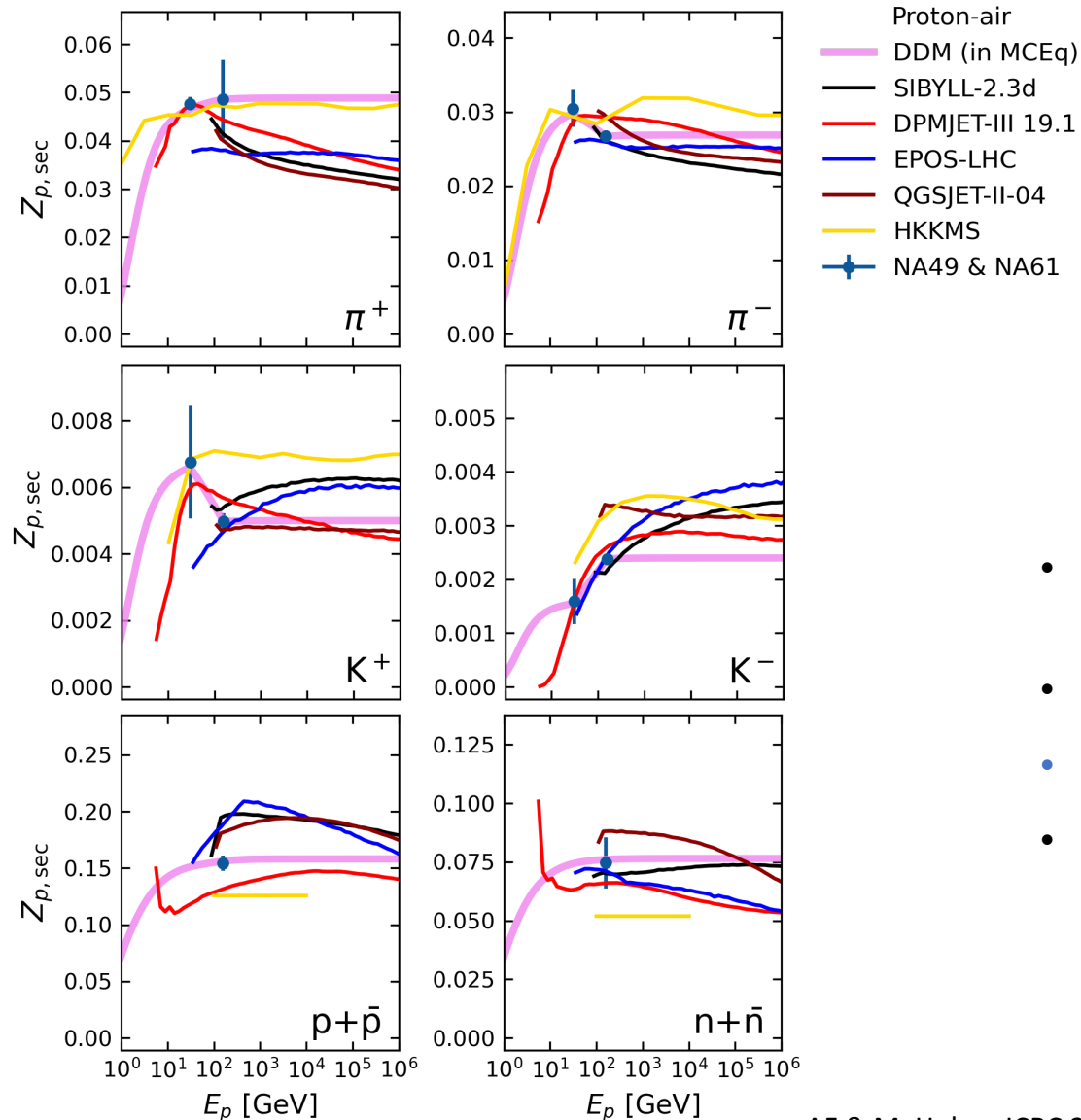
NA49 & NA61 proton-carbon

AF & M. Huber, ICRC 2021 & in prep.



- **Conservative uncertainties consistently scale up** in absence of forward data
- Models weak for π^+ (both energies) and K^- at 158 GeV
- K^+ - data at 158 GeV corrected from $pp \rightarrow pC$
- Carbon to air correction < 1%

Benchmark against post-LHC interaction models

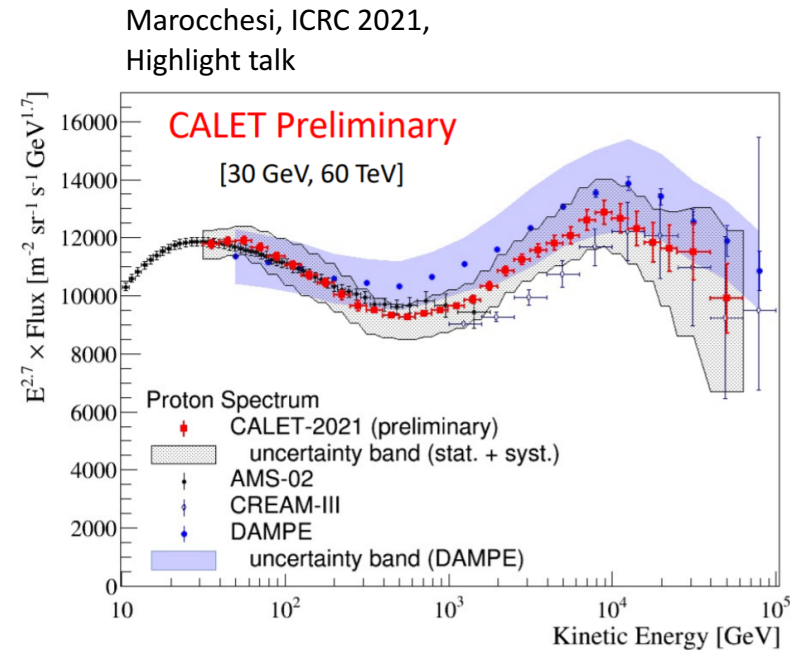
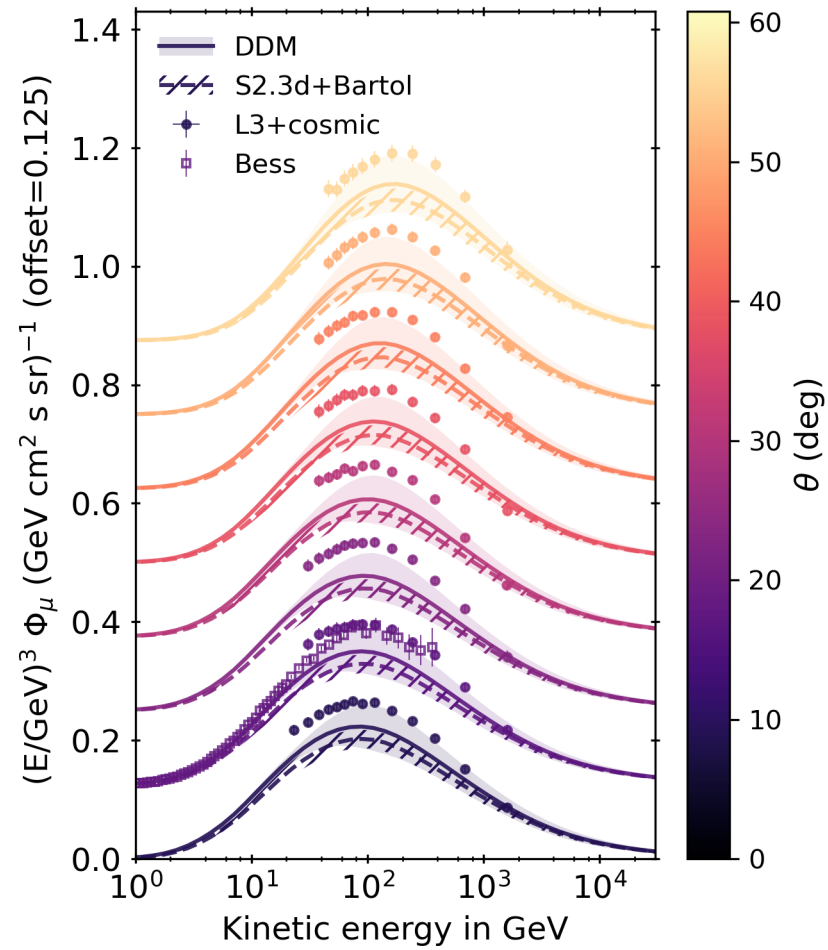


Spectrum-weighted moments:

$$Z_{N\pi} = \int_0^1 x_L^{\gamma-1} F_{N\pi}(x_L) dx_L = \int_0^1 x_L^{\gamma} \frac{dn_{\pi}}{dx_L} dx_L$$

- The spectrum weighted moments (Z-factors) are integrated particle production yields
- Represent particle production in relevant phase space
- **Assumption in DDM: Feynman scaling** beyond 158 GeV
- Higher-energy data from NA59 and intermediate energies from NA61 can be included in future

Results of the high-precision calculation



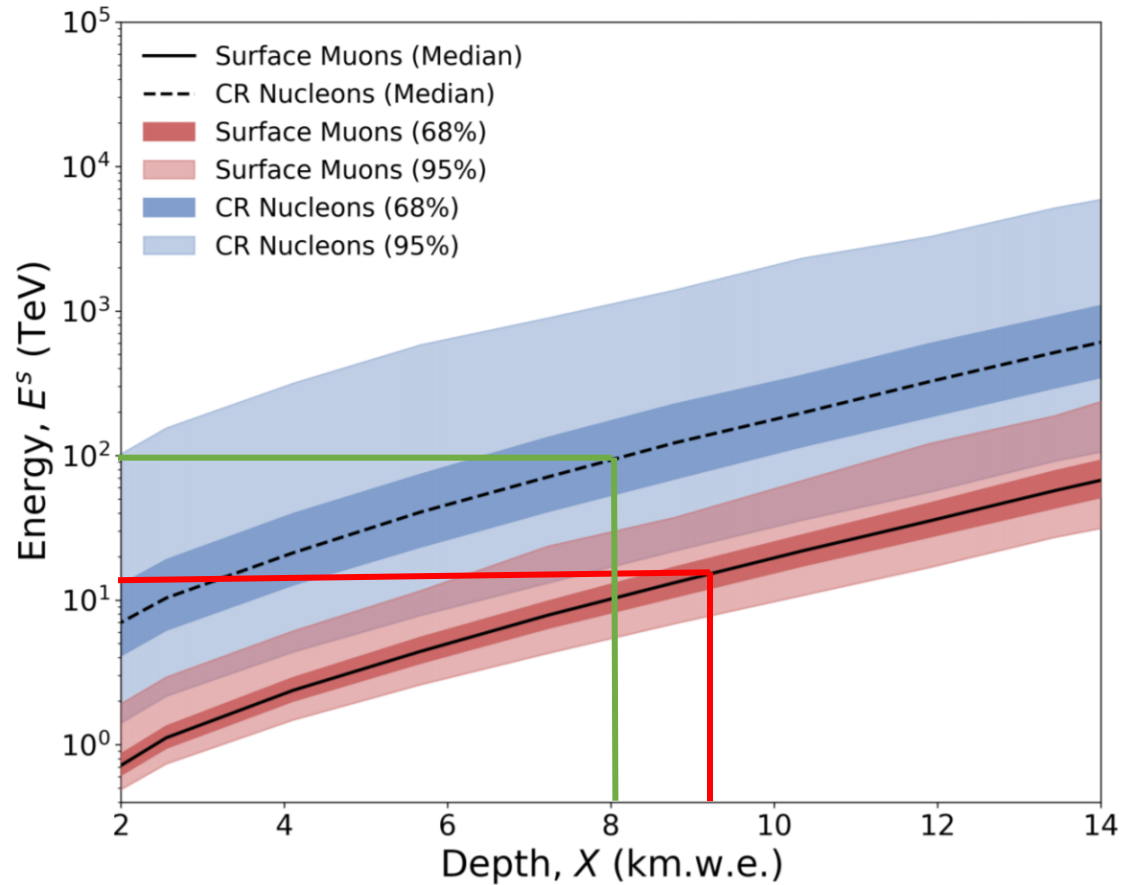
- Deviation in vertical fluxes
- Barely compatible within uncertainties
- Fitting to data imposes pulls of 2-5 sigma on the NA49/61 data
- May strongly indicate that the **direct cosmic ray measurements are not as well known as believed**
- Or processes missing that are larger than believed:
 - Photo-hadronic
 - Quasi-elastic VM production
 - ?

Summary

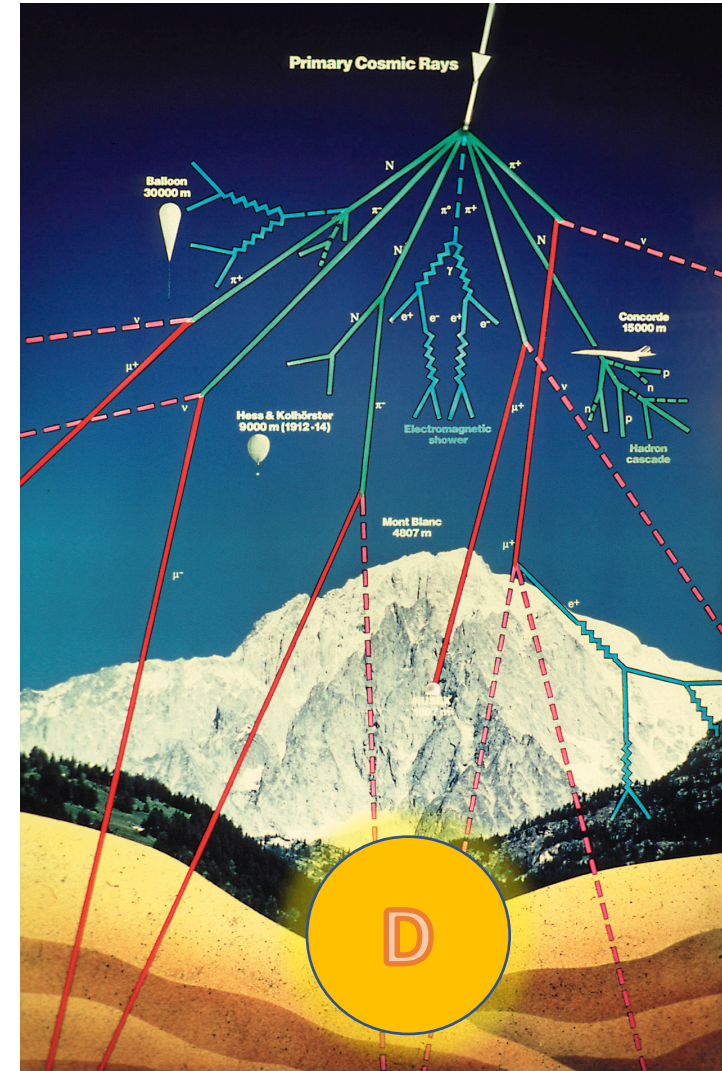
- **The Muon Puzzle is real** with significance > 8 sigma
- Origin is still unclear and is likely related to intermediate (LHC) energies
- Possible explanations: strangeness at high energy or “density”, non-perturbative effects, non-universality of string fragmentation, and new physics
- At IOP, I aim to launch a project to improve/rewrite the DPMJET-III hadronic interaction model to test new ideas. International collaborators, tools and know-how are available
- Inclusive atmospheric leptons show also a discrepancy with data but very likely of different origin
- None the less, atmospheric neutrino flux uncertainties have been significantly reduced
- Systematic differences between space-borne cosmic ray detectors may explain these differences

