

The Hierarchy Problem and the Top Yukawa: An Alternative to Top Partner Solutions

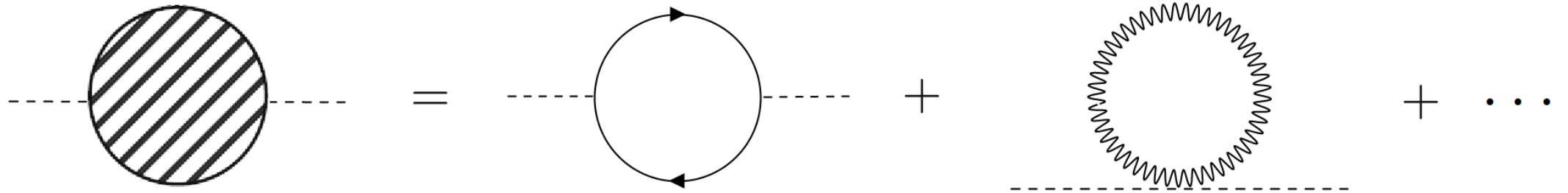
with Andreas Bally, Florian Goertz, based on arXiv:2211.17254

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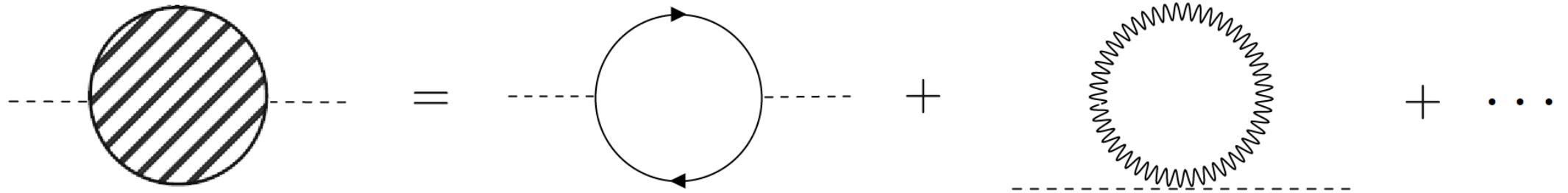
Mini-Workshop on Highlights of 2022, NCTS

The Hierarchy Problem



$$\delta m_h^2 = -\frac{3}{8\pi^2} y_t^2 \Lambda_t^2 + \frac{9}{64\pi^2} g^2 \Lambda_g^2 + \dots$$

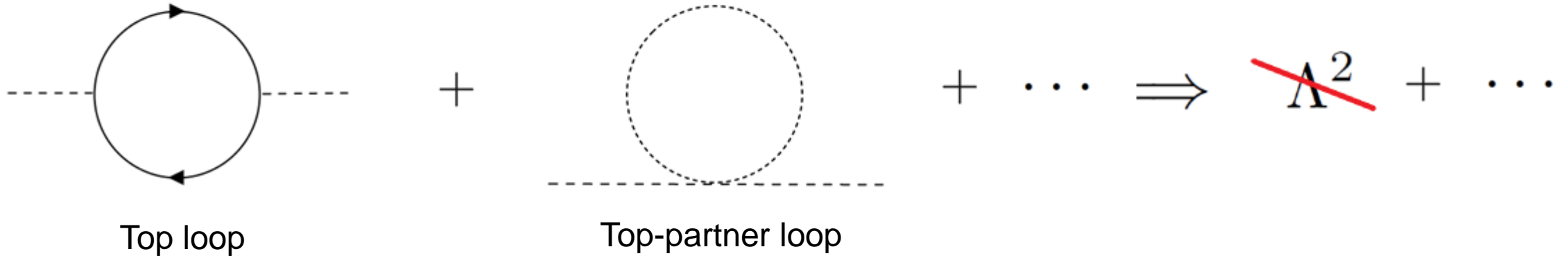
The Hierarchy Problem



$$\delta m_h^2 = \boxed{-\frac{3}{8\pi^2} y_t^2 \Lambda_t^2} + \frac{9}{64\pi^2} g^2 \Lambda_g^2 + \dots$$

The largest contribution!!

Top partner solutions



- The cancellation is guaranteed by Symmetry (ex: SUSY, shift symmetry ...)
- The Higgs quadratic is still generated due to the difference between

$$\delta m_h^2|_{\text{top}} + \delta m_h^2|_{\text{top partner}} \sim -\frac{3}{8\pi^2} y_t^2 M_T^2 \ln \left(\frac{\Lambda^2}{M_T^2} \right)$$

Problems with Colored top partner

- Absence of colored top partners up to 1.2 TeV
⇒ $\sim 10\%$ fine tuning (even worse for large log factor)

Quantum #	Scalar	Fermion
QCD x EW	SUSY	CHM / RS

⇒ Colored top partners

Alternative to Colored top partners

- Absence of colored top partners up to 1.2 TeV
⇒ $\sim 10\%$ fine tuning (even worse for large log factor)

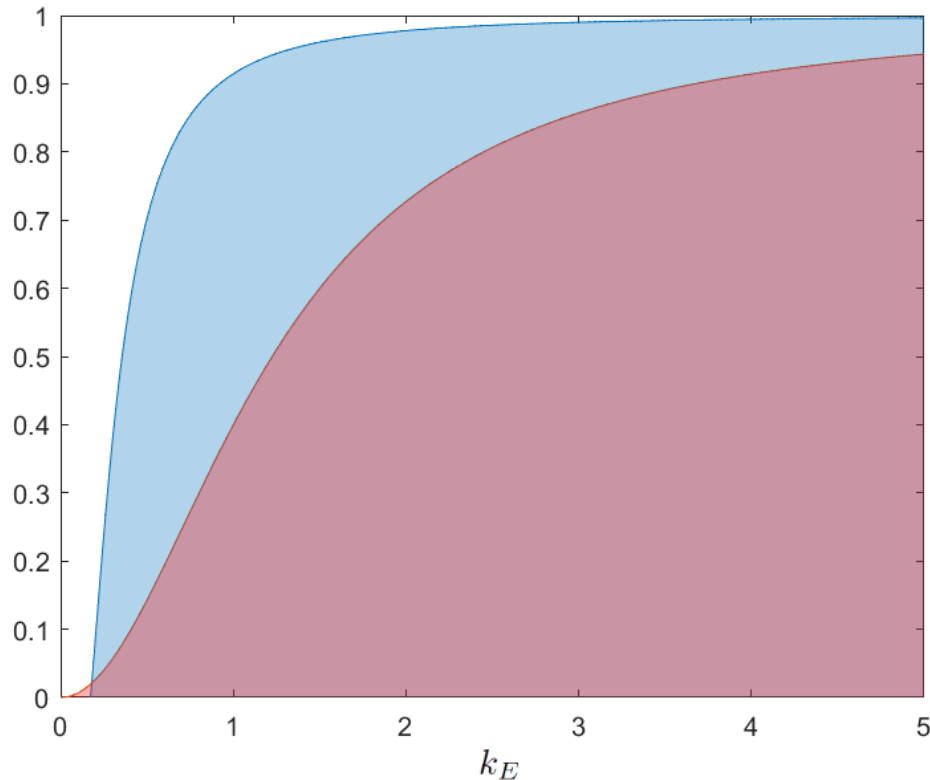
Quantum #	Scalar	Fermion
QCD x EW	SUSY	CHM / RS
Neutral x EW	Folded SUSY	Quirky Little Higgs
Neutral x Neutral	Tripled Top Hyperbolic Higgs	Twin Higgs