Very high-energy muons

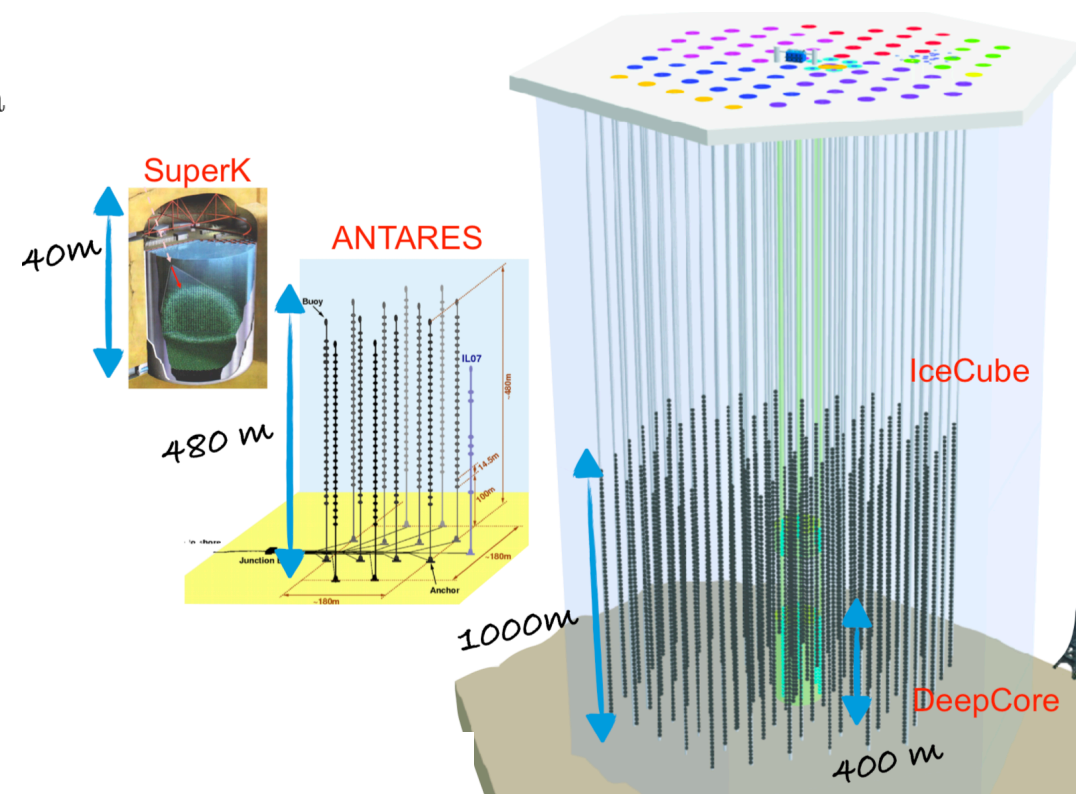
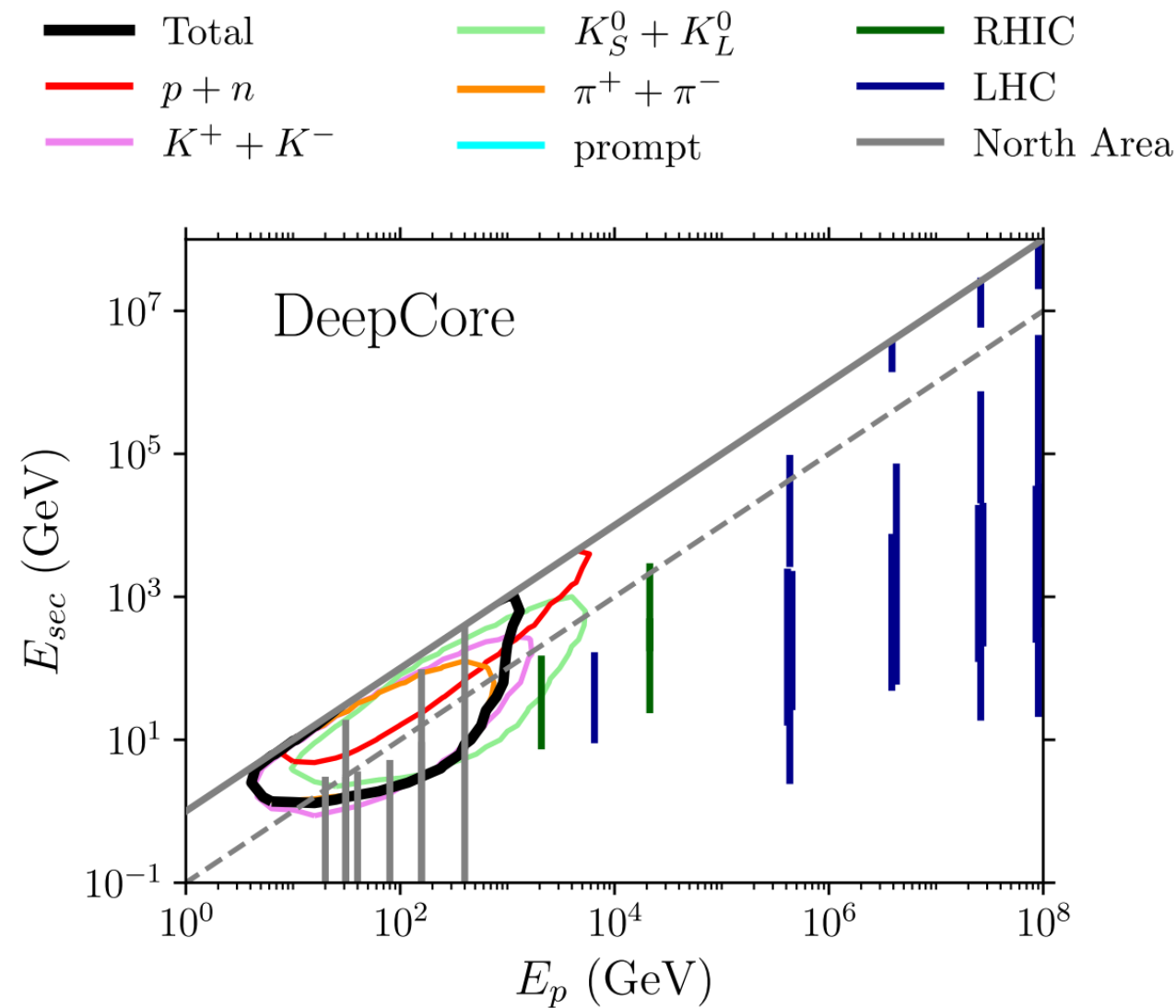
W. Woodley, AF, M.-C. Piro, ICRC 2021



Probe interactions at multi-TeV energies (lab)

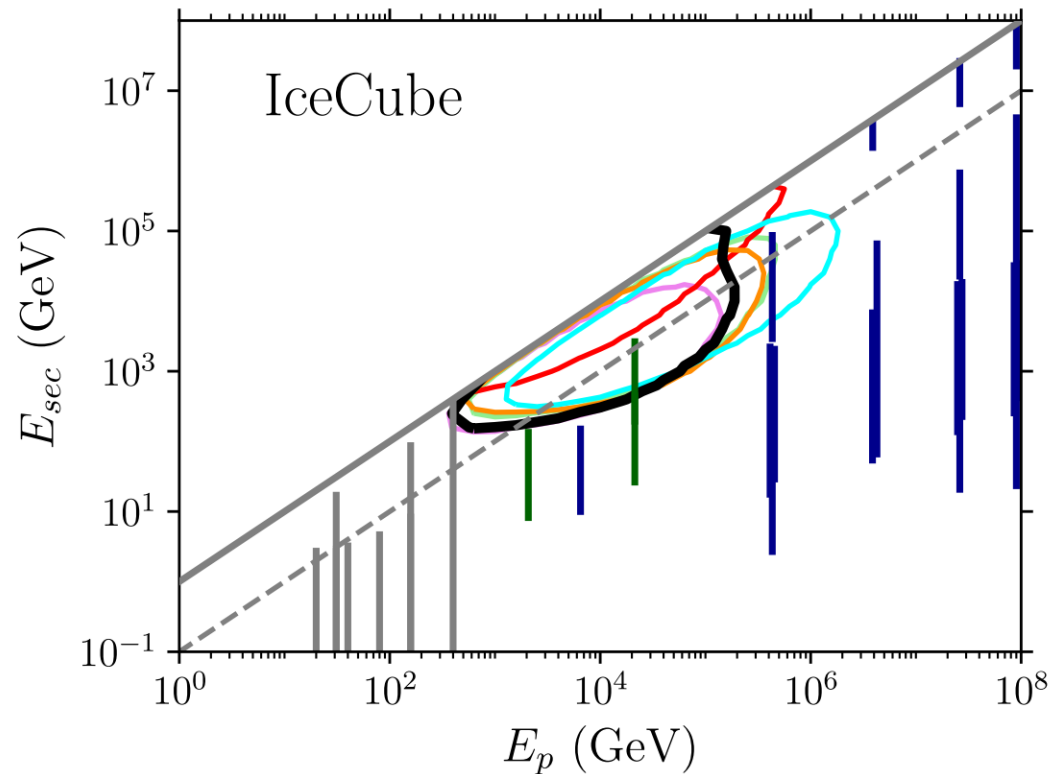


GeV-neutrinos, an energy range covered by accelerator data

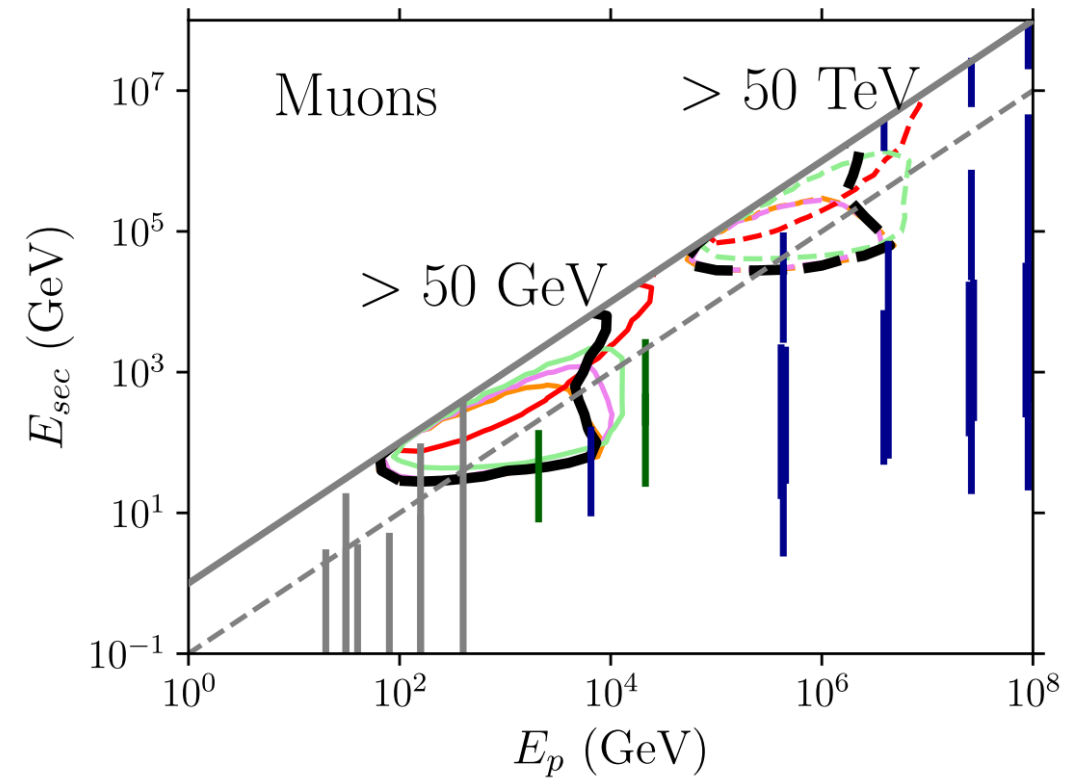


Chances to probe the “blind spot” of colliders

High-energy atmospheric neutrinos

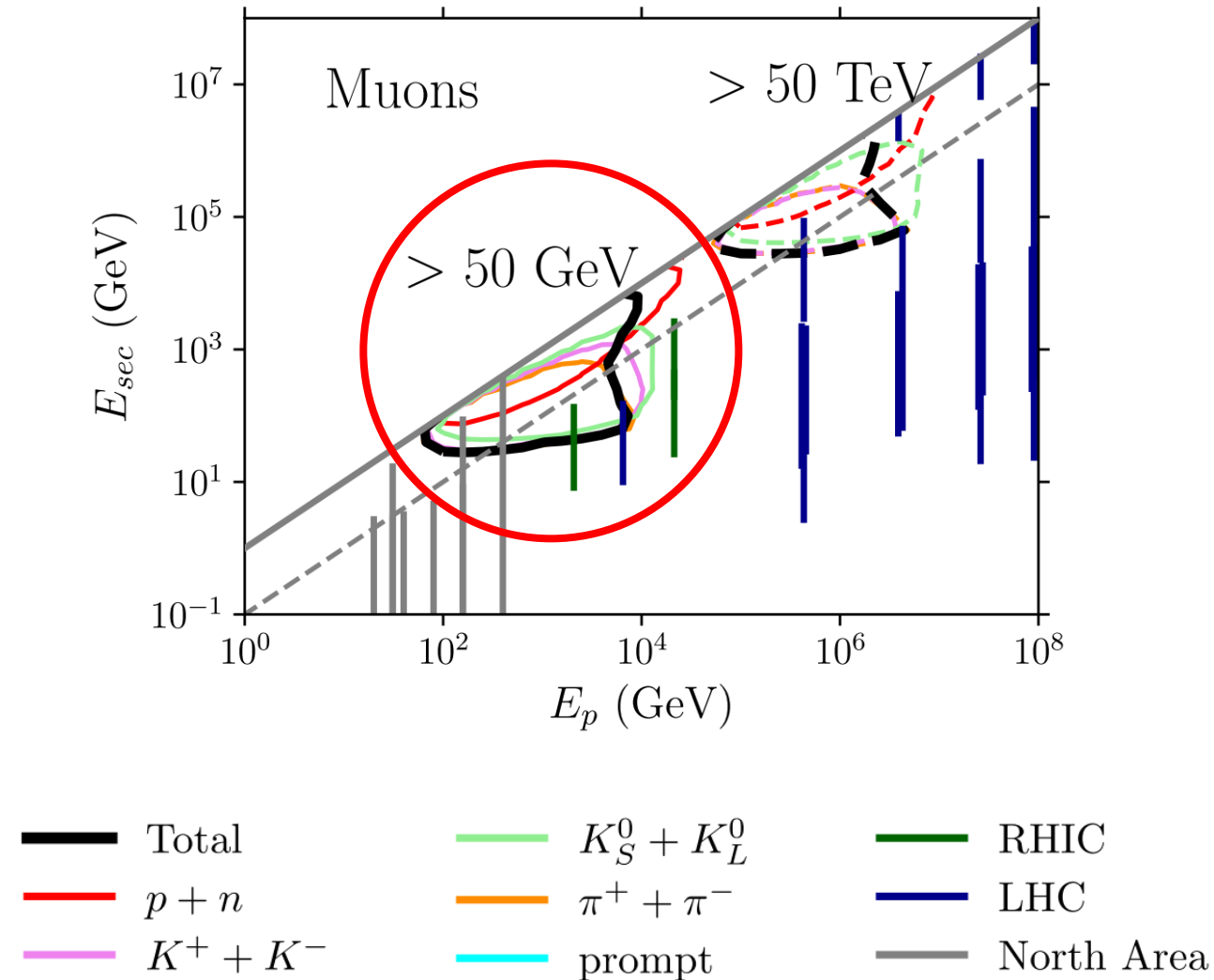


High-energy atmospheric underground muons

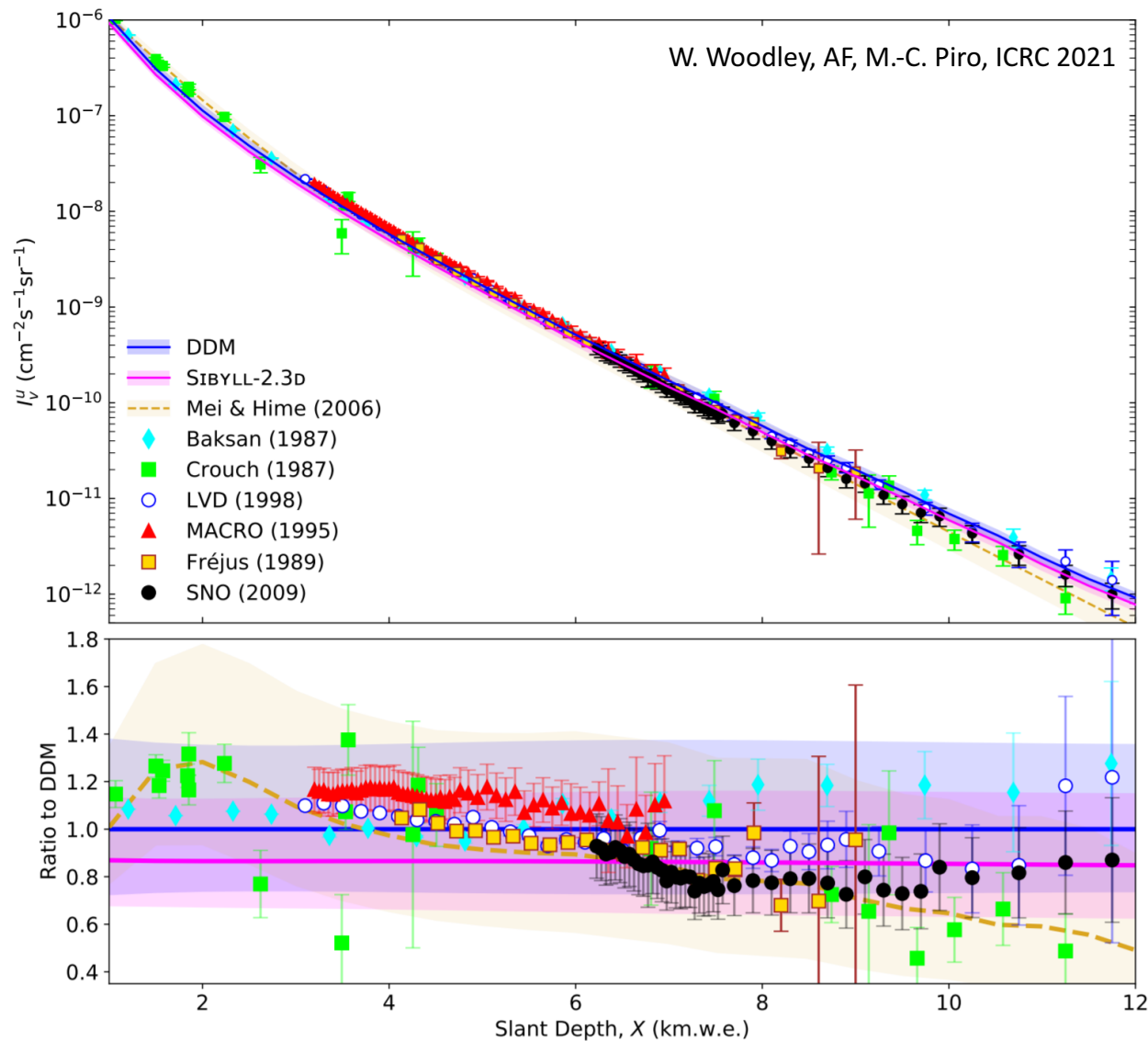


- | | | |
|---------------|-------------------|--------------|
| — Total | — $K_S^0 + K_L^0$ | — RHIC |
| — $p + n$ | — $\pi^+ + \pi^-$ | — LHC |
| — $K^+ + K^-$ | — prompt | — North Area |

The disagreement can be studied within the
“comfort zone”