⇒ Uncolored top partners

Table borrowed from Chris Verhaaren

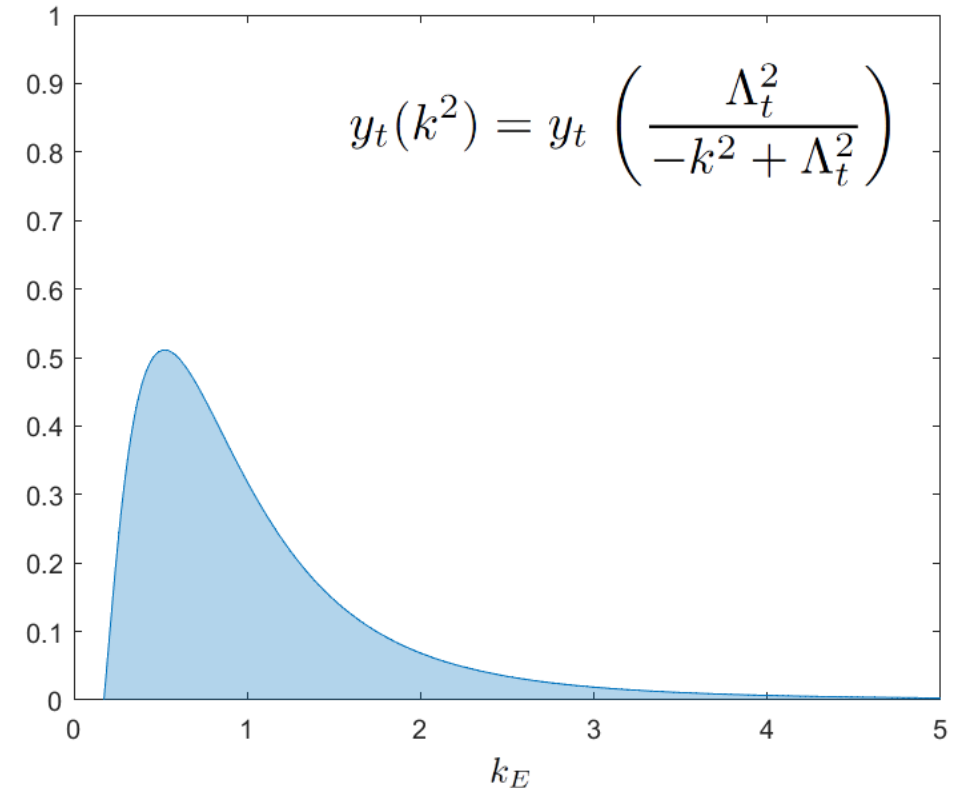
Alternative to Top-partner scenarios

- Cancellation (take $M_T = 1.2 \text{ TeV}$)



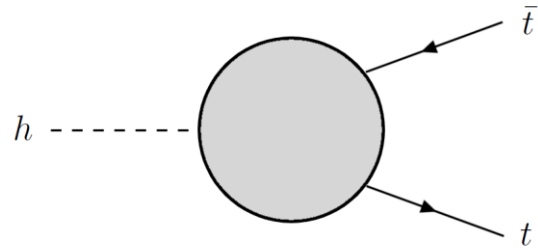
$$\delta m_h^2|_{\text{top}} + \delta m_h^2|_{\text{top partner}} \sim -\frac{3}{8\pi^2} y_t^2 M_T^2 \ln \left(\frac{\Lambda_t^2}{M_T^2} \right)$$

- Reduction (take $\Lambda_T = 1.2 \text{ TeV}$)



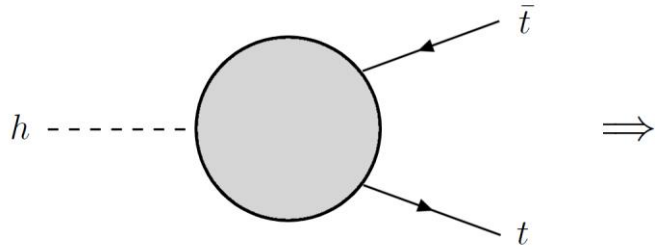
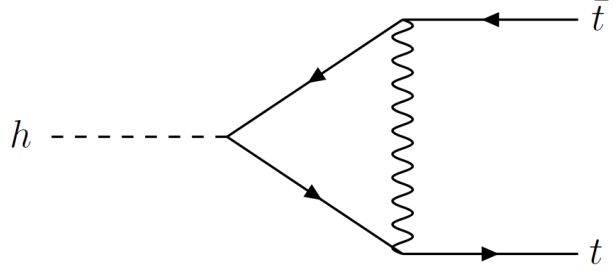
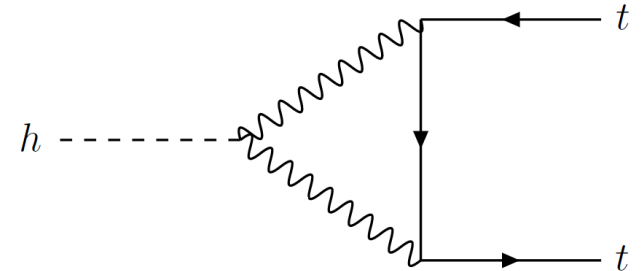
$$\delta m_h^2|_{\text{top}} \sim -i 2N_c \int \frac{d^4 k}{(2\pi)^4} y_t^2(k^2) \frac{k^2 + m_t^2}{(k^2 - m_t^2)^2} \sim -\frac{3}{8\pi^2} y_t^2 \Lambda_t^2$$

Zoom in the Top Yukawa vertex



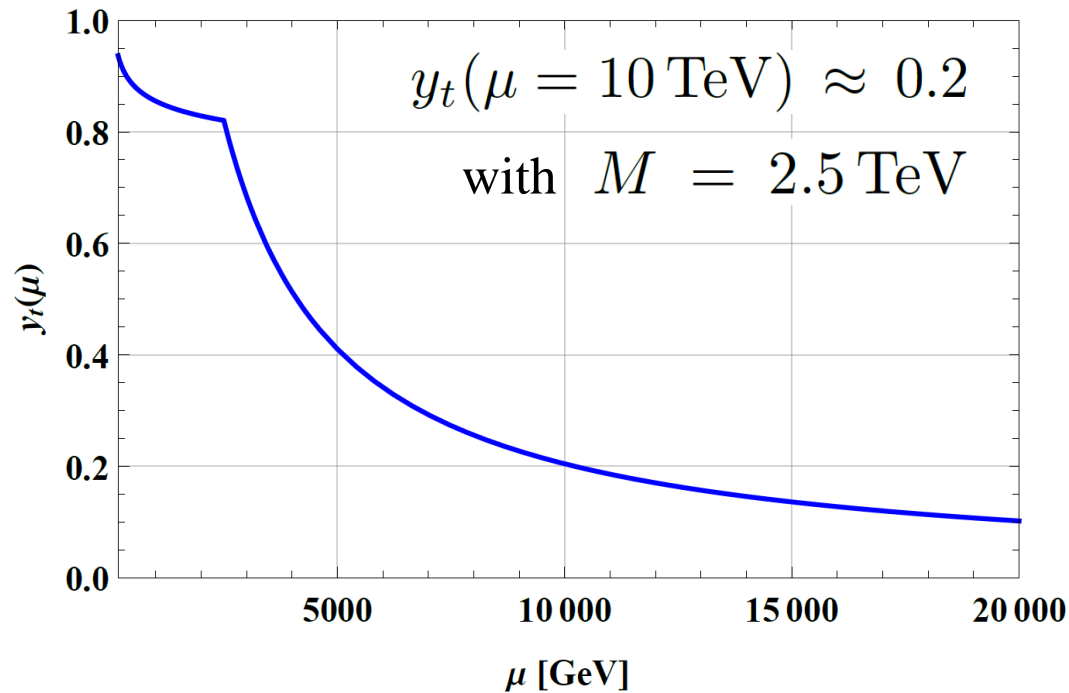
$$y_t = y_t(k^2)$$

Zoom in the Top Yukawa vertex

		
Modification	Large y_t running	y_t from dim-6 op.
New degrees of freedom	Top-philic bosons	New bosons and fermions

Large y_t running

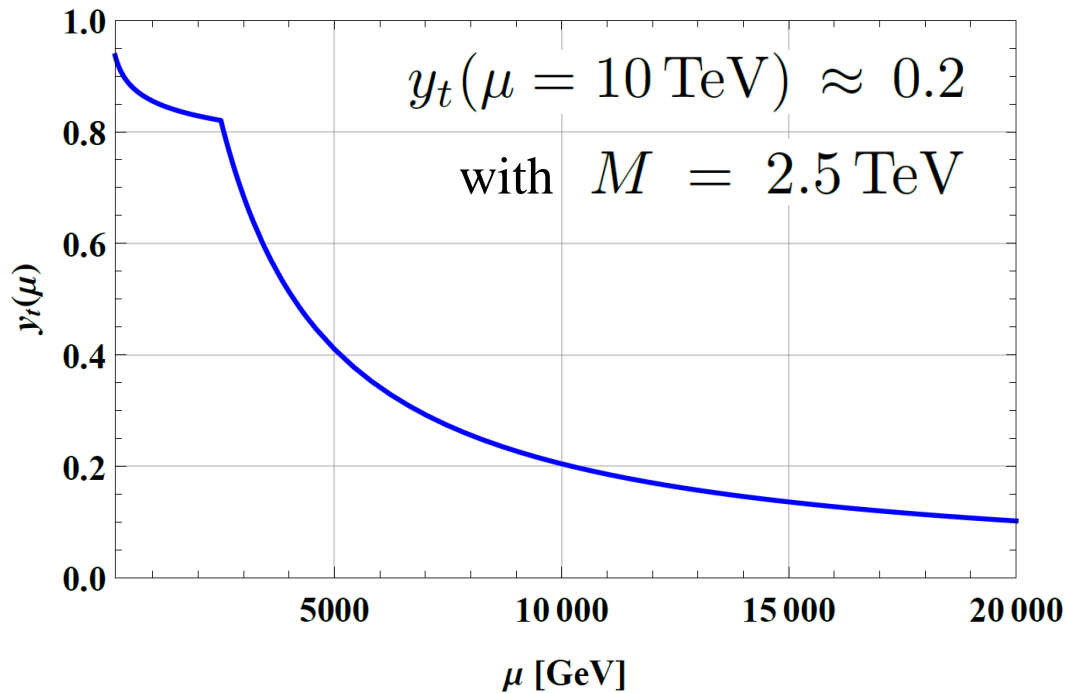
Strongly interacting top-philic boson



$$\frac{d y_t(\mu)}{d \ln \mu} = \frac{y_t(\mu)}{16\pi^2} \left(\frac{9}{2} y_t^2(\mu) - \frac{3(N^2 - 1)}{N} g_N^2 \right)$$

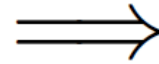
Top-loop becomes subleading with $\Lambda_{\text{NP}} = 10 \text{ TeV}$

Strongly interacting top-philic boson

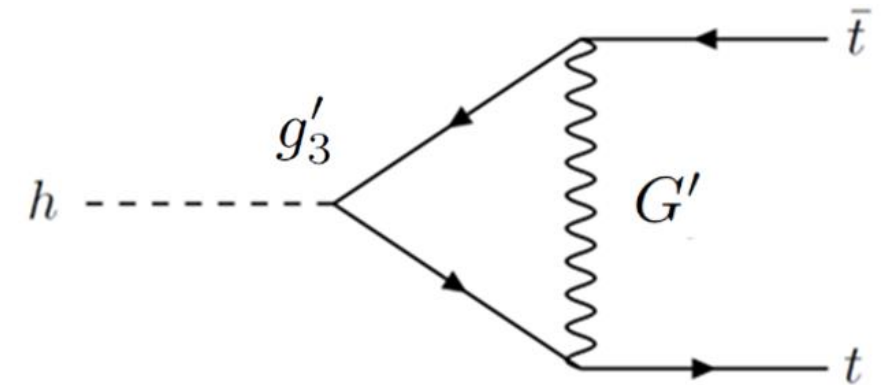


$$\frac{d y_t(\mu)}{d \ln \mu} = \frac{y_t(\mu)}{16\pi^2} \left(\frac{9}{2} y_t^2(\mu) - \frac{3(N^2 - 1)}{N} g_N^2 \right)$$

Top-loop becomes subleading with $\Lambda_{\text{NP}} = 10 \text{ TeV}$



Ex: Heavy gluons (Coloron)



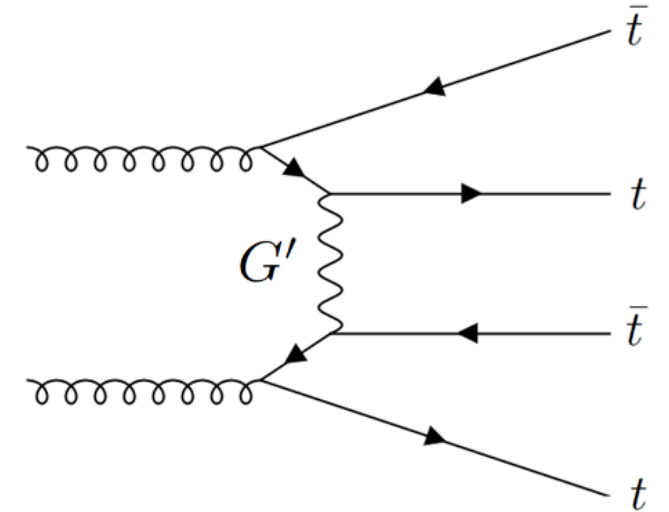
with the $SU(3)$ coupling $g'_3 \sim 4.5$

Direct consequences:

- Bound state of top-anti-top with the mass around $M = 2.5 \text{ TeV}$
- Enhancement in $4t$ cross section!!

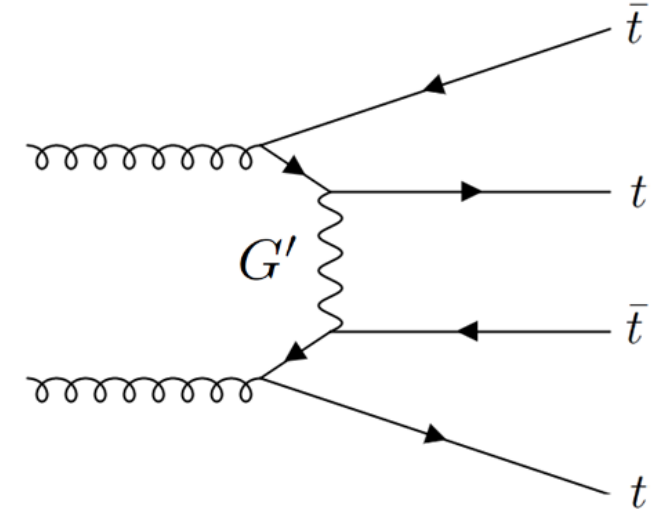
Four top quarks cross section

- Broad resonances (G' and H_t) with $\Gamma/M \gg 10\%$
→ hard to perform resonance search
- Inclusive measurement of rare SM processes such as $4t$
→ final state with two leptons of the same electric charge or with more than two leptons