Accurate calculation of deep-underground muons



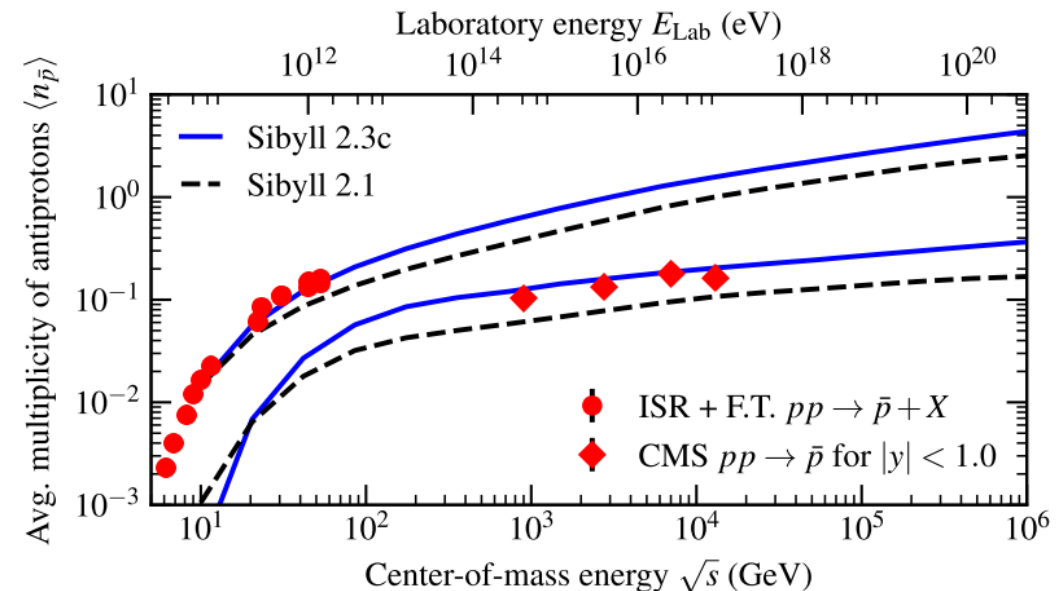
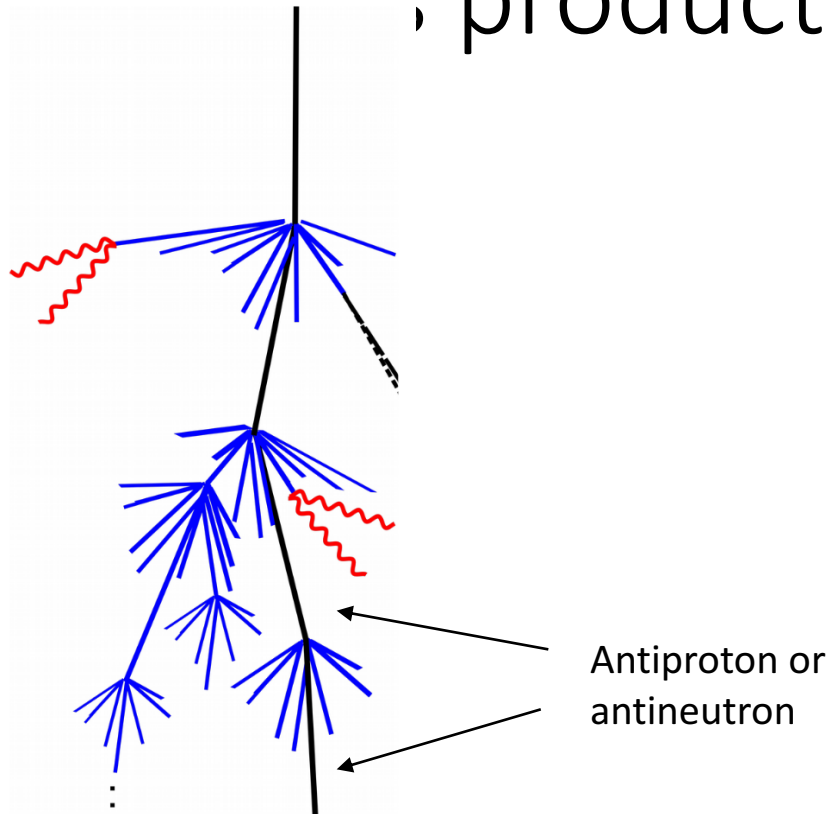
- Calculation uses MCEq and PROPOSAL ← a TUDO product!
- Calculation is fast → possible to be used in a fit
- Constrains neutrino fluxes at energies relevant for:
 1. Neutrino cross section measurement
 2. Sterile neutrino searches
 3. Astrophysical flux characterization

More low-energy muons through anti-baryons production

F. Riehn, R. Engel, AF, T. Gaisser, T. Stanev
[arXiv:1912.03300](https://arxiv.org/abs/1912.03300)

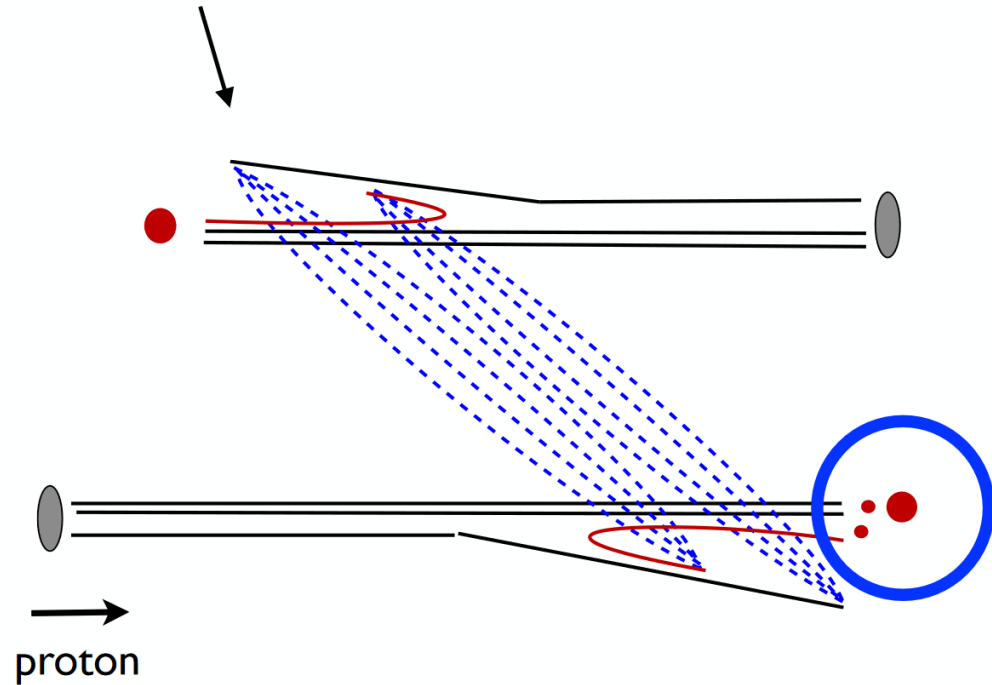
Baryon number conservation results in cascade regeneration:

- Each interaction yields at least one baryon
- These baryons re-interact, producing more pions
- Production was off in older models

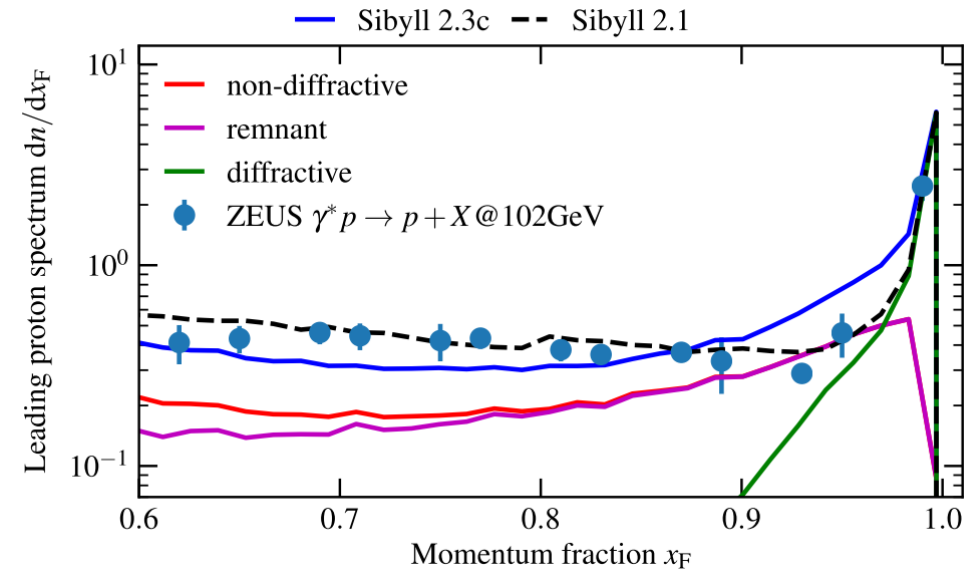
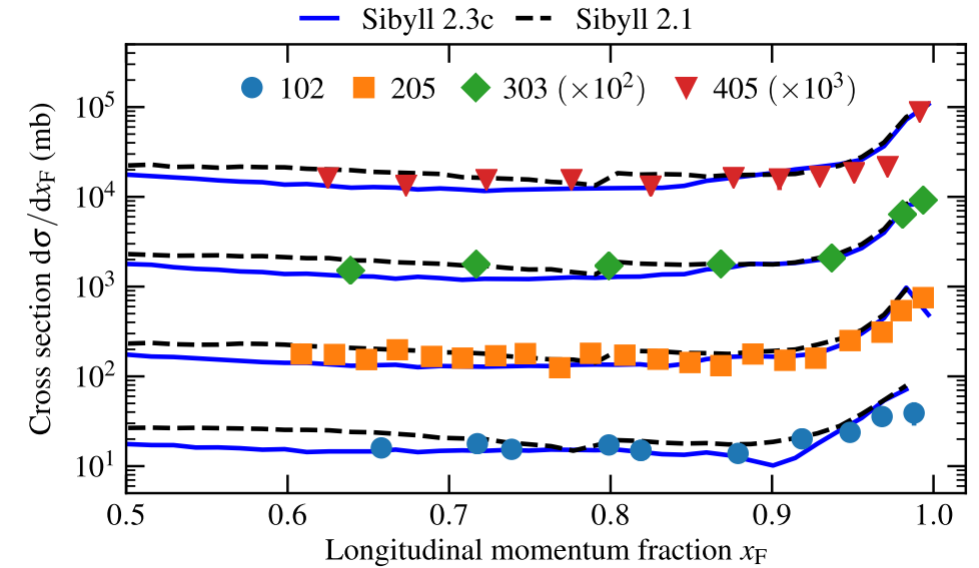


Leading particles

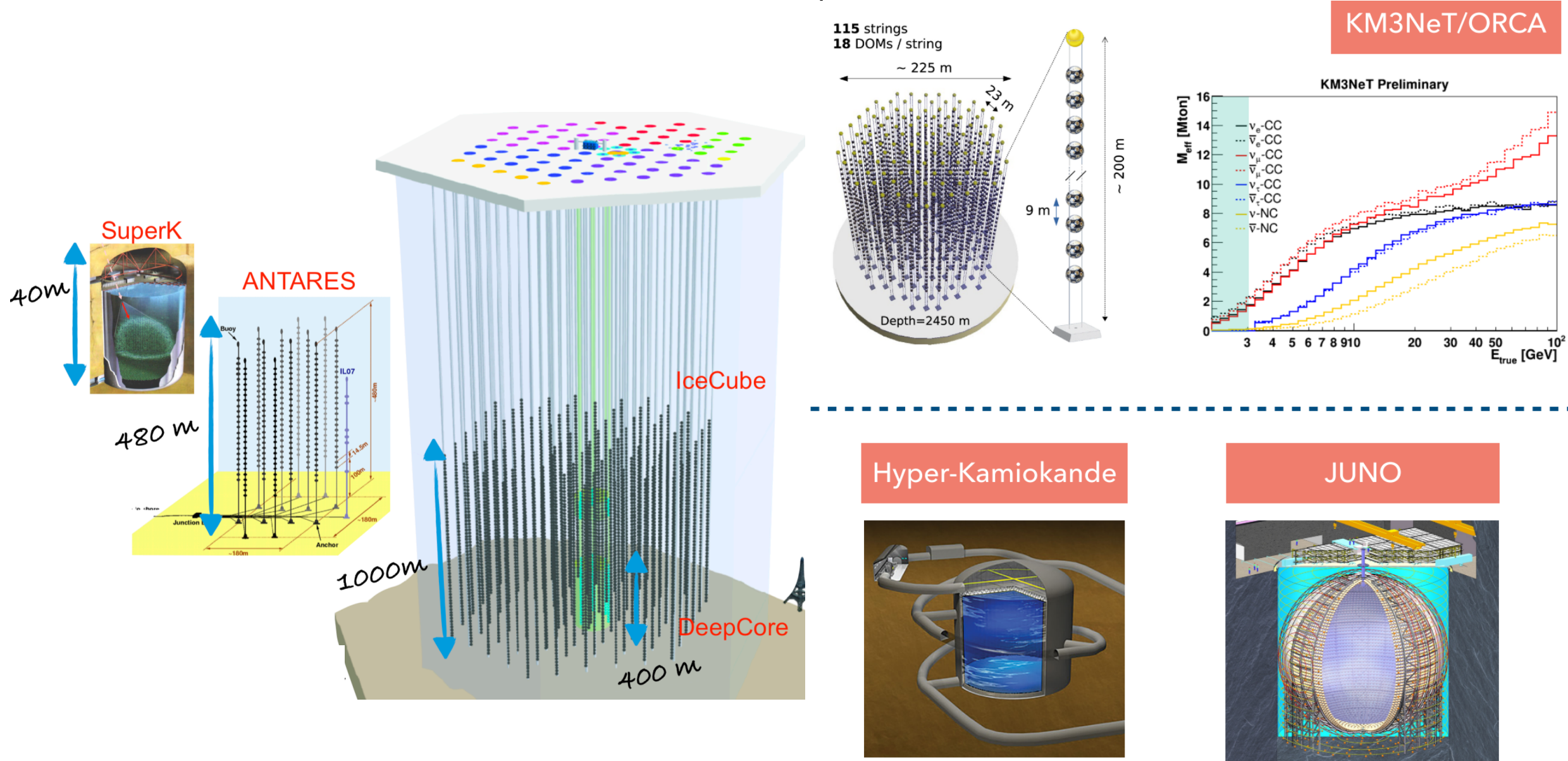
Model-dependent distributions of momentum given to partons



Fluctuations: Generation of sea quark anti-quark pair and leading/excited hadron



Difference to the late-90's: modern atmospheric neutrino detectors



Muon fluxes in the atmosphere

Equations for fluxes of particles of type h in the atmosphere:

$$\frac{d\Phi_h(E, X)}{dX} =$$

- absorption by **interactions**

- absorption by **decays**

- ionization and radiation **losses**

Depend on density or X

+ particle production in **hadronic interactions**

+ particle production through decays

Coupling between particle types

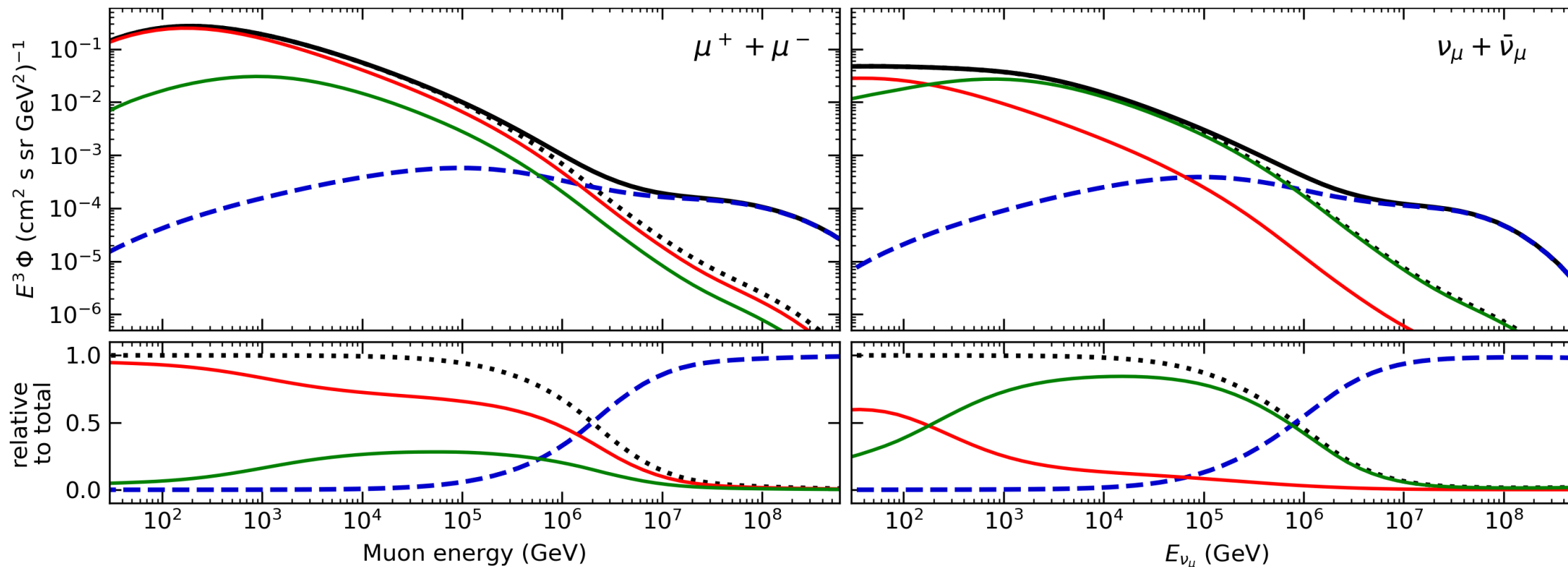
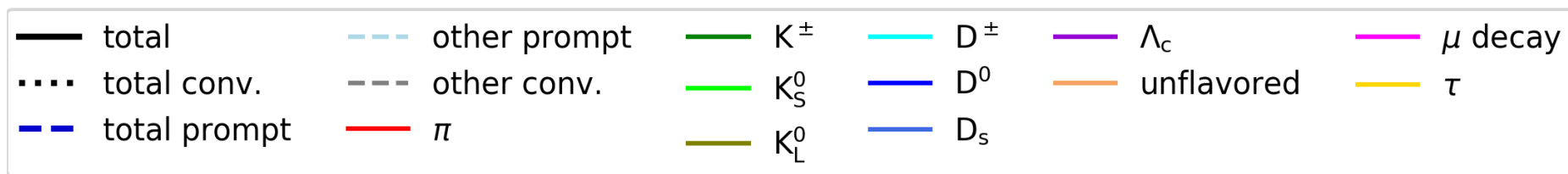
Depth along CR trajectory l :

$$X(h_0) = \int_0^{h_0} d\ell \, \rho_{\text{air}}(\ell)$$

Initial condition is the flux of cosmic ray nucleons at $X=0$.