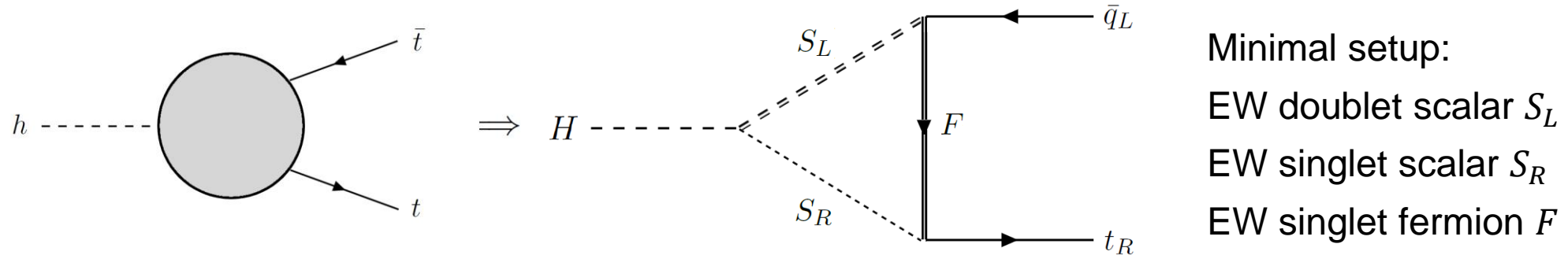
Four top quarks cross section

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→ final state with two leptons of the same electric charge or with more than two leptons
- Standard Model prediction: 12.0 ± 2.4 fb
- ATLAS with 139 fb^{-1} : 24_{-6}^{+7} fb & CMS with 137 fb^{-1} : 17_{-5}^{+5} fb
→ $\sigma_{t\bar{t}t\bar{t}} < 38$ (27) fb at 95% CL level from ATLAS (CMS)
- The bound can be reinterpreted as the bound on a vector color octet G'
$$\frac{g'_3}{M_{G'}} < 2.9 \text{ (2.5)} \text{ with } M_{G'} > 2 \text{ TeV} \Rightarrow \text{Main constraints for large top Yukawa running}$$



y_t from dim-6 operator

Top Yukawa arise from Dim-six operator



- The diagram introduces a dim-6 operator

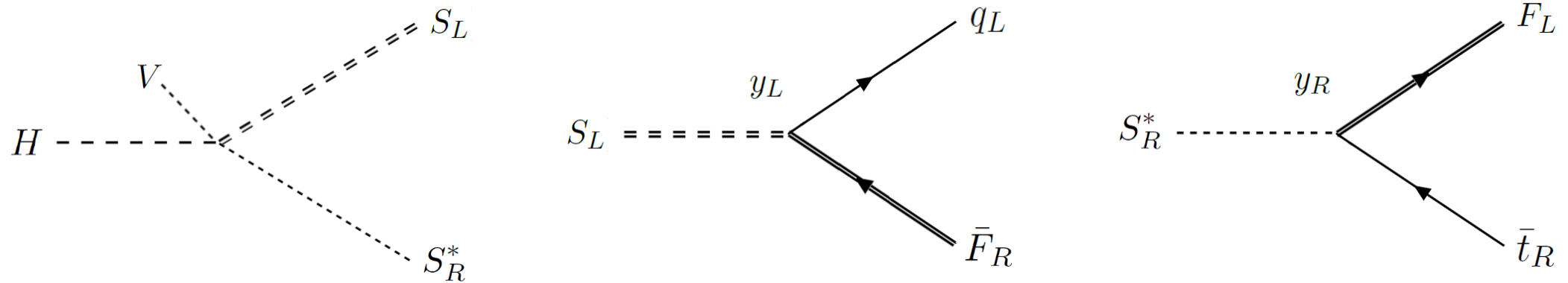
$$\sim \frac{y_L y_R}{16\pi^2} \frac{(H S_V \bar{q}_L S_F t_R)}{M^2} \Rightarrow \boxed{\frac{y_L y_R}{16\pi^2} \frac{V M_F}{M^2}} (\bar{q}_L H t_R)$$

$$= y_t \sim 1$$

from strong dynamics!!

Simplified Scalar Model

- At least three vertices are required



or written in Lagrangian

$$\mathcal{L}_{\text{int}} = -VS_R S_L^\dagger H - y_L \bar{q}_L S_L F_R - y_R \bar{t}_R S_R F_L + \text{h.c.} ,$$

where S_L is a doublet, S_R is a singlet, and F is a singlet vector-like fermion.

- Mass terms are also required

$$\mathcal{L}_{\text{mass}} = -M_L^2 |S_L|^2 - M_R^2 |S_R|^2 - M_F \bar{F}_L F_R + \text{h.c.} .$$

Simplified Scalar Model

- Focus on the neutral scalar components

$$\begin{aligned}\mathcal{L}_{\text{neutral}} &= |\partial s_L|^2 + |\partial s_R|^2 - M_L^2 |s_L|^2 - M_R^2 |s_R|^2 - V \langle H \rangle (s_L^* s_R + s_R^* s_L) \\ &= |\partial s_h|^2 + |\partial s_\ell|^2 - M_s^2 |s_h|^2 - m_s^2 |s_\ell|^2\end{aligned}$$

where the mass eigenstates are given by

$$\begin{pmatrix} s_L \\ s_R \end{pmatrix} = \begin{pmatrix} \cos\beta & -\sin\beta \\ \sin\beta & \cos\beta \end{pmatrix} \begin{pmatrix} s_{\text{heavy}} \\ s_{\text{light}} \end{pmatrix} = \begin{pmatrix} c_\beta & -s_\beta \\ s_\beta & c_\beta \end{pmatrix} \begin{pmatrix} s_h \\ s_\ell \end{pmatrix}$$

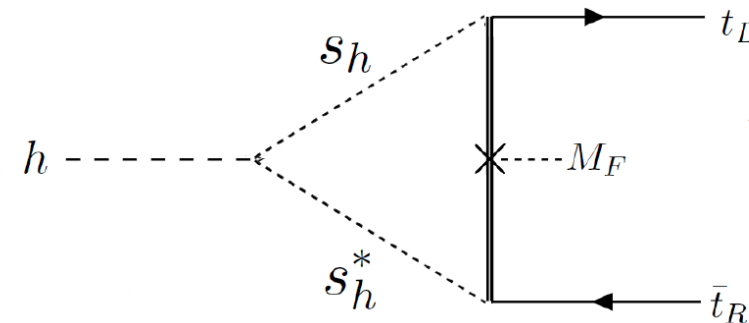
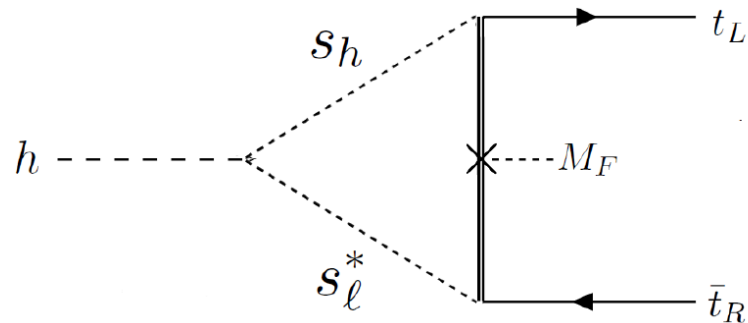
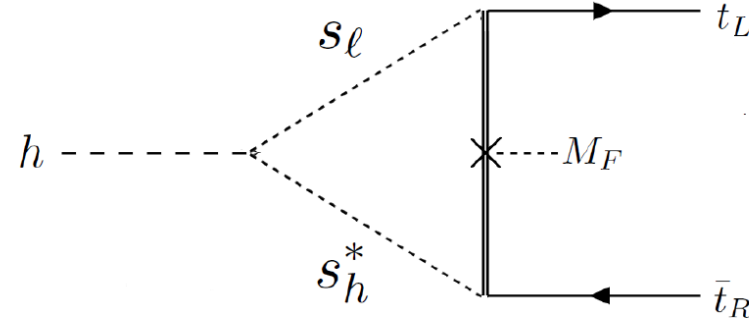
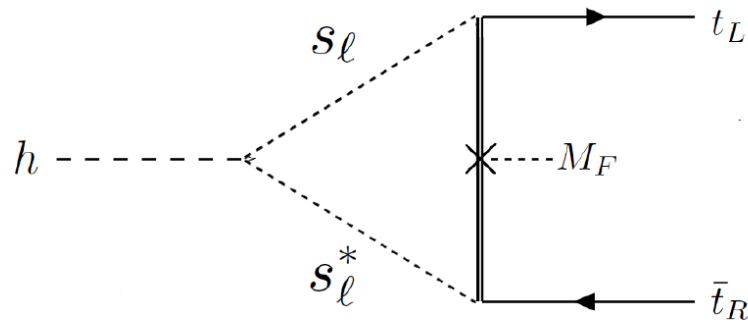
- The interaction terms also become

$$\mathcal{L}_{\text{trilinear}} = -\sqrt{2} V c_\beta s_\beta h |s_h|^2 + \sqrt{2} V c_\beta s_\beta h |s_\ell|^2 - \frac{V(c_\beta^2 - s_\beta^2)}{\sqrt{2}} h s_h^* s_\ell + \text{h.c.}$$

$$\mathcal{L}_{\text{fermion}} = -(y_L c_\beta \bar{t}_L s_h F_R + y_R s_\beta \bar{t}_R s_h F_L) - (-y_L s_\beta \bar{t}_L s_\ell F_R + y_R c_\beta \bar{t}_R s_\ell F_L) + \text{h.c.}$$

Generate the Top Yukawa coupling

- The original one-loop diagram is decomposed to the four diagrams below



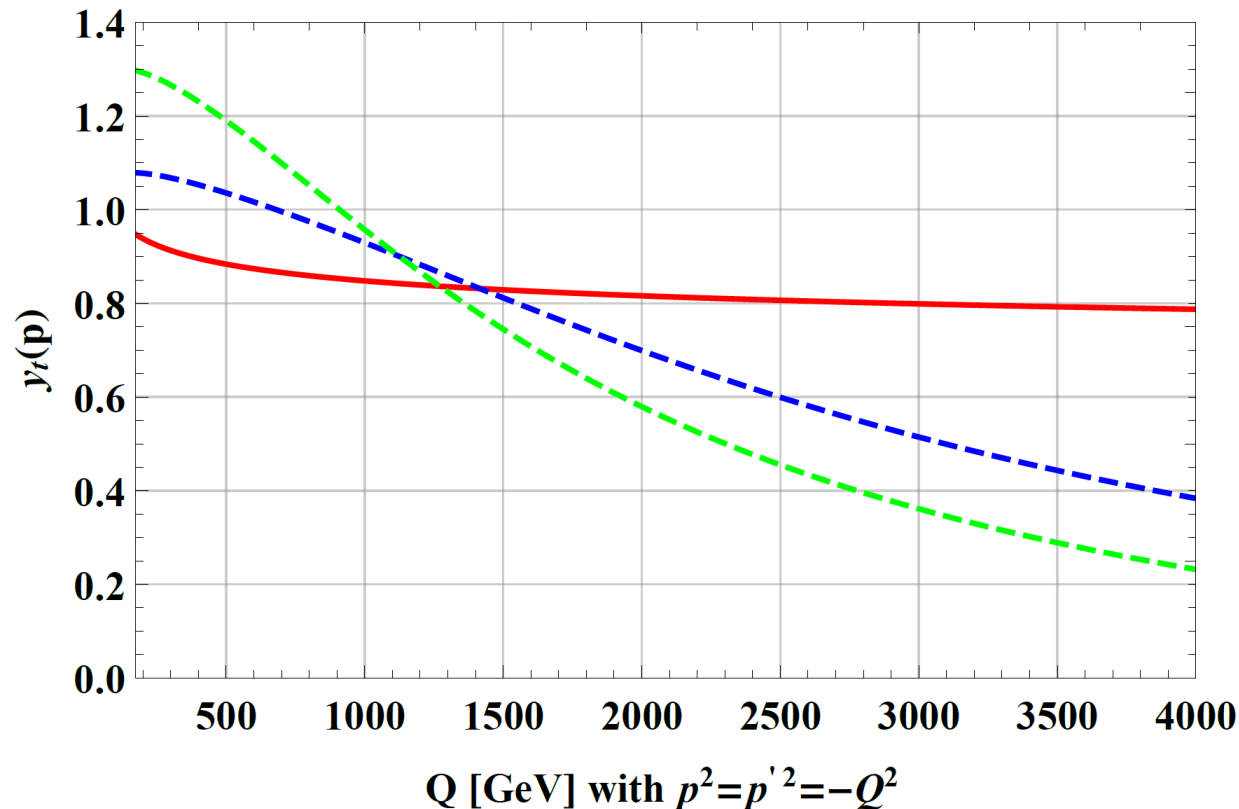
$$\Rightarrow y_t = V y_L y_R \left((c_\beta^2 - s_\beta^2)^2 \int [s_\ell, s_h, F] + 2 c_\beta^2 s_\beta^2 \int [s_\ell, s_\ell, F] + 2 c_\beta^2 s_\beta^2 \int [s_h, s_h, F] \right)$$

Top Yukawa from low scale to high scale

$M_F \sim 1550 \text{ GeV}, m_s \sim 600 \text{ GeV}, M_s \sim 1400 \text{ GeV}$ (BM1, blue)

$M_F \sim 850 \text{ GeV}, m_s \sim 450 \text{ GeV}, M_s \sim 1300 \text{ GeV}$ (BM2, green)

Two benchmarks are calculated and compared with SM running (red)

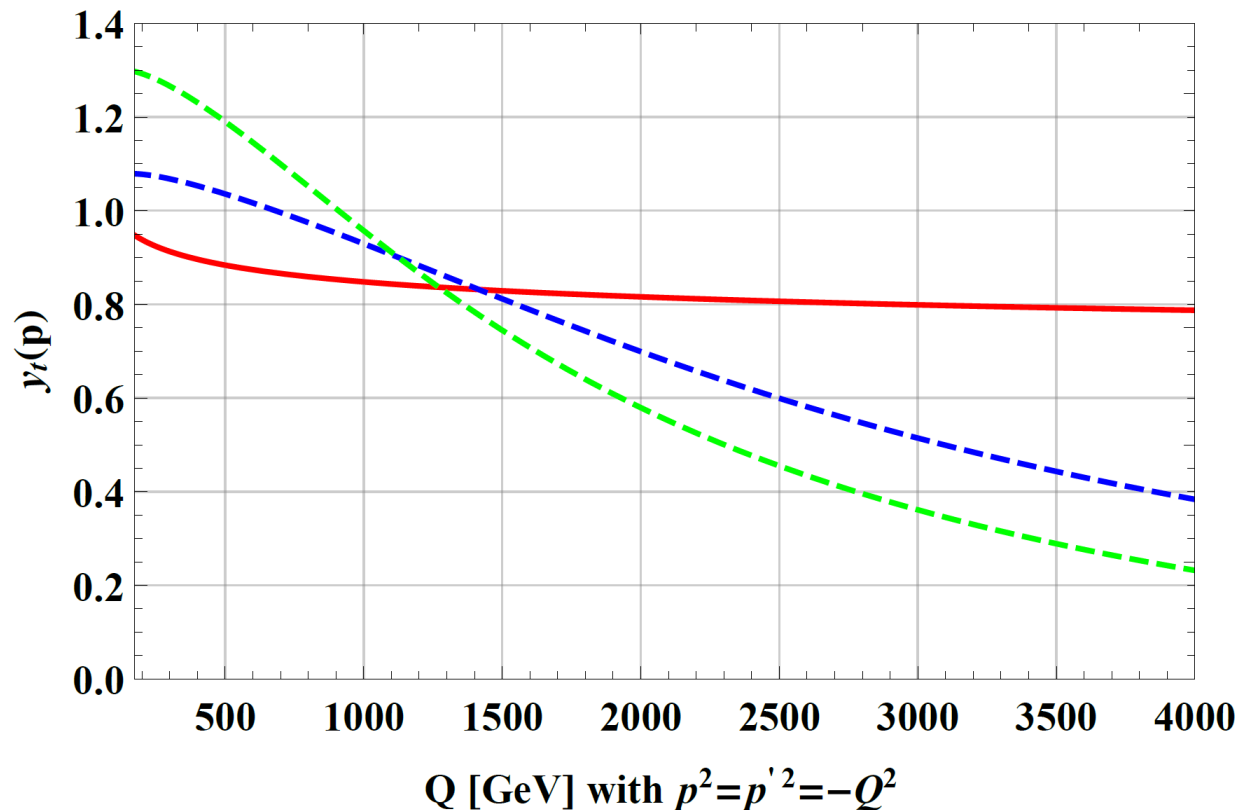


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Two benchmarks are calculated and compared with SM running (red)