50

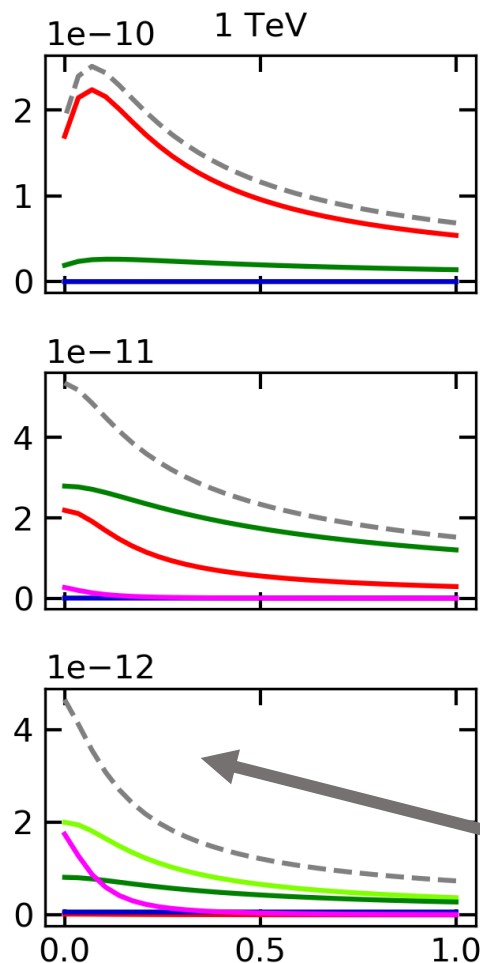
The reality is a bit more complicated



The zenith angle is an additional handle on hadronic components

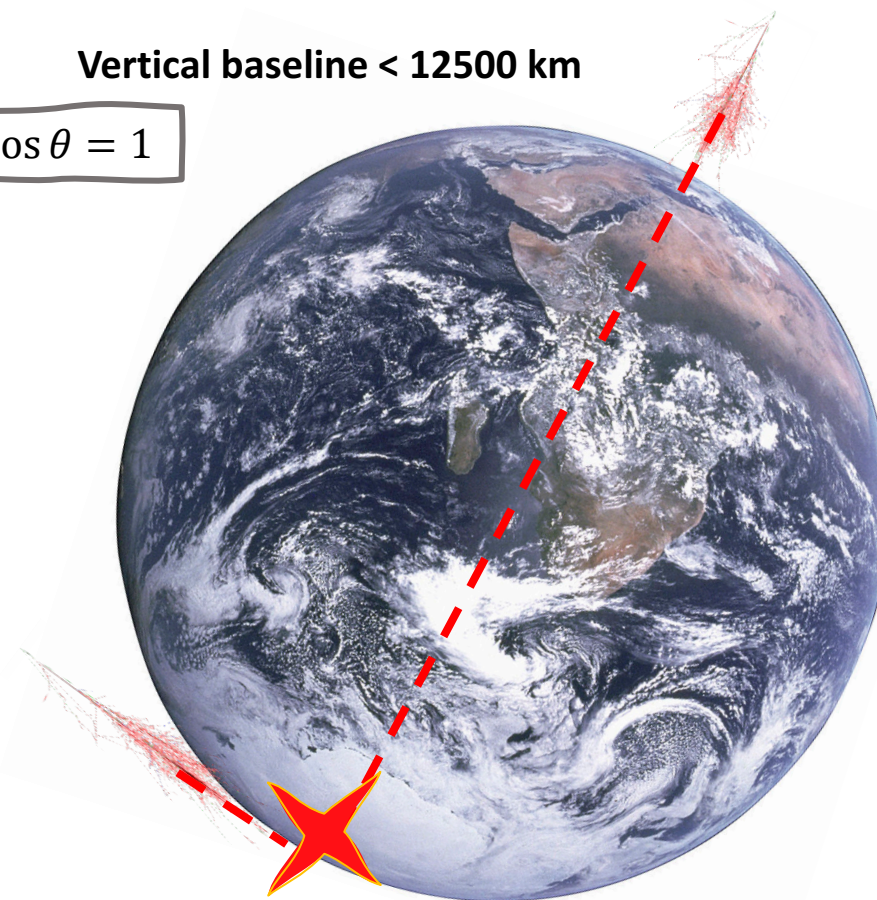
— from μ^\pm — from π^\pm — from K^\pm

horiz



vertical: $\cos \theta = 1$

Vertical baseline < 12500 km



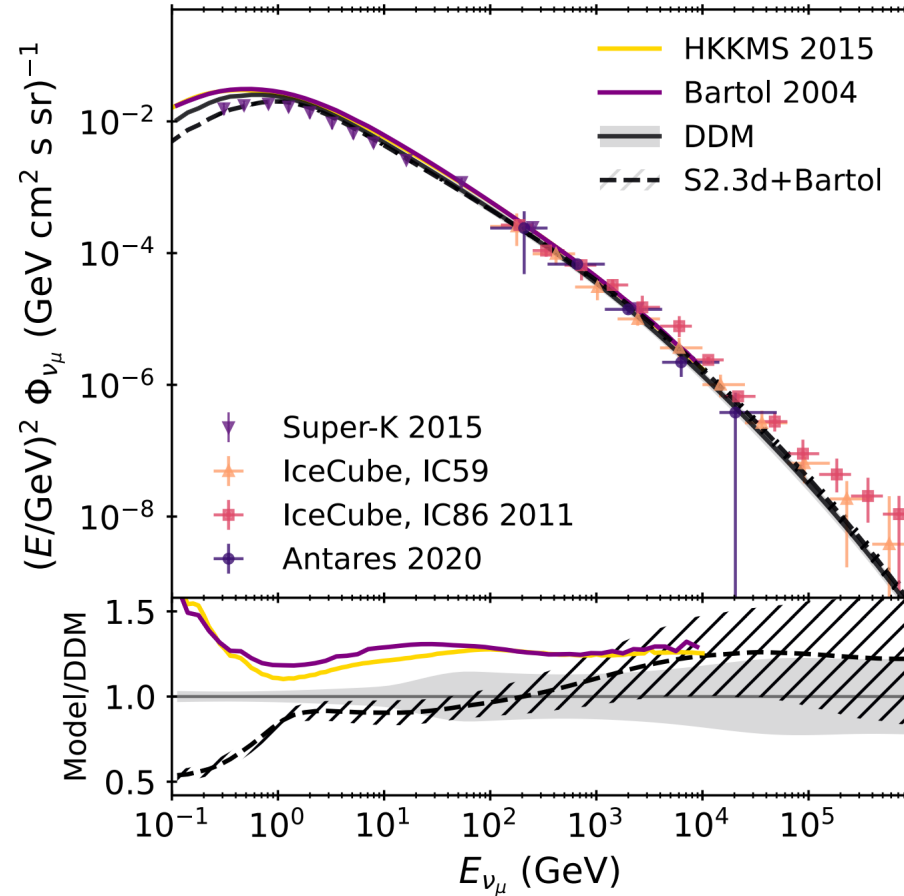
Horizontal baseline < 500 km

Various overlapping components

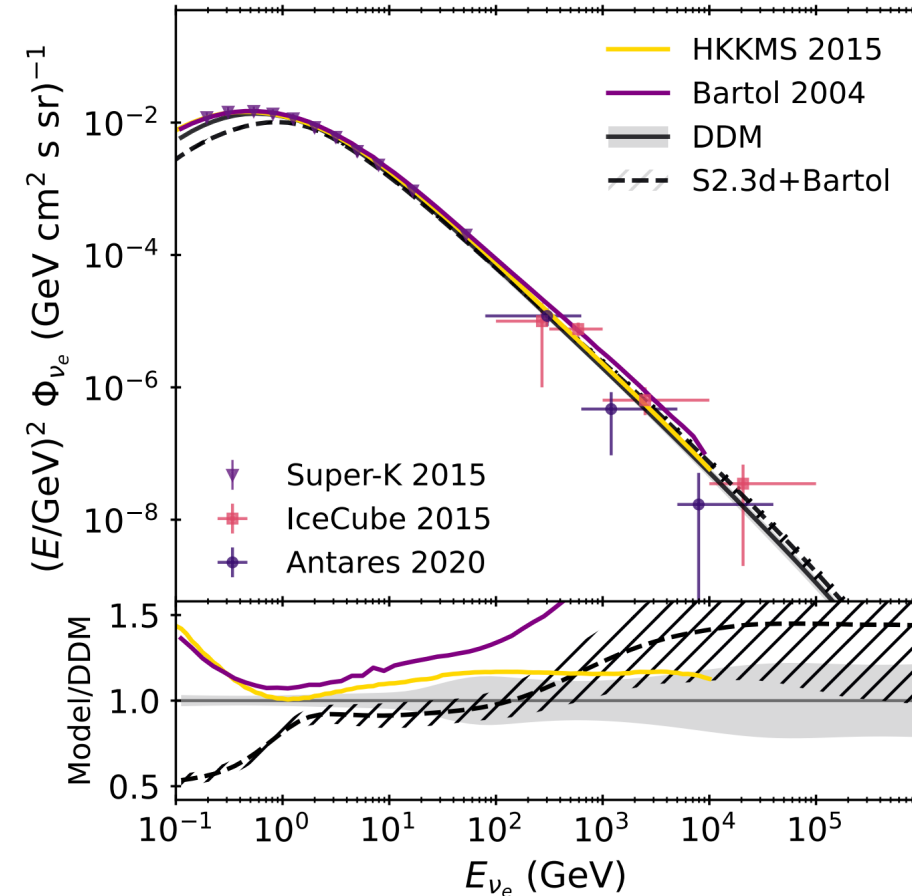
horizontal: $\cos \theta = 0$

DDM: conventional neutrino fluxes

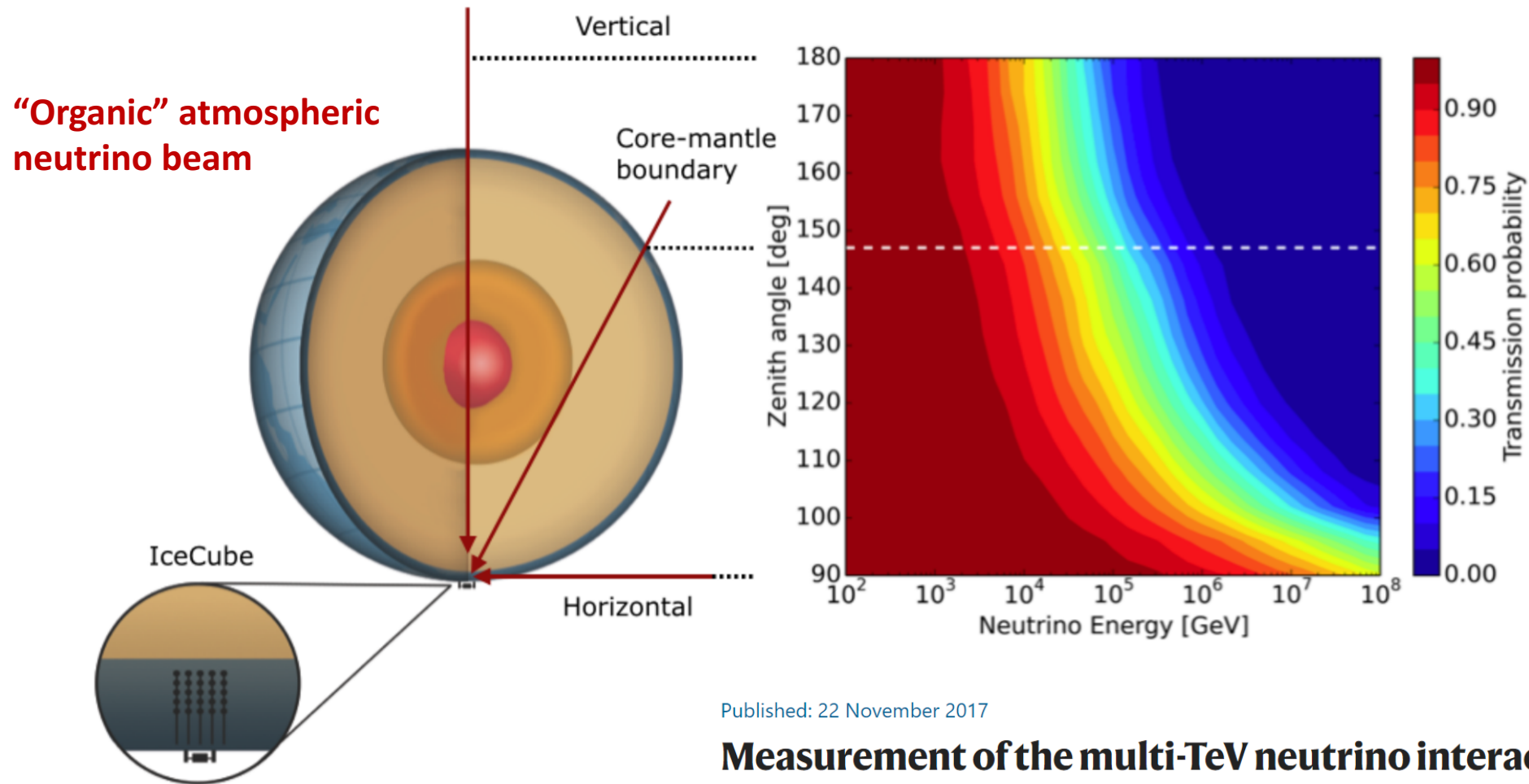
Muon neutrinos+antineutrinos



Electron neutrinos+antineutrinos



Example: why uncertainties matter?



Published: 22 November 2017

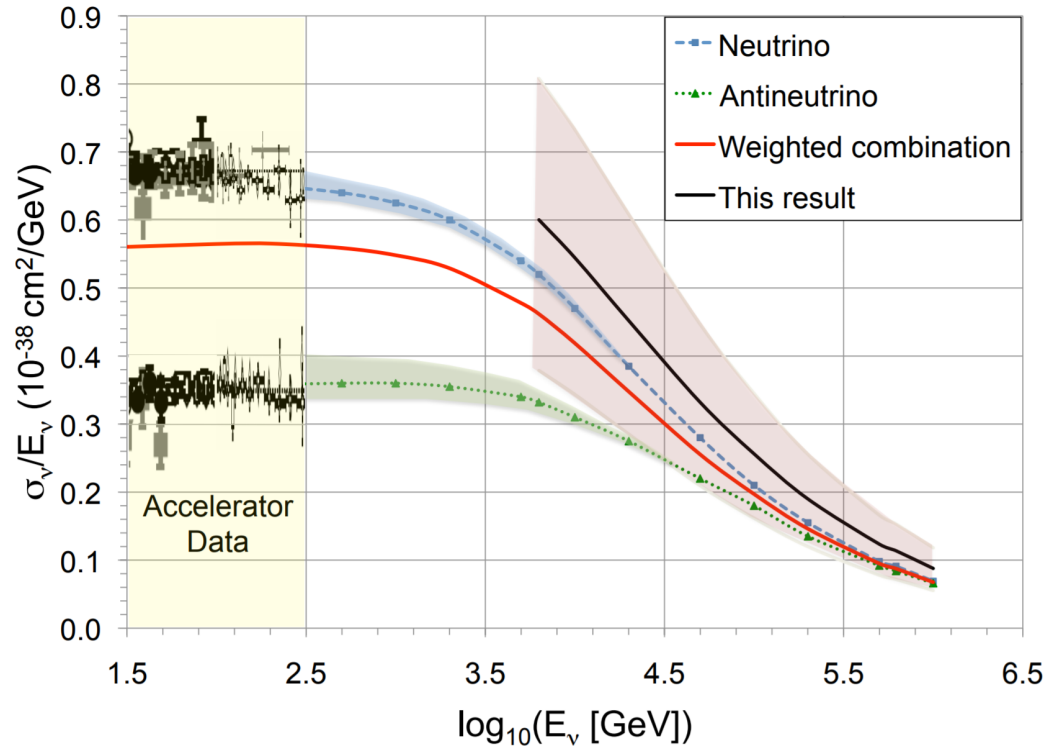
Measurement of the multi-TeV neutrino interaction cross-section with IceCube using Earth absorption

The IceCube Collaboration

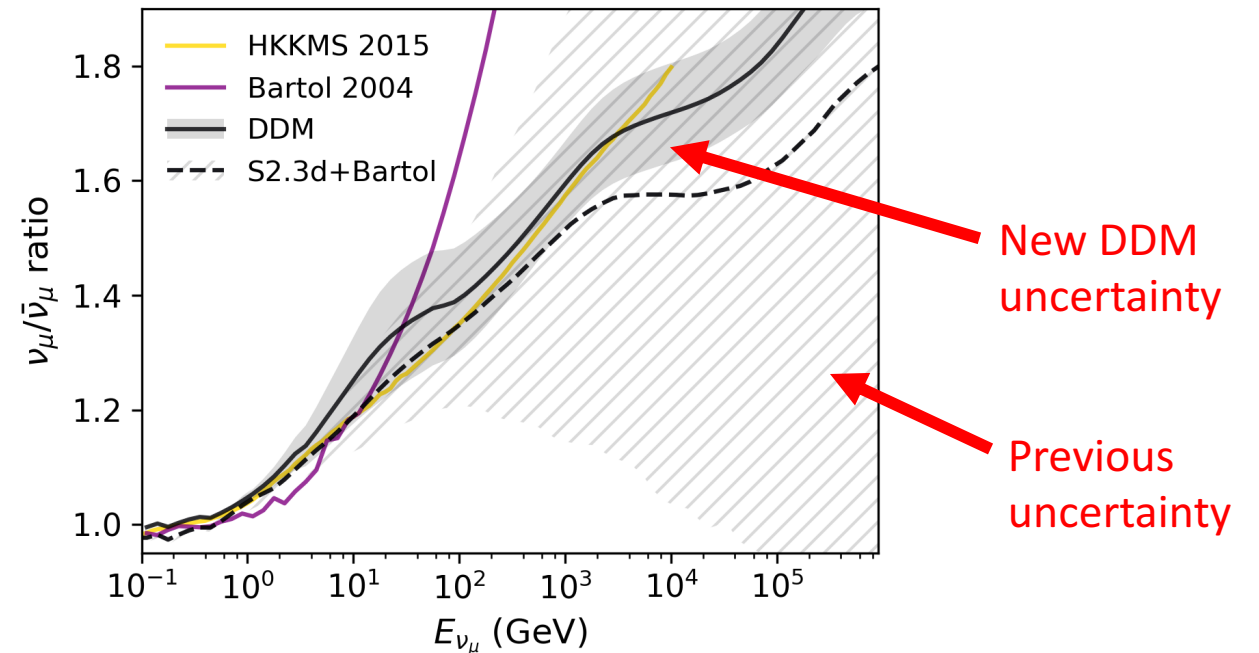
Nature **551**, 596–600 (2017) | [Cite this article](#)