- The value of y_t is normalized according to the correct top mass
- Larger y_t due to additional diagrams with extra Higgs insertion, which lead to

$$\mathcal{L}_{\text{top}} = c_6 (\bar{q}_L H t_R) + c_{6+4n} (H^\dagger H)^n (\bar{q}_L H t_R)$$

- **Main Constraint: top Yukawa measurement**

$$\kappa_t \equiv \frac{y_t}{y_t^{\text{SM}}} = 1 + \mathcal{O} \left(\frac{V^2 v^2}{M^4} \right)$$

with current bound $0.7 < \kappa_t < 1.1$ at 95% CL
(likely be weaker considering off-shell effect)

Running of the top quark mass

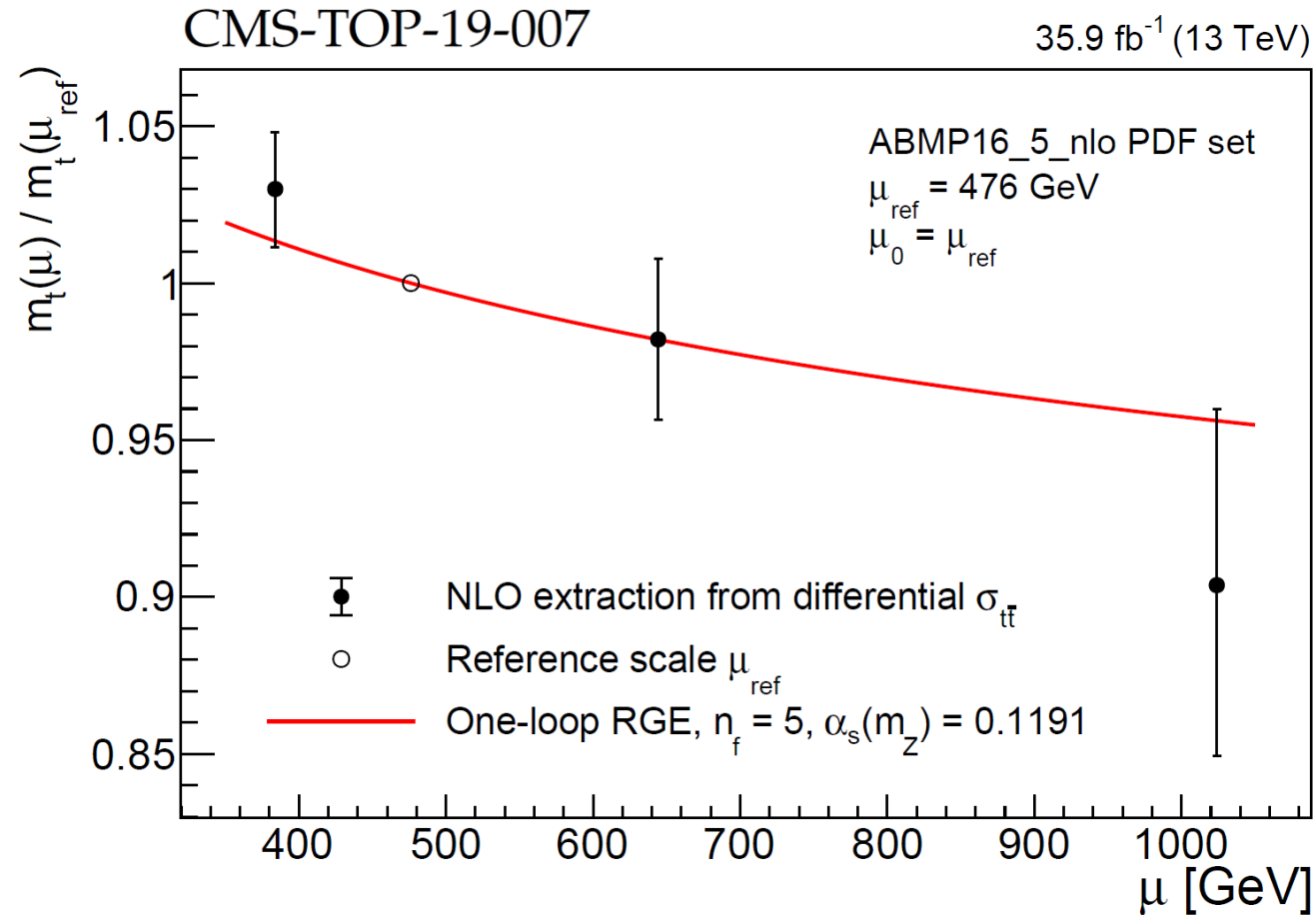
- The top quark mass is generated through

The diagram shows two Feynman diagrams for top quark mass generation, separated by a plus sign. Each diagram consists of a horizontal line representing a top quark, with an incoming arrow from the left labeled t_L and an outgoing arrow to the right labeled t_R . A vertical cross on the line indicates a mass insertion. In the left diagram, a dashed semi-circular arc labeled s_ℓ connects the line at two points. The left vertex is labeled $-y_L s_\beta$ and the right vertex is labeled $y_R c_\beta$. The segments of the line between the vertices are labeled F_R and F_L . Below this diagram is the expression $-y_L y_R c_\beta s_\beta \int [s_\ell, F]$. In the right diagram, a dashed semi-circular arc labeled s_h connects the line at two points. The left vertex is labeled $y_L c_\beta$ and the right vertex is labeled $y_R s_\beta$. The segments of the line between the vertices are labeled F_R and F_L . Below this diagram is the expression $y_L y_R c_\beta s_\beta \int [s_h, F]$.

$$\begin{aligned}
 & \text{Diagram 1 (Left): } t_L \rightarrow \text{---} \xrightarrow{-y_L s_\beta} \text{---} \xrightarrow{y_R c_\beta} \text{---} \rightarrow t_R \\
 & \quad \text{with a dashed arc } s_\ell \text{ connecting the two vertices.} \\
 & \quad \text{Below: } -y_L y_R c_\beta s_\beta \int [s_\ell, F] \\
 & + \\
 & \text{Diagram 2 (Right): } t_L \rightarrow \text{---} \xrightarrow{y_L c_\beta} \text{---} \xrightarrow{y_R s_\beta} \text{---} \rightarrow t_R \\
 & \quad \text{with a dashed arc } s_h \text{ connecting the two vertices.} \\
 & \quad \text{Below: } y_L y_R c_\beta s_\beta \int [s_h, F]
 \end{aligned}$$

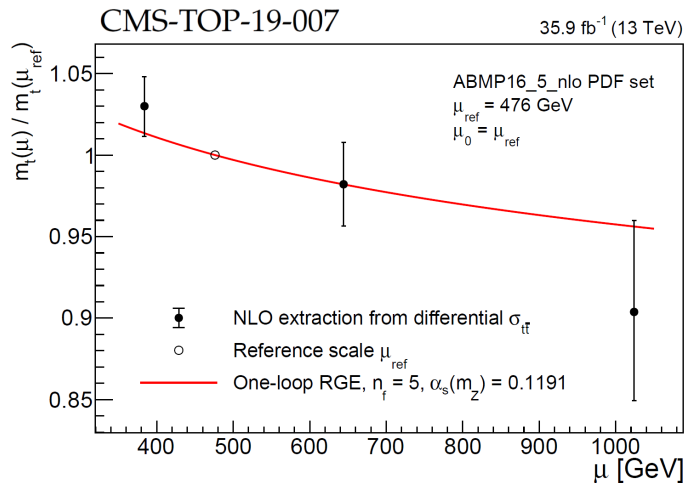
- The top quark mass m_t is radiatively generated in the intermediate scale
 \rightarrow Nontrivial running m_t at the high scale which will affect the $t\bar{t}$ cross section

Running of the top quark mass

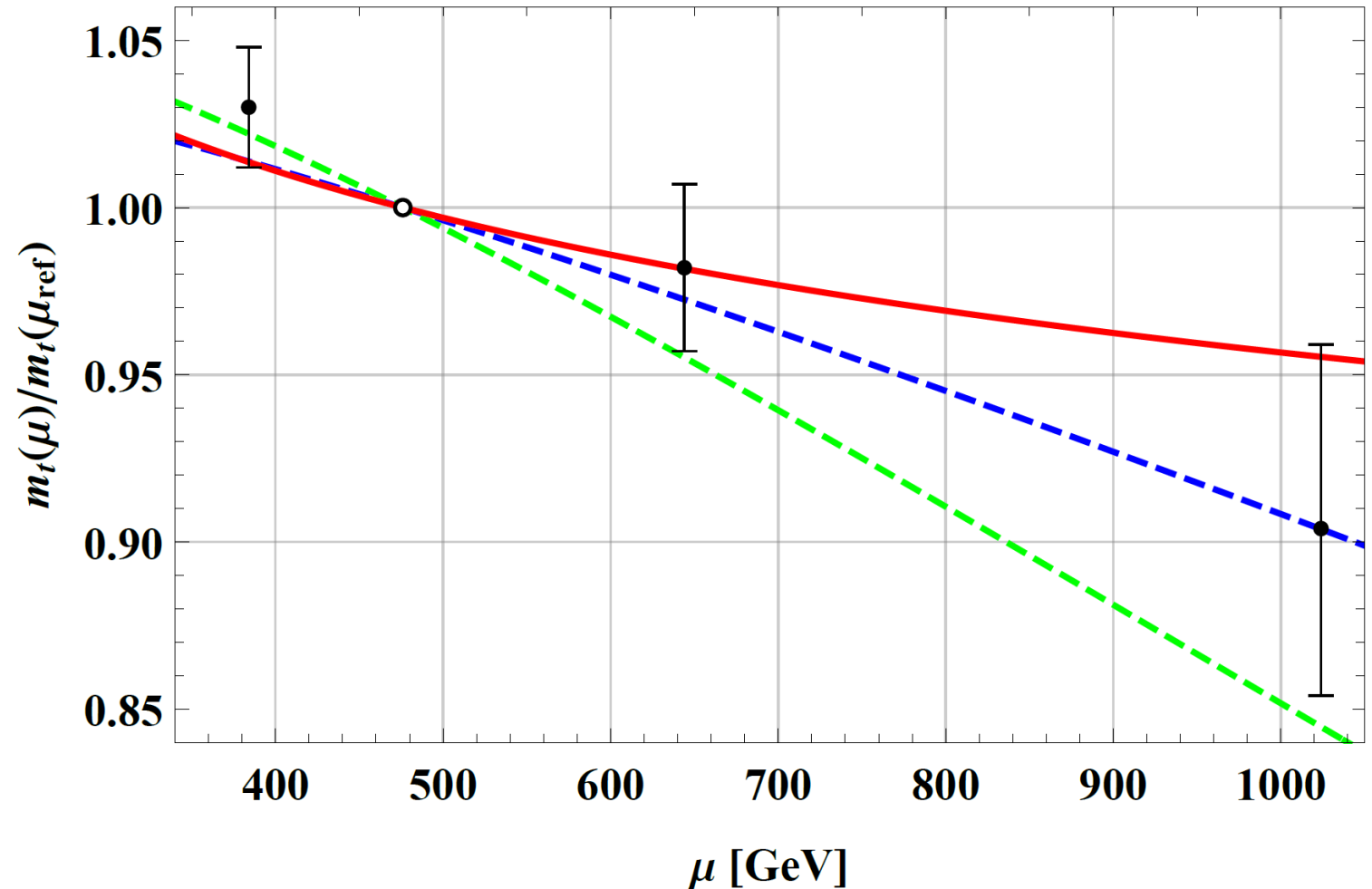
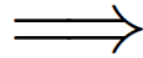


The first measurement from CMS !!

Running of the top quark mass



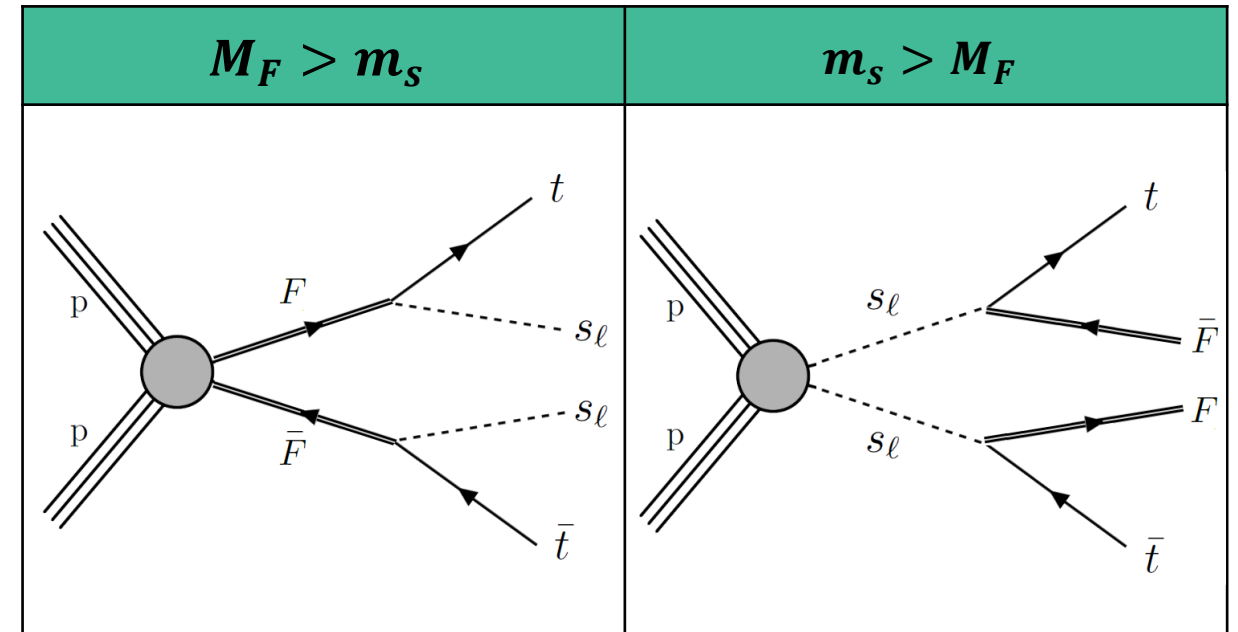
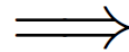
Direct test of the idea!!



Diverse phenomenology

- Phenomenology are determined by the lightest scalar s_ℓ and vector-like fermion F
- The quantum number and the spectrum of the new d.o.f. are not determined
- They can have diverse “Quantum number” and “Spectrum”

Scalar	Fermion
$(1, 0)$	$(3, +2/3)$
$(1, -1)$	$(3, -1/3)$
$(3, -1/3)$	$(1, -1)$
$(3, +2/3)$	$(1, 0)$



Warning: they might be broad resonances which are not under current search strategy.