The uncertainties of the cross section measurement

IceCube, Nature, 551, 2017

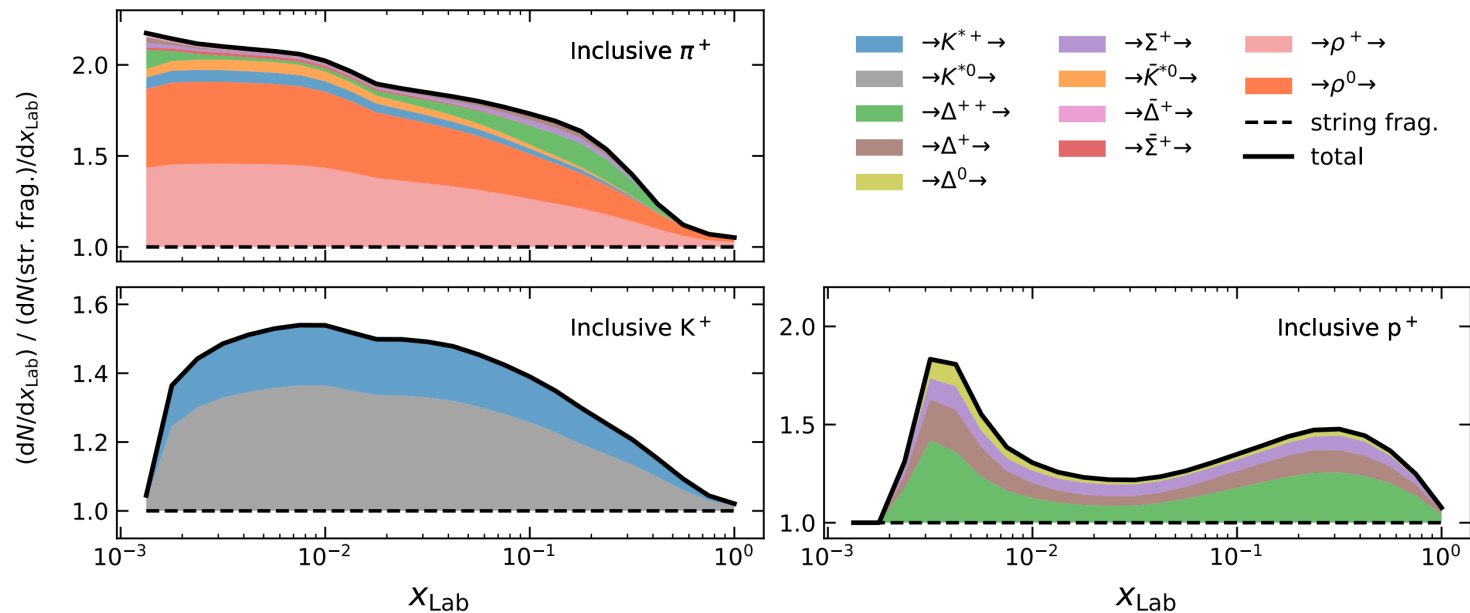


- IceCube can't separately measure neutrino and anti-neutrino
- Observed cross section is an average, weighted by the atmospheric ratio
- The result is 30% higher than the standard model prediction, but compatible within uncertainties



Why is it so difficult to just make better models

Feed-down from higher-mass states

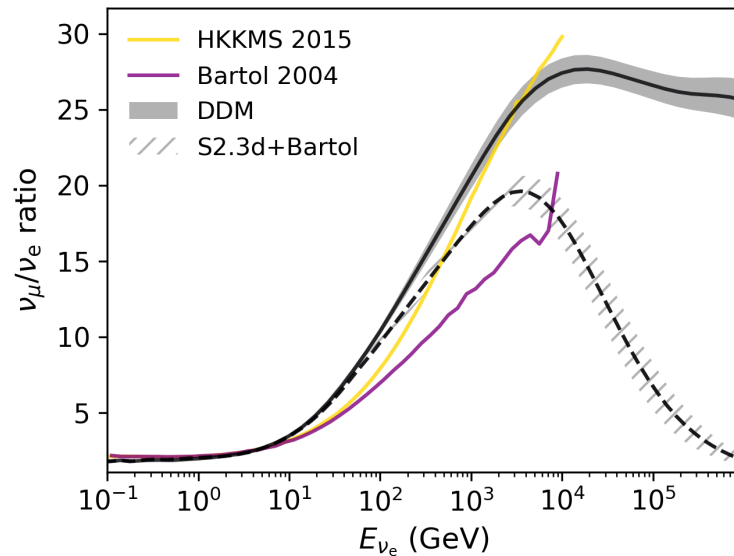
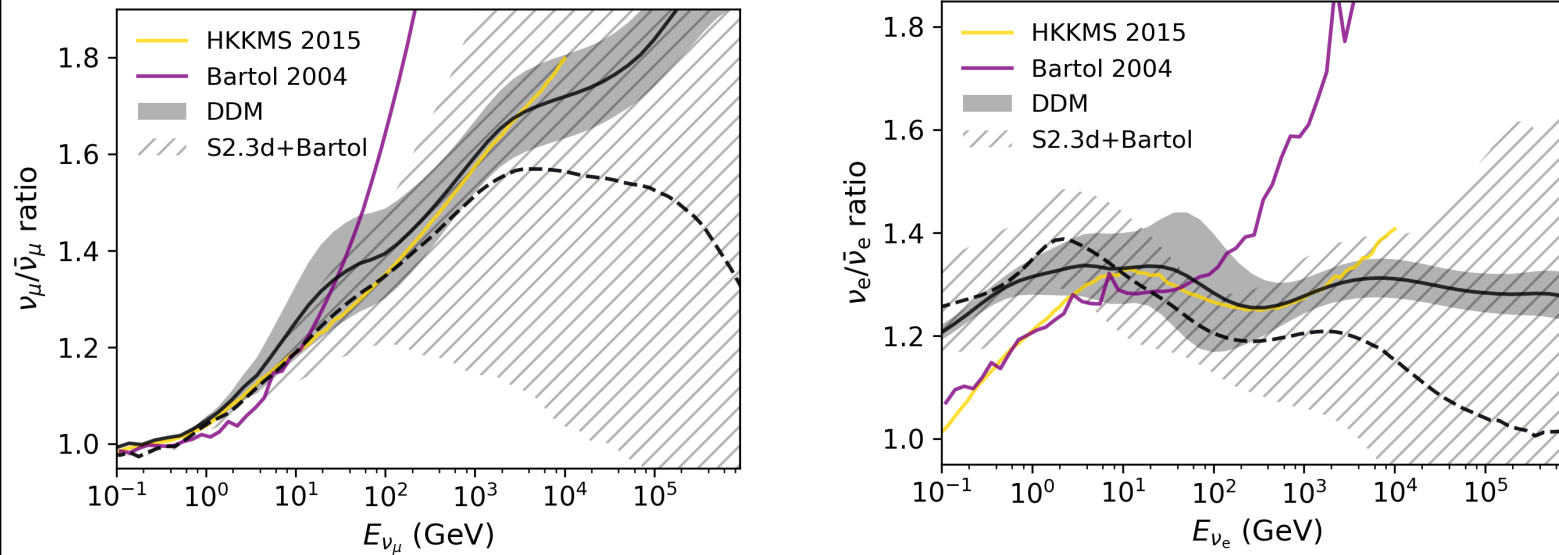


AF et al. PRD 100 (2019)

- We tried (see [Fedynitch et al. PRD 100 \(2019\)](#) and [Riehn et al. PRD102 \(2020\)](#))
- A major problem is the definition of what “pions” or “kaons” are, since a large fraction originates from feed-down of higher mass states
- For cascades in the atmosphere, the definition coincides with that of NA49/61 that only correct for longer lived strange particles like Λ
- Older data from accelerators may not be useful, since it is not corrected for feed-down (see e.g. epic papers by [S. Wenig](#) and [H.G. Fischer](#) from NA49)
- For most interaction models the inclusive (pion) yields are a superposition of ρ , Δ etc., which are explicitly produced in the model’s fragmentation routines
- There are no “easy to tune” free parameters

DDM+ GSF vs data: neutrino ratios

Neutrino-antineutrino ratios

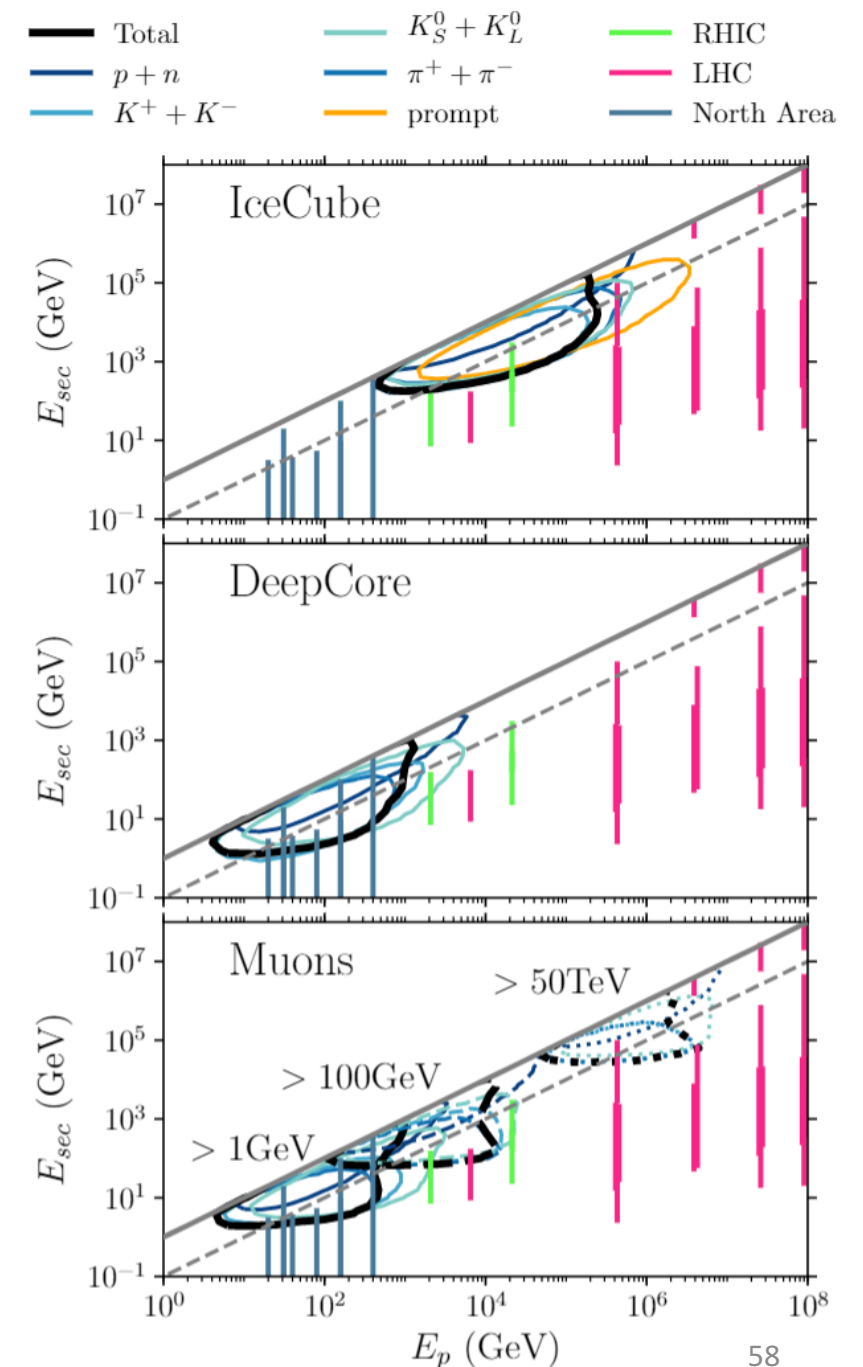


Flavor ratio

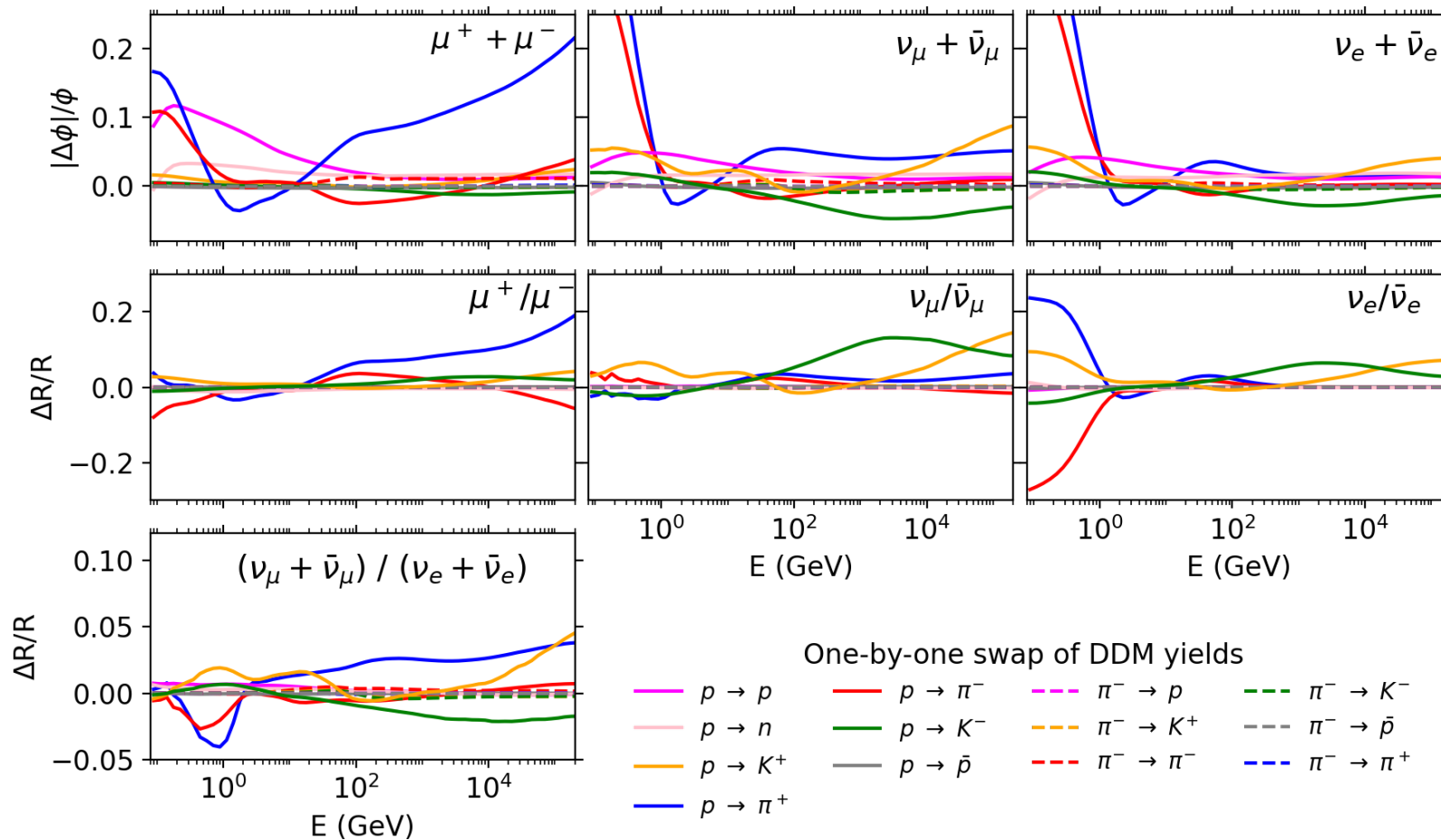
- Neutrino antineutrino ratio compatible over a wide energy range with HKKMS within error
- At low energy notable improvement compared to Bartol errors due to NA61 31 GeV dataset
- Error on ratios at 100 MeV — GeV may be slightly underestimated due to extrapolation in DDM below 31 GeV
- Flavor ratio above 20 GeV significantly different due to less kaons in DDM wrt HKKMS or Bartol 2004

Atm. leptons <-> accelerators

- Contours show phase-space probed by atmospheric muon and neutrino experiments
- The lines show **taken** data (not necessarily analyzed) assuming pion secondaries
- Interactions within contours responsible for 90% of the event rate
- Atmv in IceCube probes hadronic interactions at $E < E_{\text{LHC}}$.
- DeepCore probes same phase-space as Super-/Hyper-K
- Muons: vertical, surface, flux integrated above threshold



Impact of individual DDM channels



- Exchanging only one channel of a DPMJET prediction
- Largest impact from π^+ and K^- as expected from sub-panels on Sl. 10
- Only small differences for most other channels: DPMJET (also, SIBYLL and QGSJET) similar to DDM
- Large impact on low energy muons \rightarrow hence also neutrinos from muon decay
- Baryon distributions can shift production depth that matters for unstable particles such as muons

Neutrinos from charm

Charm production in SIBYLL 2.3d

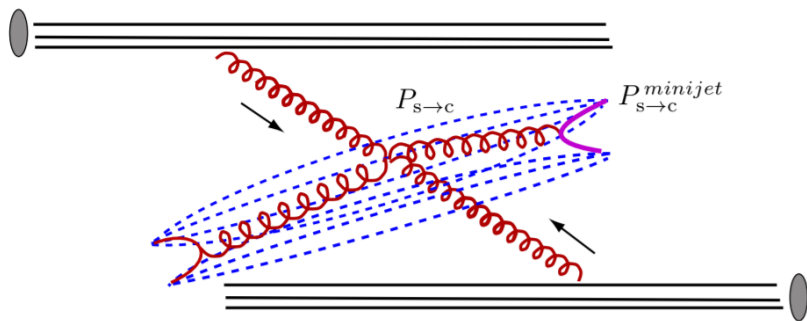
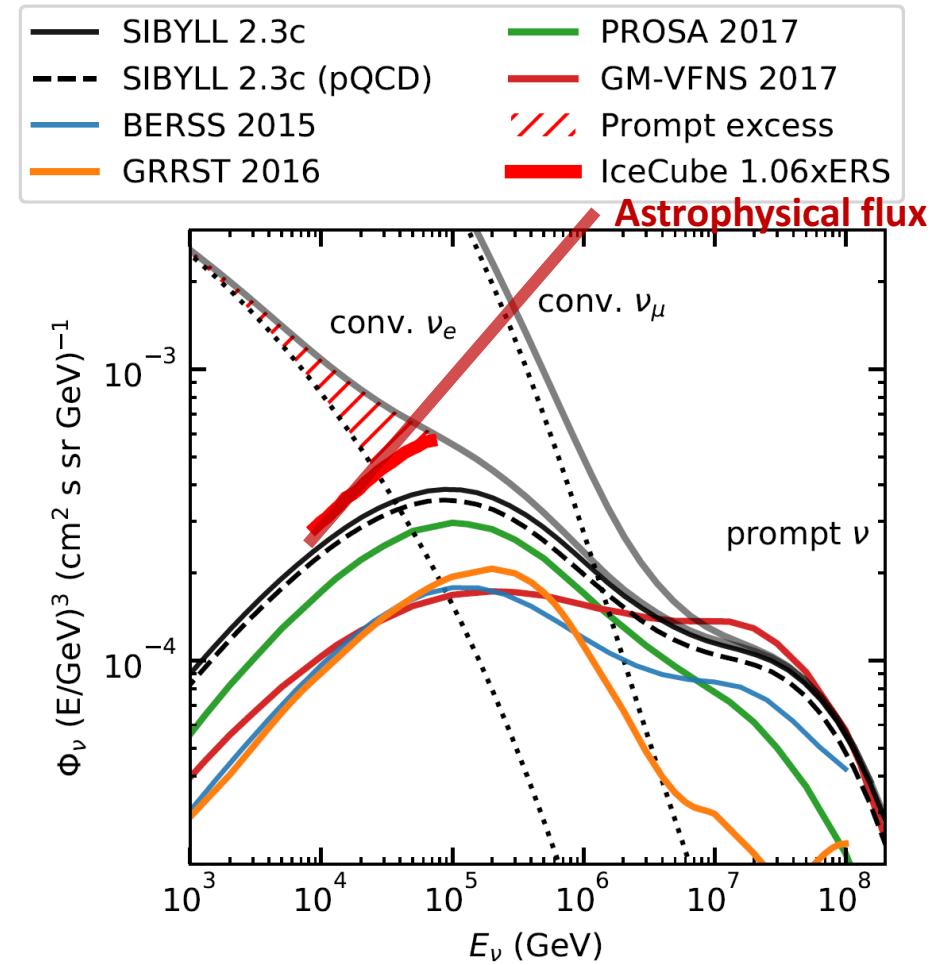
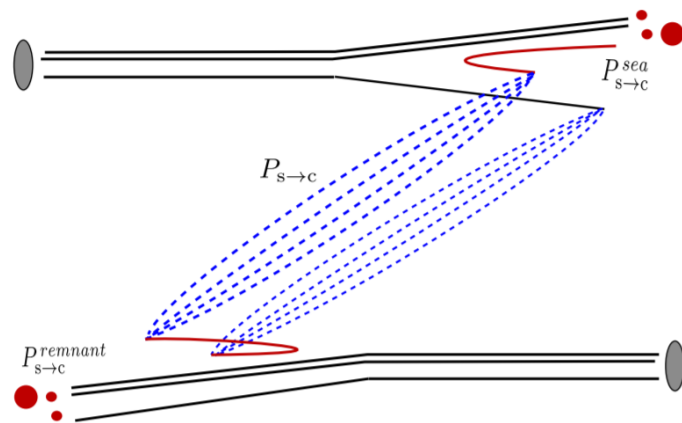
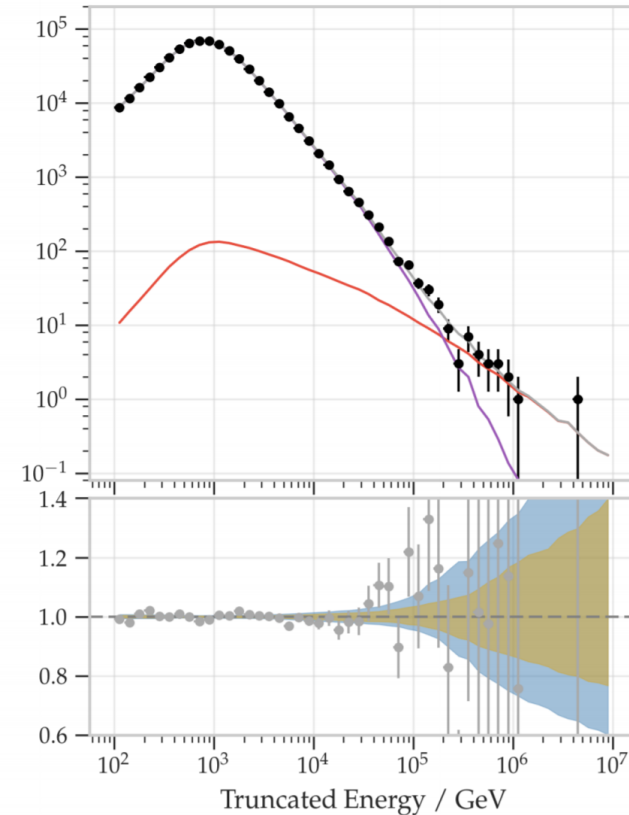
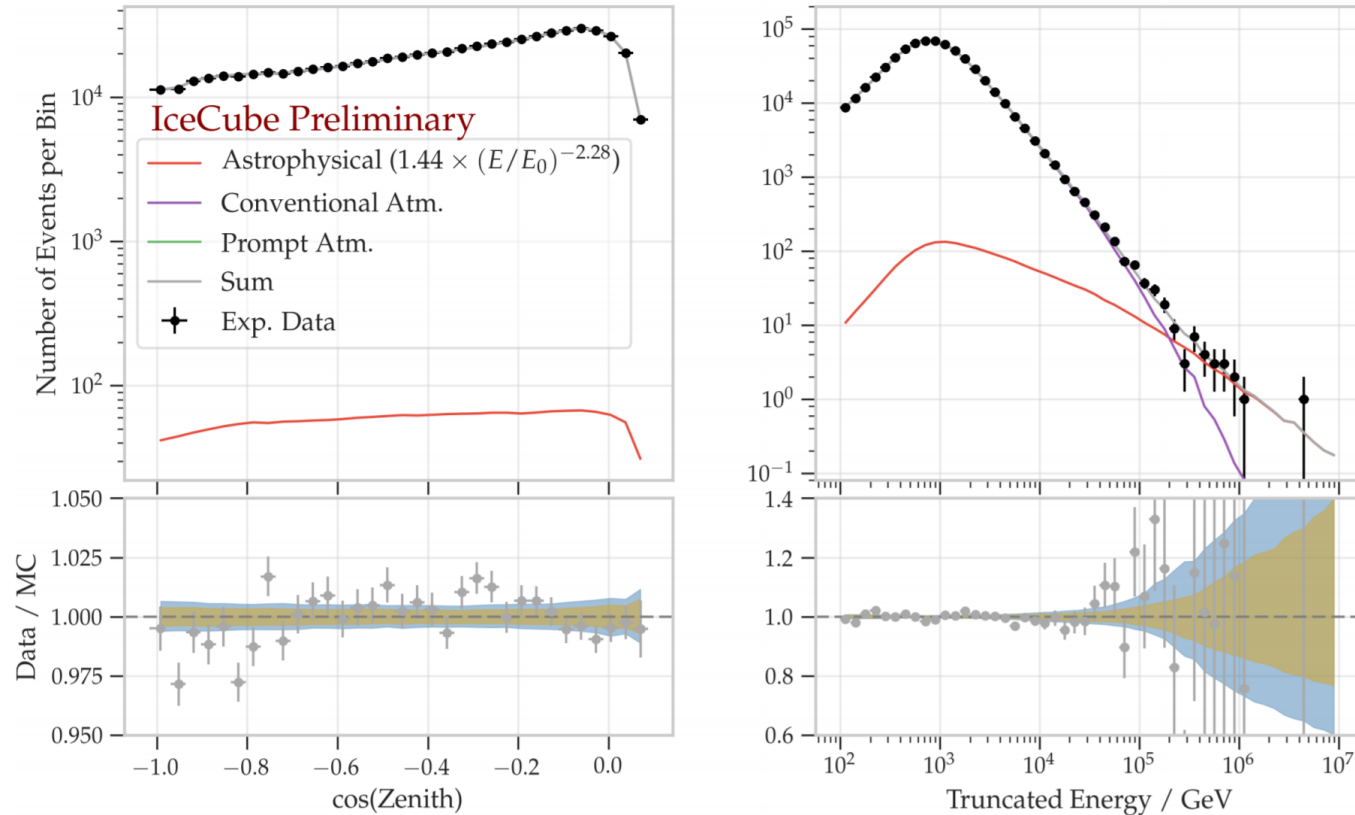


FIG. 5.7. String configuration for minijets in SIBYLL.

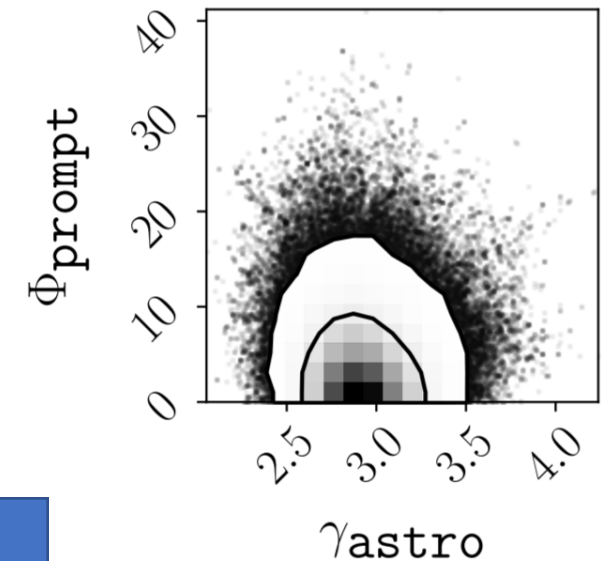
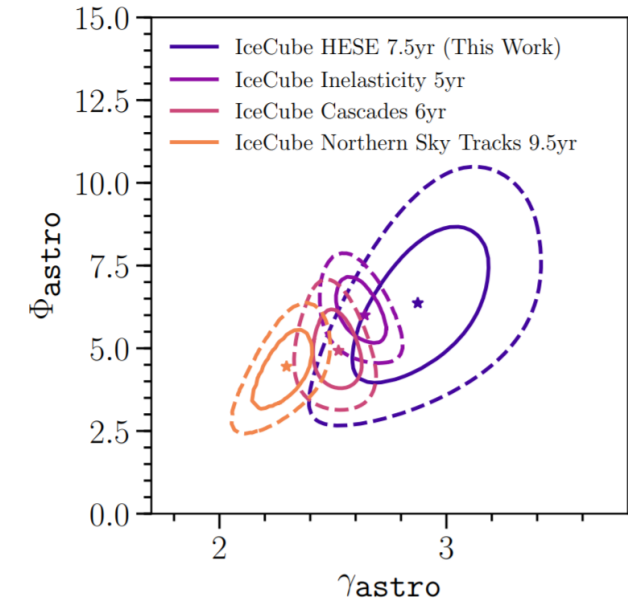


Challenge: where is the charm?

J. Stettner, IceCube Collaboration, ICRC 2019

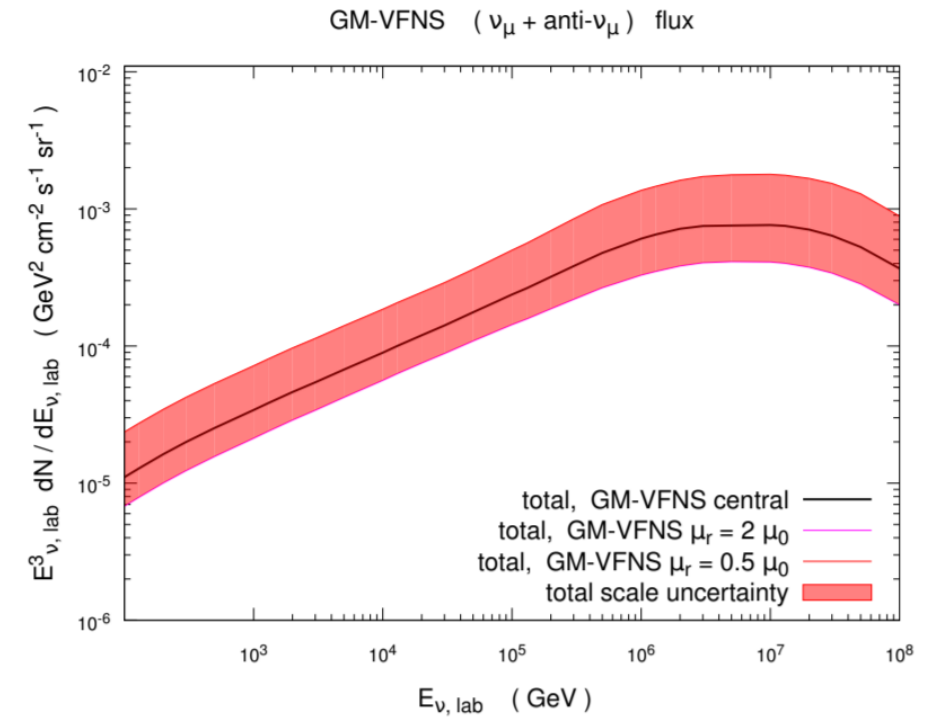
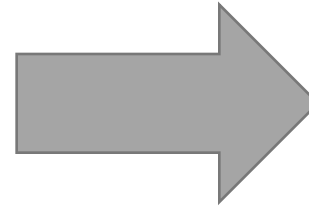
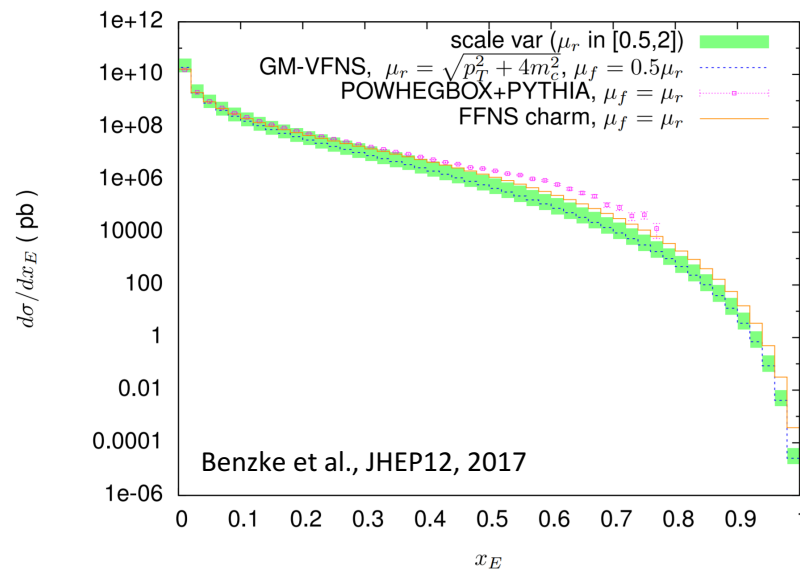
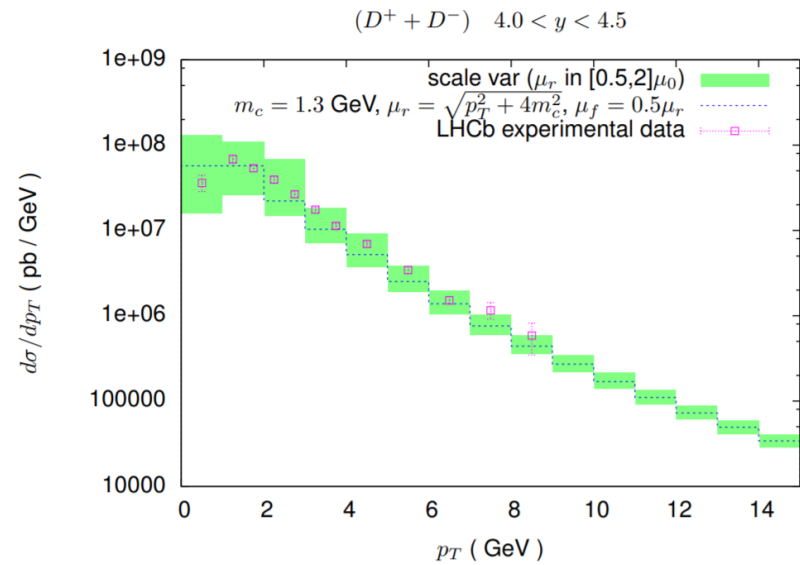


HESE 7.5 yr, IceCube, PRD 104, 2020



IceCube is not really sensitive to charm given the poor theoretical constraints.