Conclusion

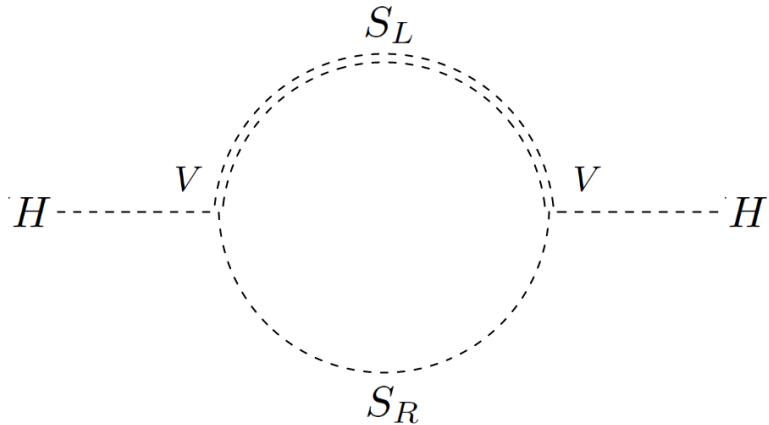
- Top quark is the most important part of the hierarchy problem
- Traditionally, top partners are introduced to **cancel** the top-loop contribution
- Alternative: **modify the running** of y_t to lower the top-loop contribution
- What should show up at Λ_t : **Top partner** → **New d.o.f.** related to the top quark
- Features of the alternative scenario (y_t from dim-6 operator)
 - **New bosons and VL fermions** accompanied with **strong interaction** are required
 - Direct impact on the **top Yukawa coupling** and **running of the top quark mass**
 - **Diverse phenomenology** to be explored (new methods for broad resonances required)
 - Even more diverse taking (1) scalar bosons → vector bosons (2) singlet → multiplet

Warning: It can NOT solve the hierarchy problem on its own but assist existing models.

Back up

Additional contribution

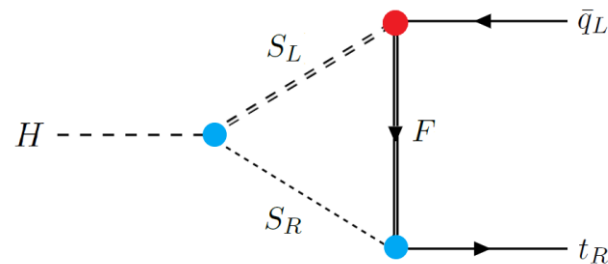
- The trilinear couplings between the Higgs and scalars will introduce a new loop


$$\Rightarrow \Delta m_H^2|_{\text{scalar}} \sim \frac{1}{16\pi^2} V^2 \ln \left(\frac{\Lambda_{\text{NP}}^2}{M^2} \right)$$

- This loop is however logarithmically sensitive to NP and will not reintroduce a HP
- Assuming a low-scale UV completion, the correction leads to 7% tuning in both benchmarks, which is at the same order as the top-quark tuning. Therefore, the new scalar loops do not worsen the tuning.

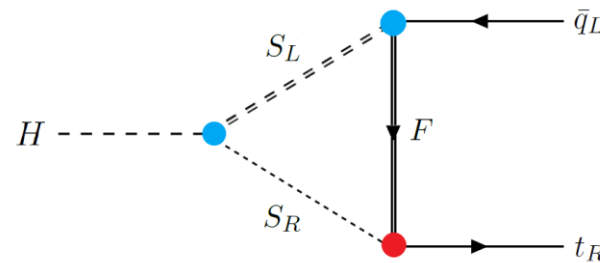
Top Yukawa from strong dynamics

- If y_t comes from pure strong dynamics, then even at one-loop level we expect $y_t \sim 4\pi$
- A **suppression ε** is required between the **strong** and **weak** sector to get $y_t \sim 1$
- Three possibilities



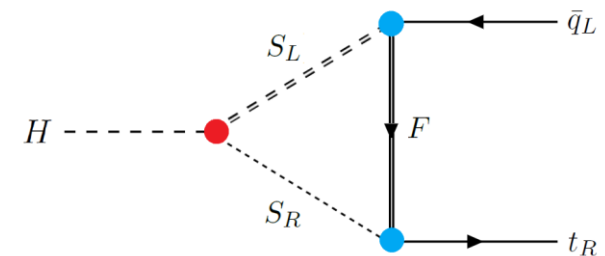
Strong sec.
 S_L, S_R, F
 H, t_R

Weak sec.
 q_L



Strong sec.
 S_L, S_R, F
 H, q_L

Weak sec.
 t_R



Strong sec.
 S_L, S_R, F
 q_L, t_R

Weak sec.
 H

small M without large κ_t

Strongly coupled UV theory

- A Top seesaw-like model based on $SU(3)_L \times SU(2)_R$ global symmetry with bound states

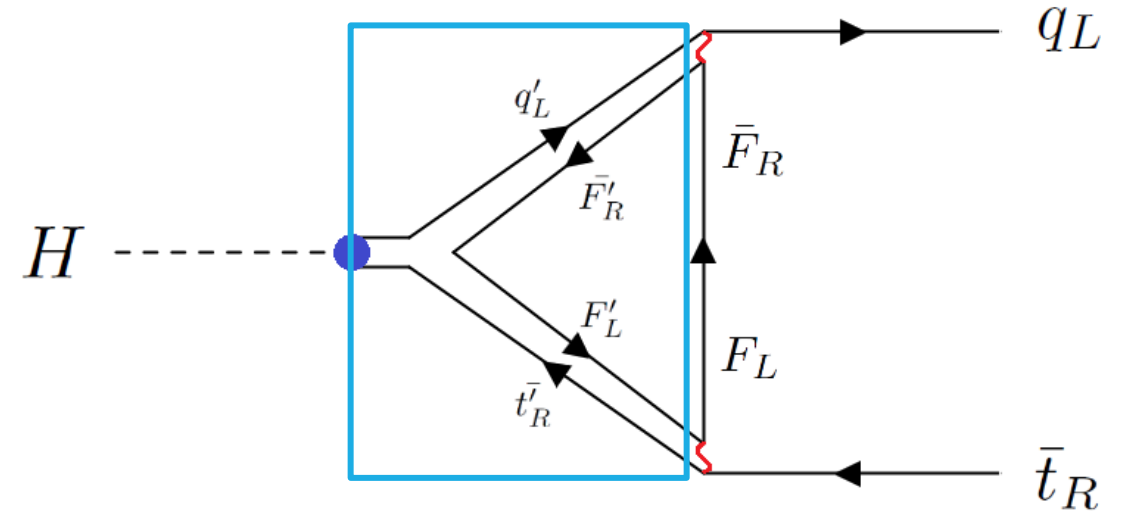
Weak sector:

$$H, Q_L = \begin{pmatrix} F_L \\ t_L \\ b_L \end{pmatrix}, \quad Q_R = \begin{pmatrix} F_R \\ t_R \end{pmatrix}$$

Strong sector:

$$\Phi, Q'_L = \begin{pmatrix} F'_L \\ t'_L \\ b'_L \end{pmatrix}, \quad Q'_R = \begin{pmatrix} F'_R \\ t'_R \end{pmatrix}$$

$$\Phi = \bar{Q}'_R Q'_L = \begin{pmatrix} S_V^* & S_R^* \\ S_L & S_H \end{pmatrix}$$



\Rightarrow

$$\mathcal{L}_\Phi = |\partial\Phi|^2 - \tilde{M}(\mu)^2 |\Phi|^2 - \tilde{\lambda}(\mu) |\Phi|^4 - \tilde{y}(\mu) \bar{Q}'_L \Phi Q'_R$$

$$\supset 2\tilde{\lambda} \langle S_V \rangle (S_R S_L^\dagger S_H) - \tilde{y} \bar{q}'_L S_L F'_R - \tilde{y} \bar{t}'_R S_R F'_L$$

$$\tilde{\lambda}(\mu) = \frac{16\pi^2}{NC}, \quad \tilde{y}(\mu) = \frac{4\pi}{\sqrt{NC}}, \quad C = \ln \left(\frac{M'^2}{\mu^2} \right)$$