Prompt neutrinos: theoretically challenging



Intrinsic charm is back in the game

Stan Brodsky

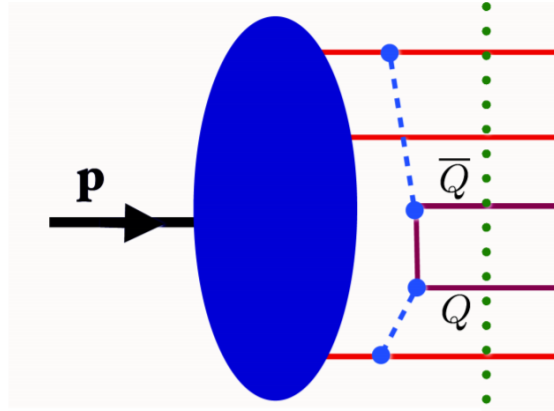
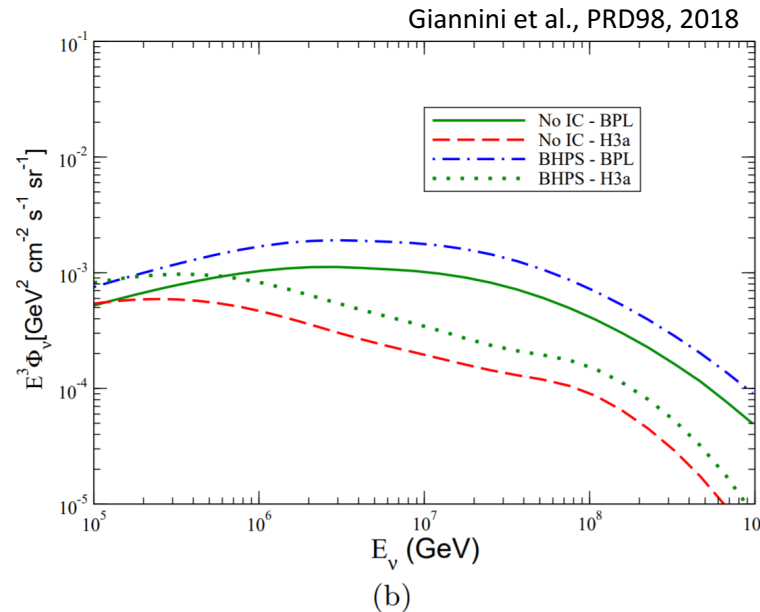
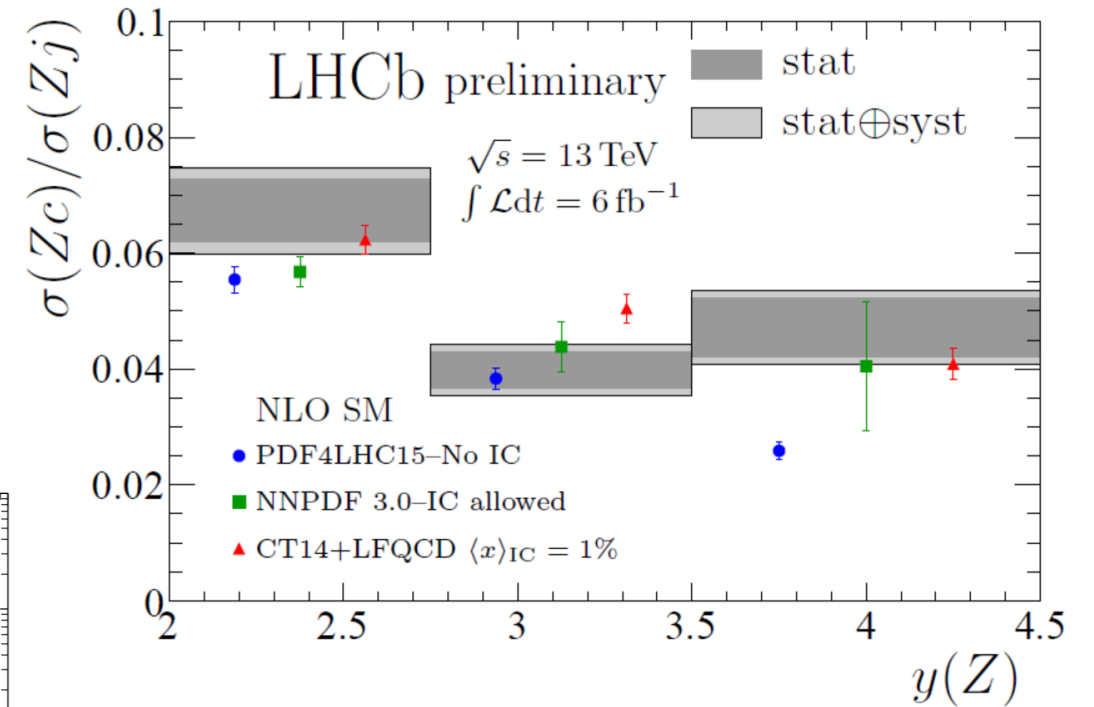


Figure 1: Five-quark Fock state $|uudQ\bar{Q}\rangle$ of the proton and the origin of the intrinsic sea.



[LHCb, EPS-HEP 2021](#)



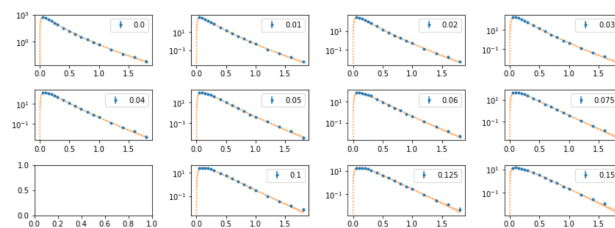
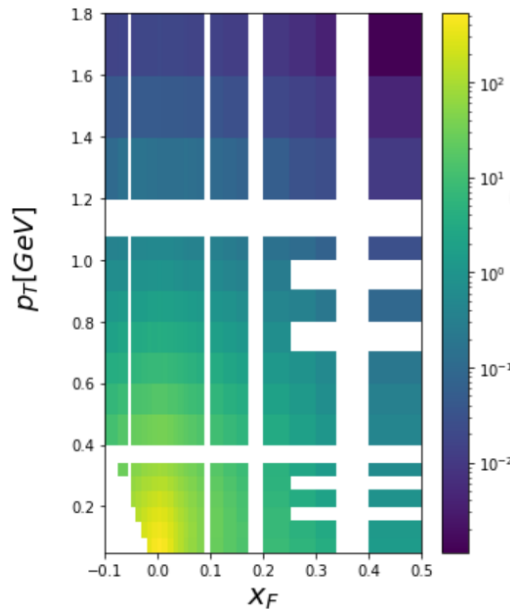
IC can have some impact for IceCube.

Building the DDM

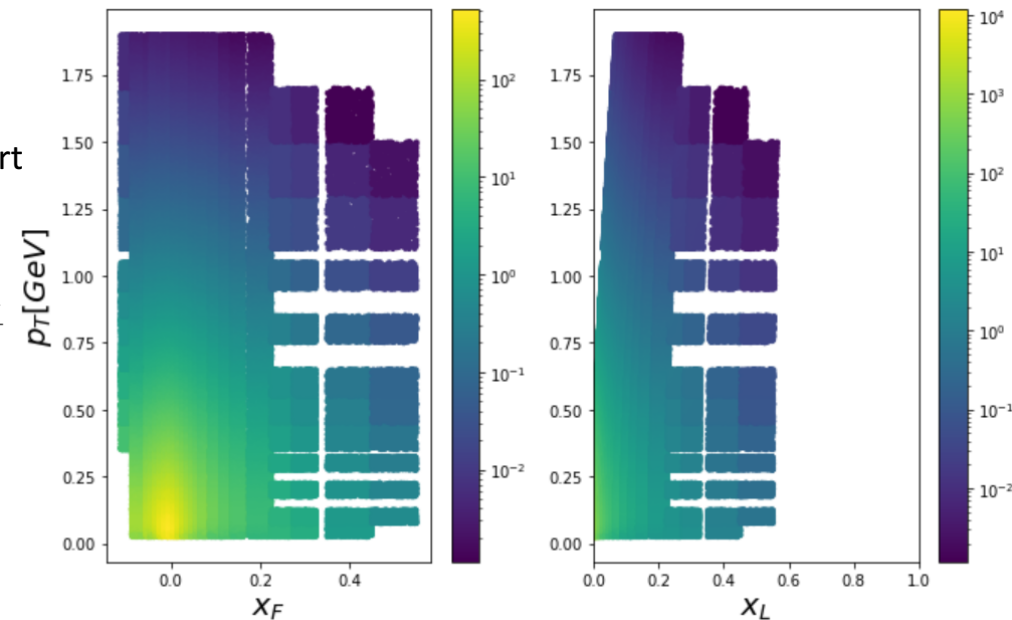
Sample from
 $x_F = p_z/\sqrt{s}$ and convert
 into $x_L = E_{\text{secondary}}/E_{\text{proj}}$

$$x_{Lab} = \frac{E_c}{E_a} = \frac{\gamma \sqrt{m_c^2 + \frac{1}{4}x_F^2 E_{c.m.}^2 + p_{c,T}^{*2} + \frac{1}{2}\gamma\beta x_F^2 E_{c.m.}}}{E_a}$$

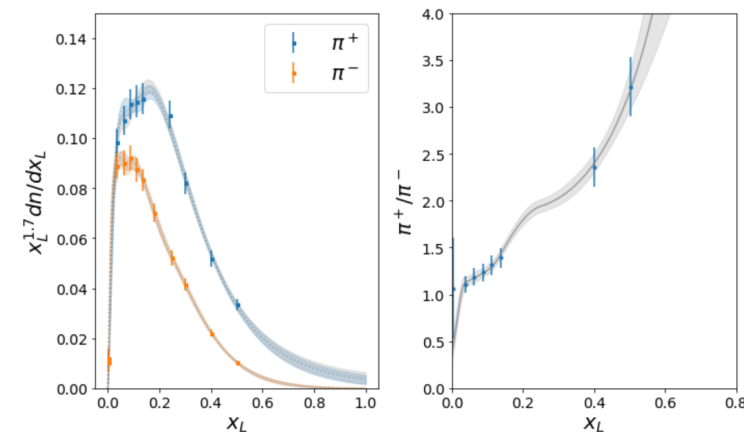
NA49 proton-carbon @ 158 GeV



Fit p_T in each x_F bin using
 $\frac{dn}{dp_{\perp}} = a_0 p_{\perp}^{a_1} e^{a_2 p_{\perp}^{a_3}}$



Fit dn/dx_L with
 splines, get
 covariance matrix



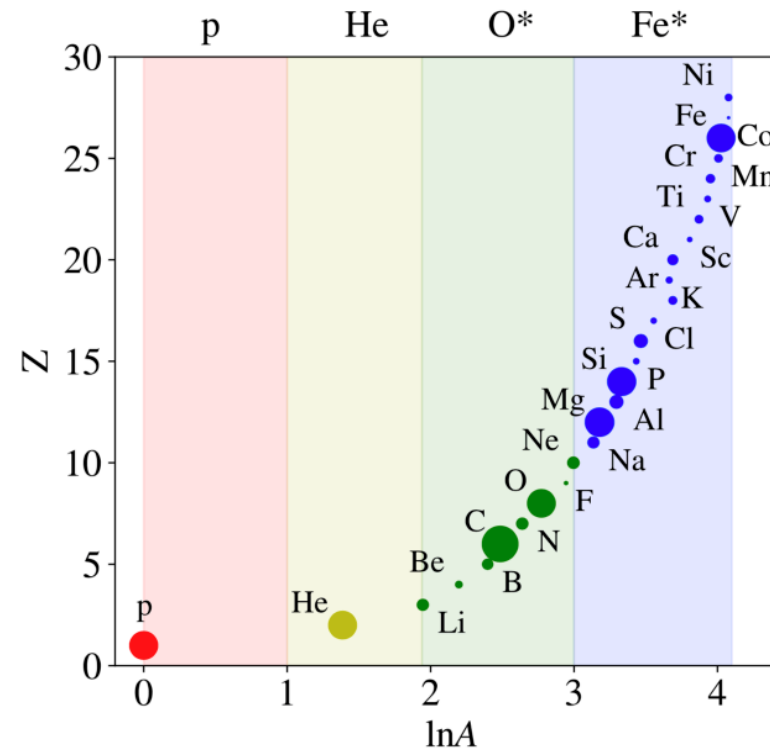
Included data

Experiment	beam	$E_{\text{beam}}/\text{GeV}$	Secondaries	Variables
NA49	pC	158	π^{\pm}, \bar{p}, n	x_F, p_{\perp}
NA49	pp	158	K^{\pm}	x_F, p_{\perp}
NA61/SHINE	pC	31	$\pi^{\pm}, K^{\pm}, K_S^0, \Lambda$	p, θ
NA61/SHINE	π^-C	158, 350	$\pi^{\pm}, K^{\pm}, \bar{p}$	p, p_{\perp}

(In the next iteration we would like to include new results from
 NA61 and old results from NA59 that require Be->C extrapolation.)

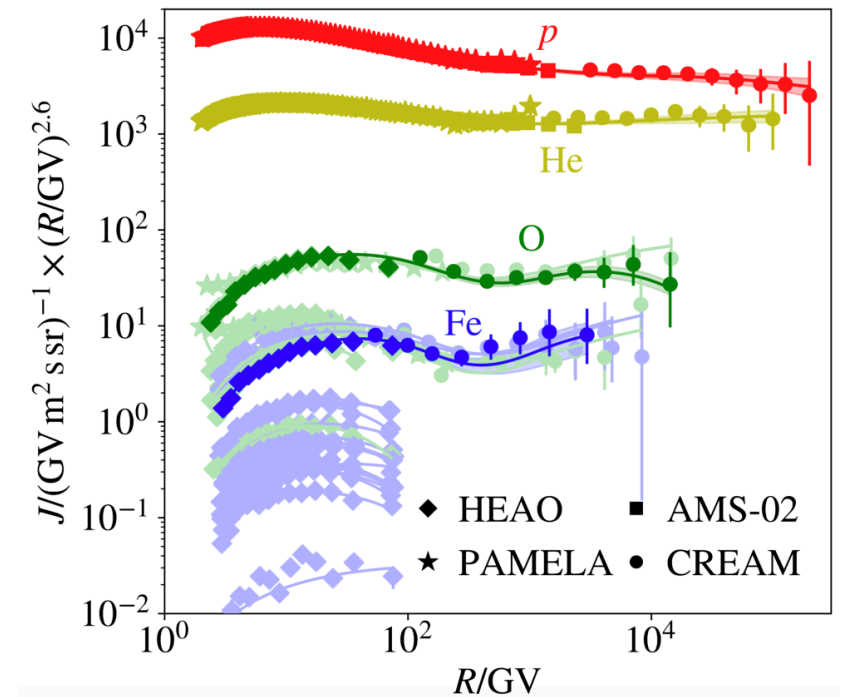
Global Spline Fit – fit to direct & indirect observations

- Fit **four** independent mass groups, which cover equal ranges in $\ln A$:
proton (p), helium (He), oxygen group (O*), and iron group (Fe*)
- Assumption: this holds **at all energies**
- One leading element L per group described by smooth spline curve
- Other elements j in a group kept in constant ratio: $J_j(R)/J_L(R) = \text{const.}$



Mass sensitivity of air-shower experiments is $\sim \ln A$

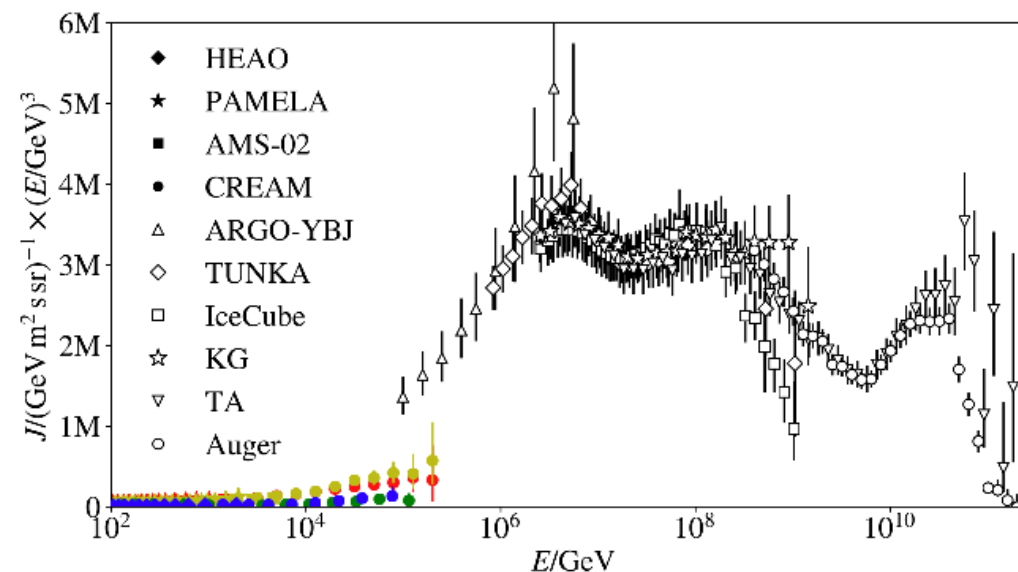
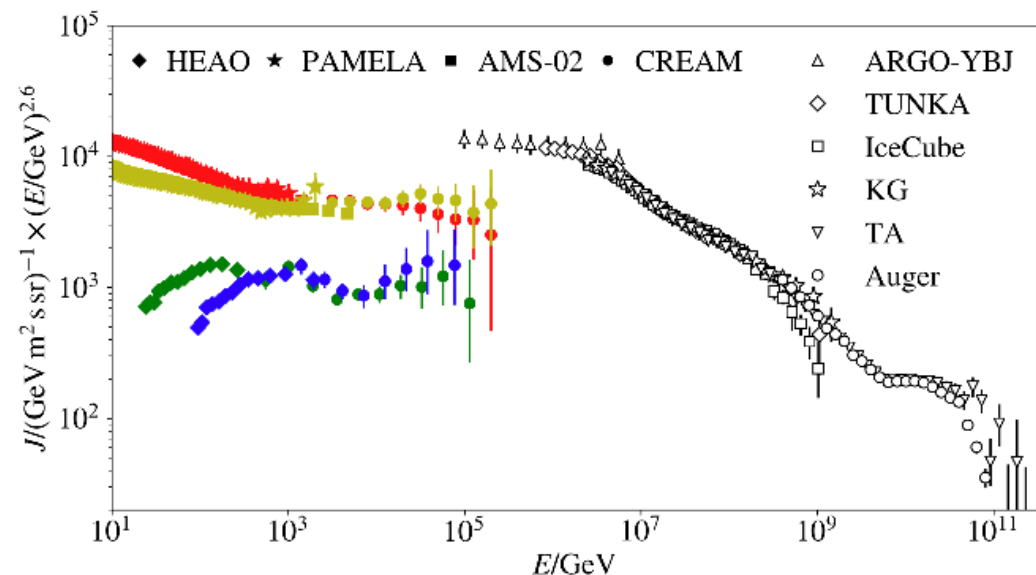
H. Dembinski, AF, T. Gaisser
PoS(ICRC2017)533



Handling energy-scale uncertainty

H. Dembinski, AF, T. Gaisser
PoS(ICRC2017)533

Adjusted data



- The determination of **energy scale in air-shower experiments is uncertain**
- This is caused by inconsistencies of **hadronic interaction models**
- Fit adjusts energy scales **within systematic uncertainties** of the experiment

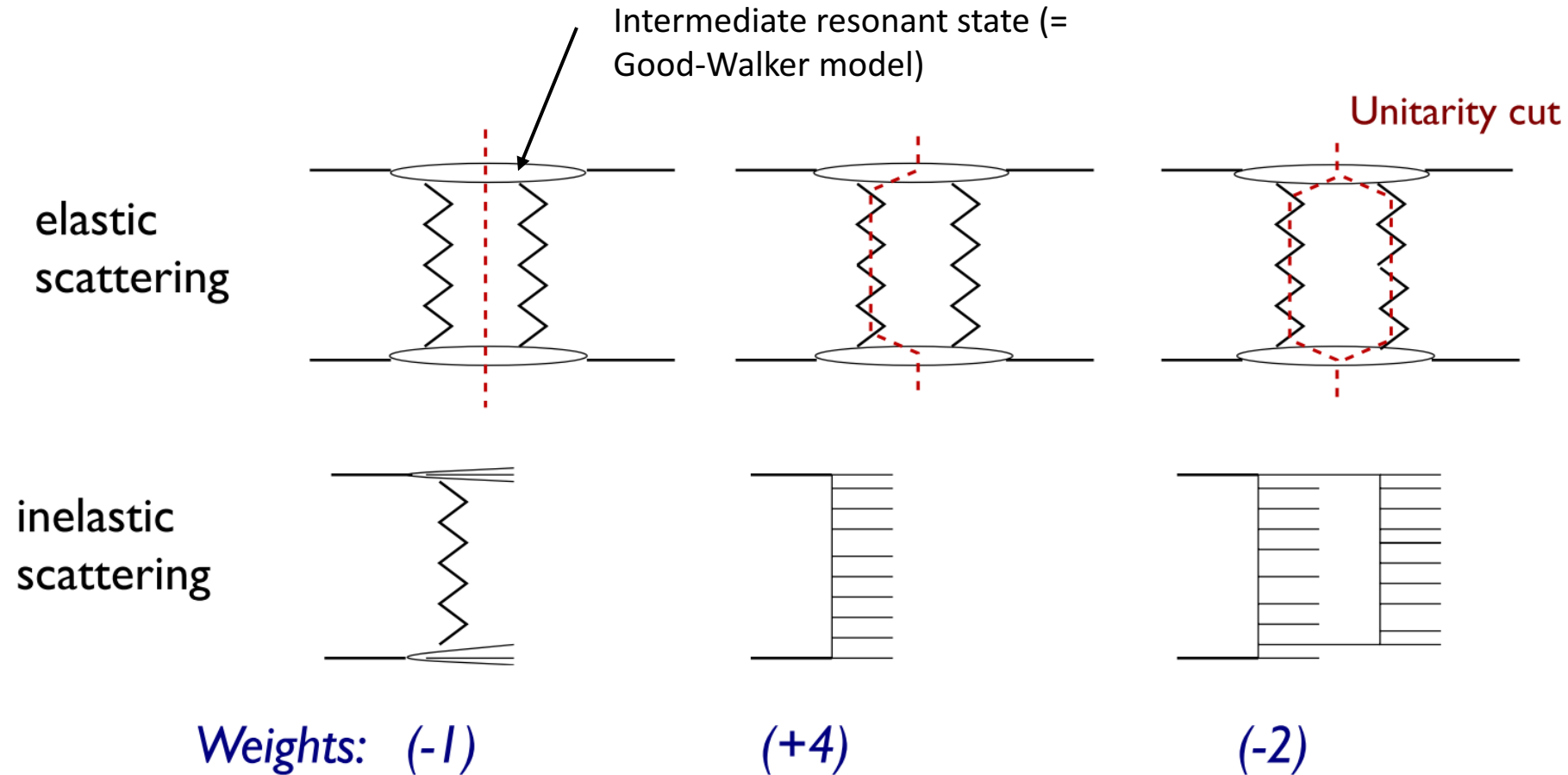
$$\tilde{J}(\tilde{E}) = J(E) \frac{dE}{d\tilde{E}} = J \left(\frac{\tilde{E}}{1 + z_E} \right) \frac{1}{1 + z_E}$$

Flux distortion caused by energy-scale offset z_E

$$S = \sum_i z_i^2 + \sum_j \left(\frac{z_{Ej}}{(\sigma[E]/E)_j} \right)^2$$

Flux residuals Energy-scale offset residuals

AGK cutting rules = unitarity cuts

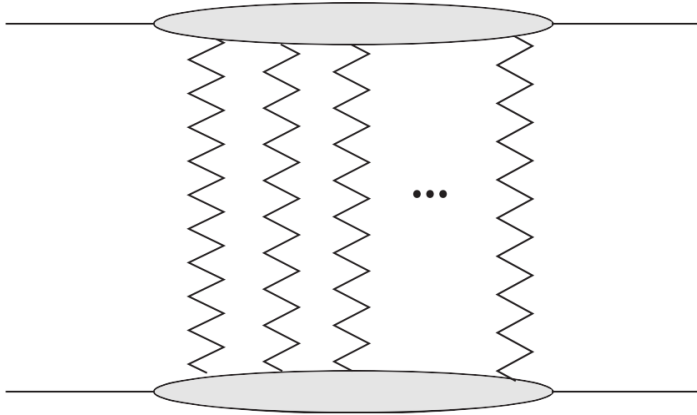


(Abramovskii, Gribov,
Kancheli 1974)

Mathematical model that tells how to sum the different combinations of cut graphs to conserve unitarity without double counting

Construction of scattering amplitudes

N-Pomeron exchange graph



t-channel (momentum space) N-pomerton scattering amplitude,
 $t = (q)^2 \sim (k_T)^2$

$$A^{(n)} = -i(i)^n \frac{1}{n!} \left(\frac{1}{2s}\right)^{n-1} \prod_{i=1}^n \left(\int d^2 k_{\perp, i} A^{(1)}(s, k_{\perp, i}^2) \right) \frac{\delta^{(2)}(q_{\perp} - \sum_{i=1}^n k_{\perp, i})}{(2\pi)^{2(n-1)}}$$

One-pomeron elastic amplitude

Couplings to particle A, B

$$A_{AB}^{P_s} = i s_0 g_{AP}(t) g_{BP}(t) \left(\frac{s}{s_0}\right)^{\alpha_{P_s}(t)}$$

$$g_{iP}(t) = g_{iP}^0(t) \exp\left(\frac{1}{2} b_{iP}^0 t\right)$$

Connected to transverse/impact-parameter b-space via
 inv. Fourier-tr.

$$A(s, t) = 4s \int_0^\infty d^2 \vec{B} \, a(s, \vec{B}) e^{i\vec{q}\vec{B}}$$

Multi-Pomeron amplitude in impact parameter space (Eikonal
 approximation). Much simpler representation!!

$$a(s, \vec{B}) = \sum_{n=1}^{\infty} a^{(n)}(s, \vec{B}) = \frac{i}{2} \left(1 - \exp \left[-\chi(s, \vec{B}) \right] \right)$$

$$\chi(s, \vec{B}) = -2i a^{(1)}(s, \vec{B}) \quad \text{and}$$

$$2 \int d^2 \vec{B} \, \chi(s, \vec{B}) = \sigma^{\text{Born}}(s)$$

Computation of cross sections (for all models similar)

Optical theorem for total cross section
(needs only elastic amplitude)

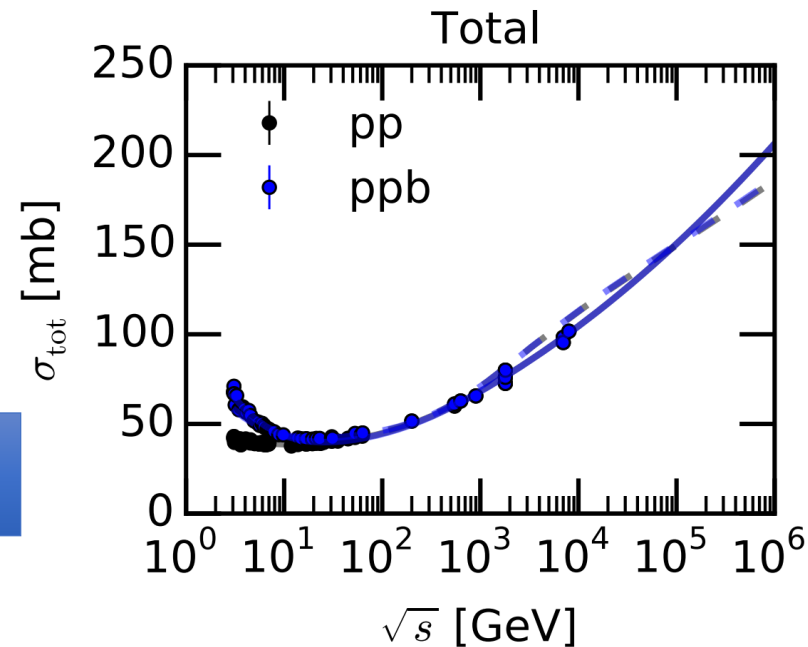
$$\sigma_{\text{tot}} \approx \frac{1}{s} \Im m(A(s, t = 0))$$

In practice done in impact parameter space

$$\sigma_{\text{tot}} = 2 \int d^2 \vec{B} \Im m(a(s, \vec{B})) = 2 \int d^2 \vec{B} (1 + e^{-\chi_R} \sin \chi_I)$$

$$\sigma_{\text{el}} = 2 \int d^2 \vec{B} |a(s, \vec{B})|^2 = \int d^2 \vec{B} (1 + 2e^{-\chi_R} \sin \chi_I + e^{-\chi_R})$$

$$\sigma_{\text{inel}} = \sigma_{\text{tot}} - \sigma_{\text{el}} = \int d^2 \vec{B} (1 - e^{-2\chi_R})$$

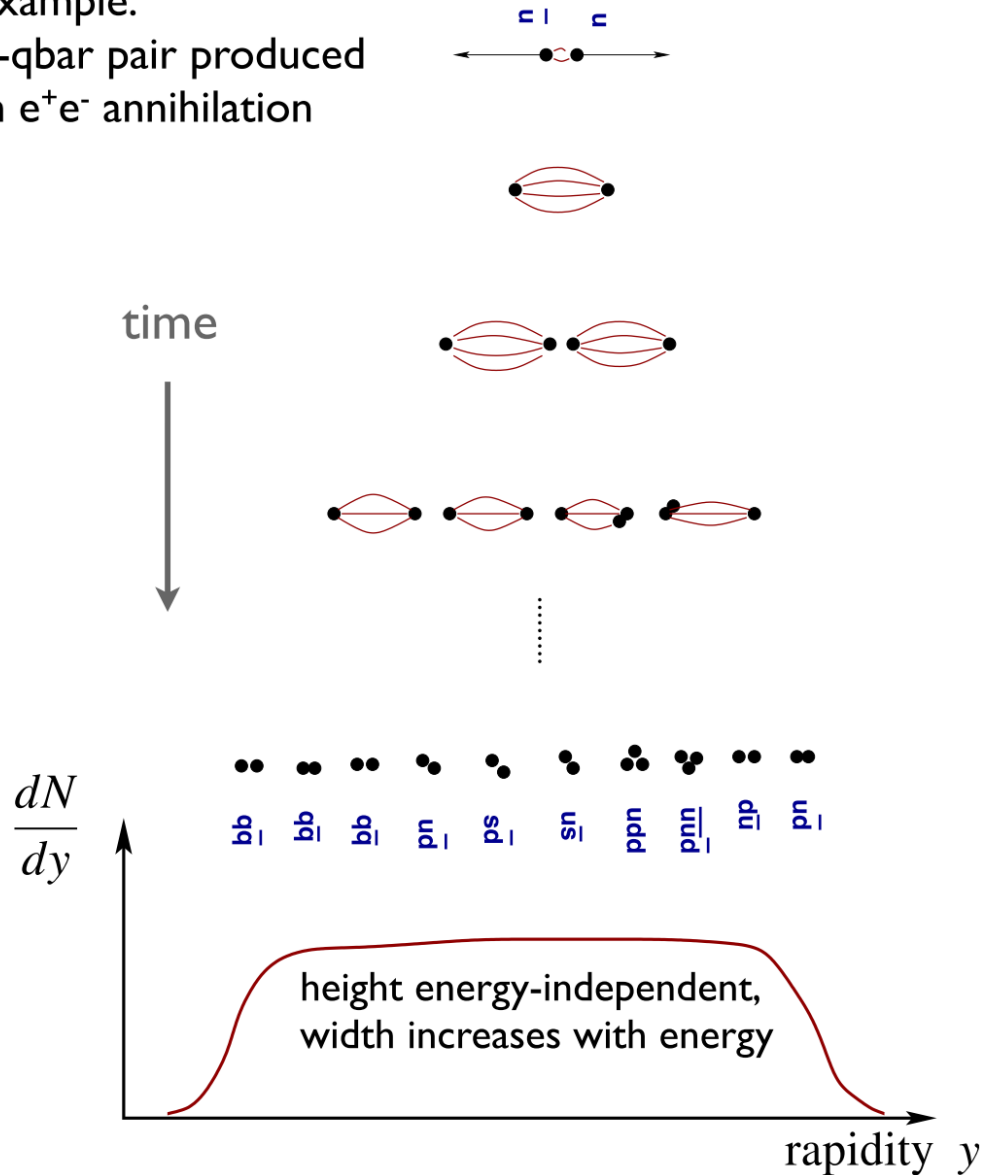


Reggeon component: drop with s
(at low energy) $s^{\Delta_R} \sim s^{-0.5}$

Pomeron component: growth with s
(cms-energy squared) $s^{\Delta_P} \sim s^{0.08}$

String fragmentation (Lund-model)

Example:
q-qbar pair produced
in e^+e^- annihilation



Rapidity

$$y = \frac{1}{2} \ln \frac{E + p_{\parallel}}{E - p_{\parallel}}$$

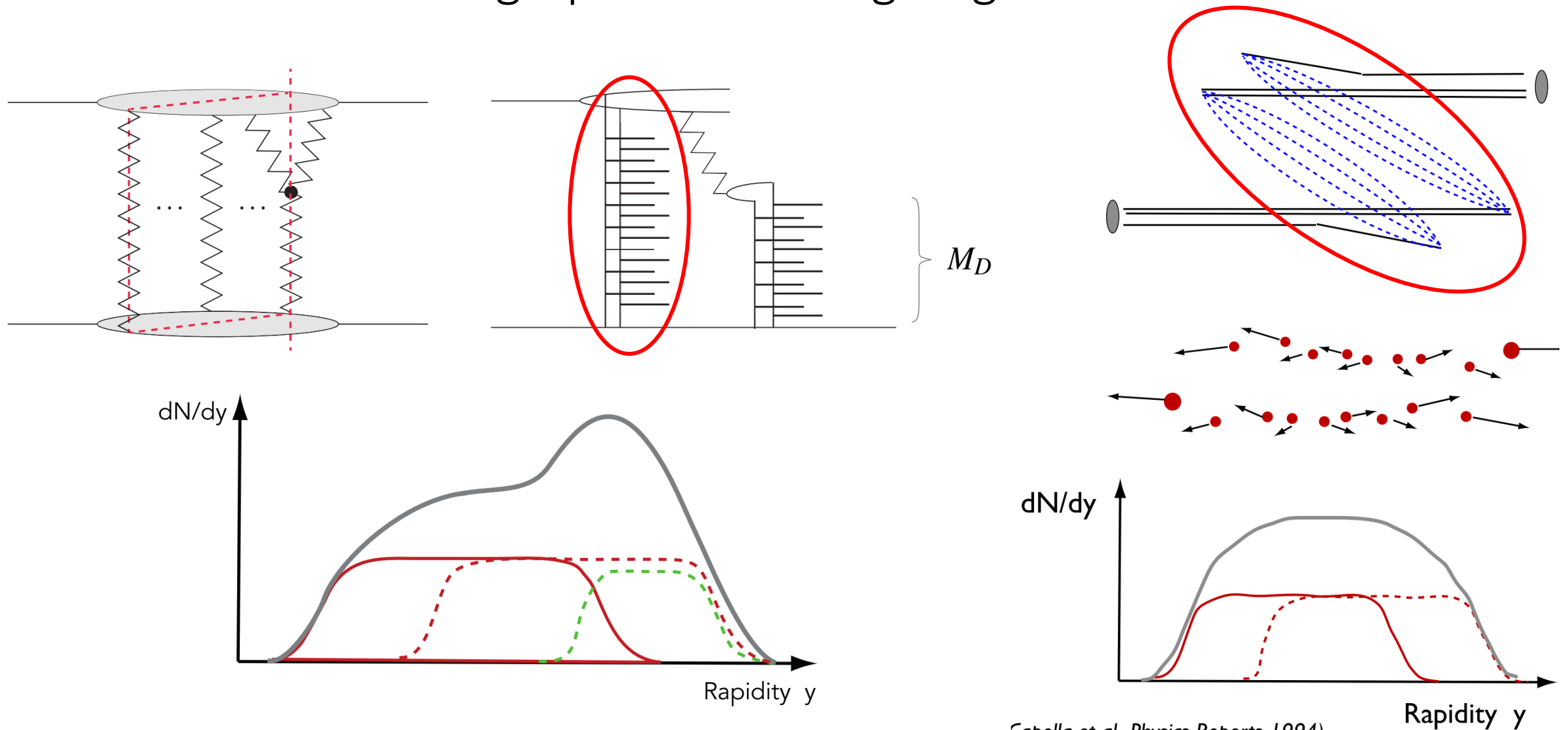
Rapidity of massless particles

$$y = \frac{1}{2} \ln \frac{1 + \cos \theta}{1 - \cos \theta} = -\ln \tan \frac{\theta}{2}$$

Pseudorapidity

$$\eta = -\ln \tan \frac{\theta}{2}$$

Realization of cut graphs with string fragmentation



Capella et al., Physics Reports 1994)